Prototype and Feature Generation

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International Autumn Meeting on Power, Electronics and Computing 2014 IEEE XVI ROPEC

November 5, 2014

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Introduction

The Classification task consists in associating objects with predefined categories (e.g. Text classification). Among the variety of classification models proposed so far, nearest-neighbors (NN) methods are among the most popular ones.



Figure: Example of the kNN method.

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Introduction

Altough NN methods are highly effective, and easy to implement, they present some issues that hinder their application to certain types of problems:

- High computational time requirements.
- High storage requirements.
- Sensitivity to noisy (e.g., misclassified instances and outliers).

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Introducción

There are different techniques for data reduction.



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Related Work

- There are a number of approaches for prototype generation (PG) such as incremental, decremental, mixed (e.g., GENN, PSCSA, PSO methods).
- Triguero et al. review and classify most of the existing PG methods up to 2012, additionally, a taxonomy and experimental comparison of these methods is also reported.
- On the other hand, for the feature extraction there are several approaches such as evolutionary algorithms.

Both tasks, prototype generation and feature extraction, are performed independently due to computational cost. However, there are methods that try to combine both techniques.

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- We present a extension of the Simultaneous Generation of Prototypes and Features through Genetic Programming (SGPFGP) method. The goal is to learn class-specific prototypes and features for pattern classification by NN through multi-objective optimization.
- The method is based on NSGA-II algorithm and SGPFGP method.
- We use genetic programming to the generation of prototypes and features by combining instances and features, respectively.
- Our proposal tries to find a good trade-off between accuracy, reduction of instances and features.
- The main difference of the multi-objective approach against the SGPFGP method is the multi-objective optimization.

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Figure: Flow chart of the multi-objective approach.

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Figure: Representation of an individual: class-specific prototype-feature trees.

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Figure: Prototype repersentation (left): instances are combined, feature representation (right): features are combined

- The function set for combining instances and features is the following set of operators: {+,-,*,/(Protected), Min, Max}.
- The Fitness function was the classification performance obtained by a 1NN when classify in all instances in a validation set.

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Experimental Framework

Table: Summary of features for the 59 data sets of the considered benchmark.

	Small	Large
# data sets	40	19
# Classes	[2, 15]	[2, 28]
# Instances	[101, 1,728]	[2,201, 19,020]
# Attributes	[3, 90]	[2, 85]

- Number of generations is 100.
- Population size is set to 200.
- Maximum tree depth is fixed to 3.
- Statistically test: Wilcoxon signed-rank, with confidence level of 95 %.

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Table: Average classification accuracy for SGPFGP and reference methods.

	Multi-Objective	SGPFGP	1NN	
Small	$70,\!84\pm17,\!24$	$71,\!97 \pm 15,\!76$	$73{,}48 \pm 16{,}64$	
Large	$76{,}19\pm21{,}25$	$80{,}25 \star \pm 19{,}93$	$80{,}60 \pm 22{,}24$	
statistically simplificant difference				

statistically significant difference.

Table: Average instance reduction rates obtained by the considered methods.

	Multi-Objective	SGPFGP
Small	$98{,}43 \pm 1{,}65$	$98,\!39 \star \pm 1,\!37$
Large	$99{,}82\pm0{,}16$	$99{,}43 \star {\pm}0{,}09$

* statistically significant difference.

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Table: Average feature reduction rates obtained by the considered methods.

	Multi-Objective	SGPFGP
Small	$88,\!65\pm7,\!52$	$42{,}62\star\pm5{,}13$
Large	$89{,}74\pm12{,}36$	$41,\!45\star\pm\!12,\!76$

 \star statistically significant difference.

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The Chess data set is associated to a binary classification task (2-classes) that contains 3,196 instances described by 36 attributes.



Figure: Feature space and prototype of class 1.

Figure: Feature space and prototype of class 2.



Figure: Pareto front of Chess data set (3-D)

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Figure: Pareto front of Chess data set (2-D) (Accuracy, Instance reduction)

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Conclusions

- The multi-objective is able to reduce data dimensionality and the number of training instances without compromising the classification performance.
- Instance-reduction performance of multi-objective approach is very close to the optimal reduction rates (i.e., one instance per class).
- The multi-objective reduces about 90% data sets dimensionality. Building new features that are more informative for designing NN classifiers.
- The multi-objective method outperforms statistically in terms of instance and feature reduction rate to SGPFGP method.

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Future Work

- Explore the use of distances for different types of data such as Value Difference Metric or Heterogeneous Value Difference Metric.
- Use other metrics to evaluate the classification performance such as the area under the curve.
- Mixing the different solutions obtained for each Pareto front, in order to exploit each of the solutions generated.

Questions

Questions? Thank you for your attention! Inno nP

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