

# Machine Learning through Genetic Programming

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# Contents

- **Evolutionary algorithms**
  - Introduction
- **Genetic Algorithms**
  - Introduction
- **Genetic programming**
  - Introduction
- **Some applications of GP 1: Machine learning**
  - GP for classification
  - Generation of prototypes / instance selection
  - Ensemble generation
  - Term-weighting scheme learning
- **Applications of GP 2: Computer vision**
  - Visual descriptors
  - Spatio-temporal descriptors
  - CBIR
- **Applications of GP 3: Text-mining**
  - Term-weighting information retrieval
  - Term-weighting text-classification

Machine Learning through Genetic Programming

# **EVOLUTIONARY COMPUTATION**

# Evolutionary Computing

- EC Is the collective name for a range of **problem-solving** techniques based on principles of biological evolution, such as **natural selection** and **genetic inheritance**. These techniques are being increasingly widely applied to a variety of problems, ranging from practical applications in industry and commerce to leading-edge scientific research.

# Evolutionary Computing

- Trial and error problem solving approach:
  - While not\_satisfied\_with\_solution
    1. Generate candidate solution(s) for the problem at hand
    2. Evaluate the quality of the candidate solution (s)
  - Return best\_solution\_found

EC techniques generate new solutions according to (rough) analogies with biological evolution principles

# The Main Evolutionary Computing Metaphor

A given environment is filled with a population of individuals that strive for survival and reproduction

A problem is to be solved via stochastic trial-and-error, using a starting point a set of candidate solutions

## EVOLUTION

## PROBLEM SOLVING

Environment



Problem (search space)

Individual



Candidate Solution

Fitness

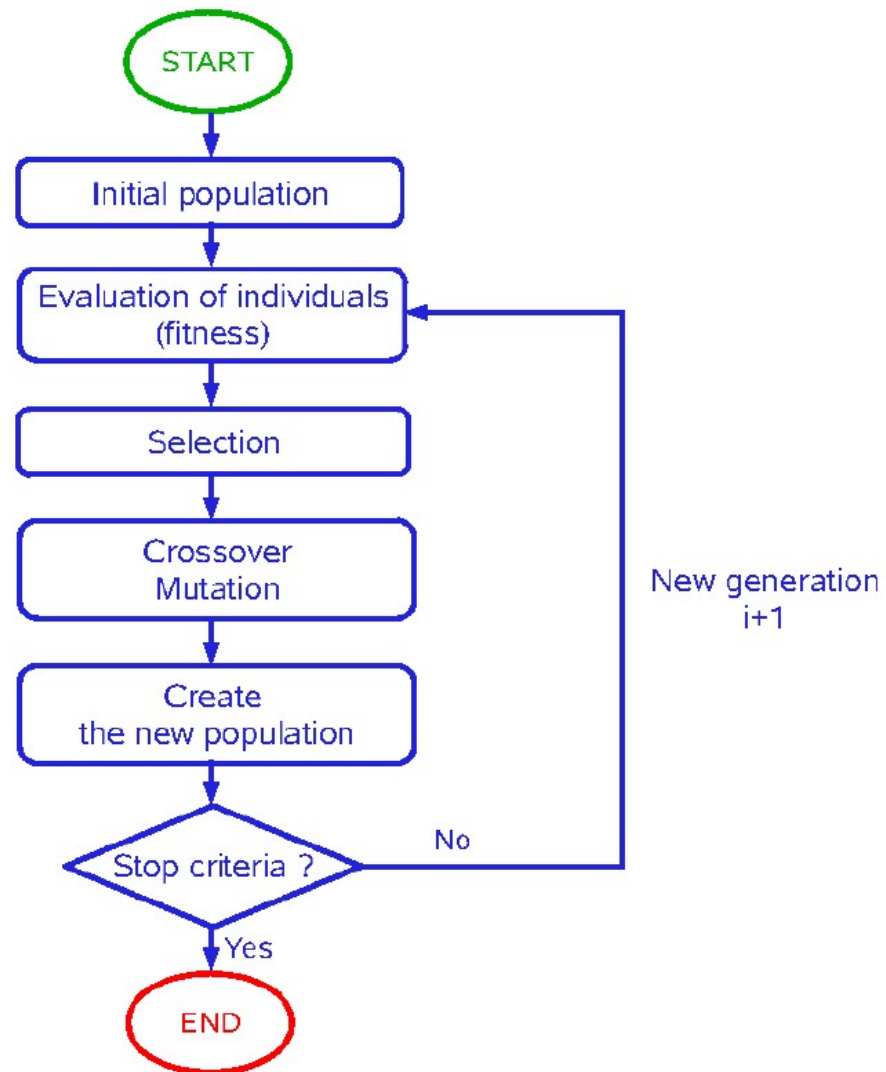


Quality of the solution

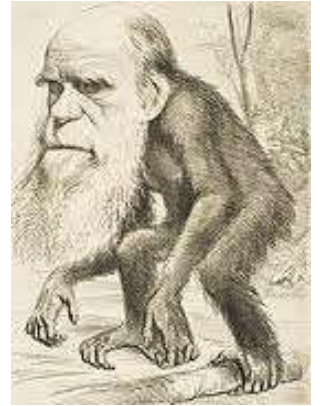
Fitness → chances for survival and reproduction

Quality → chance for seeding new solutions

# Generic EA

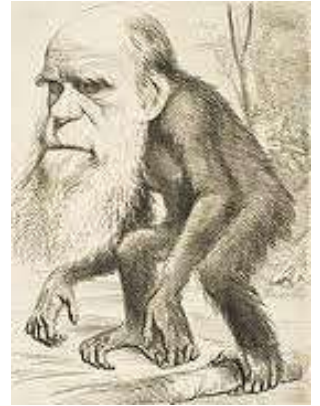


# Darwinian Evolution 1: Survival of the fittest



- All environments have finite resources  
(i.e., can only support a limited number of individuals)
- Lifeforms have basic instinct/ lifecycles geared towards reproduction
- Therefore some kind of selection is inevitable
- Those individuals that compete for the resources most effectively have increased chance of reproduction

# Darwinian Evolution 2: Diversity drives change



- Phenotypic traits:
    - Behaviour / physical differences that affect response to environment
    - Partly determined by inheritance, partly by factors during development
    - Unique to each individual, partly as a result of random changes
  - If phenotypic traits:
    - Lead to higher chances of reproduction
    - Can be inherited
- then they will tend to increase in subsequent generations,
- leading to new combinations of traits ...

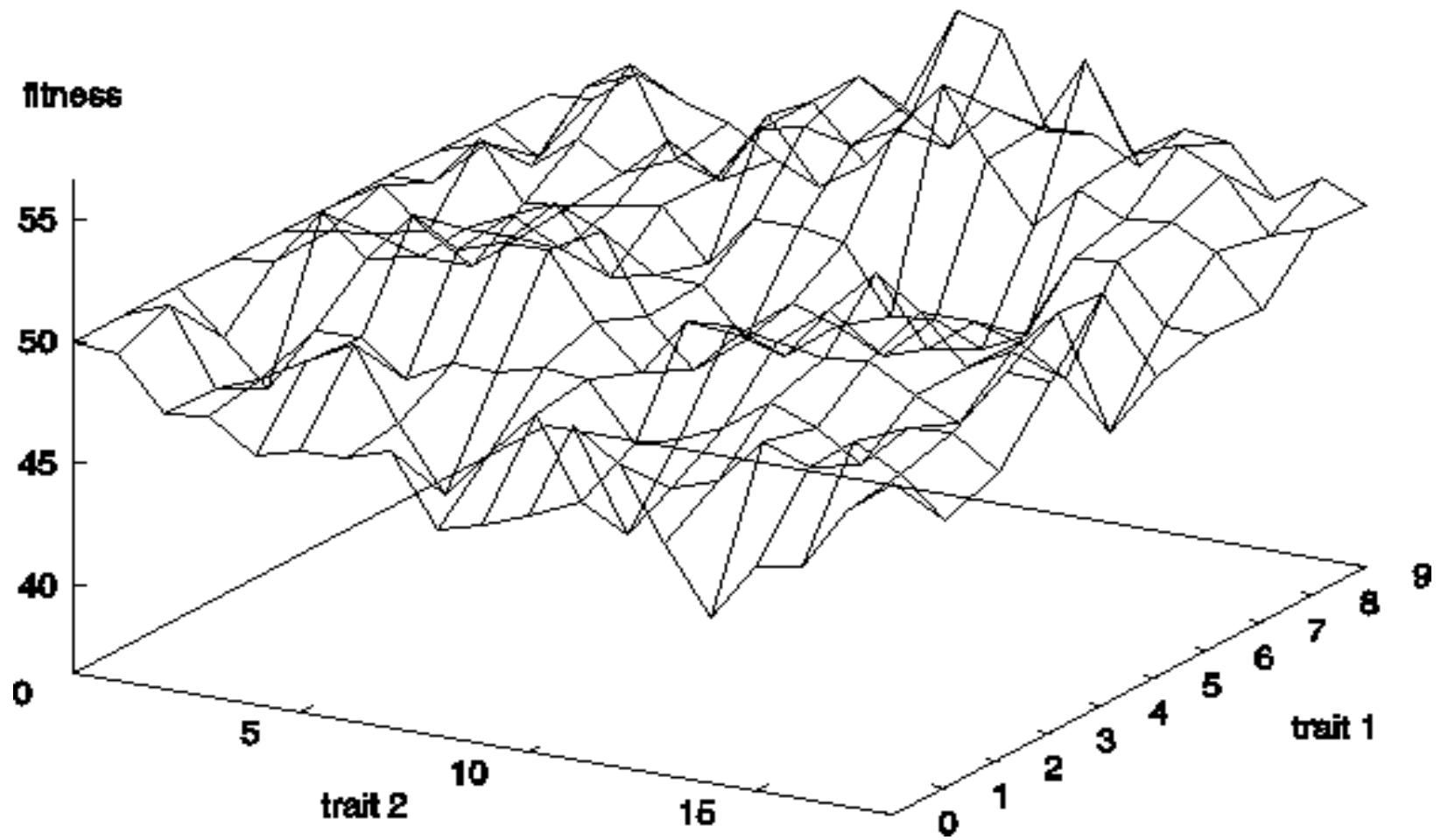
# Darwinian Evolution: Summary

- Population consists of diverse set of individuals
- Combinations of traits that are better adapted tend to increase representation in population
  - Individuals are “units of selection”
- Variations occur through random changes yielding constant source of diversity, coupled with selection means that:
  - Population is the “unit of evolution”
- Note the absence of “guiding force”

# Adaptive landscape metaphor (Wright, 1932)

- Can envisage population with  $n$  traits as existing in a  $n+1$ -dimensional space (landscape) with height corresponding to fitness
- Each different individual (phenotype) represents a single point on the landscape
- Population is therefore a “cloud” of points, moving on the landscape over time as it evolves - adaptation

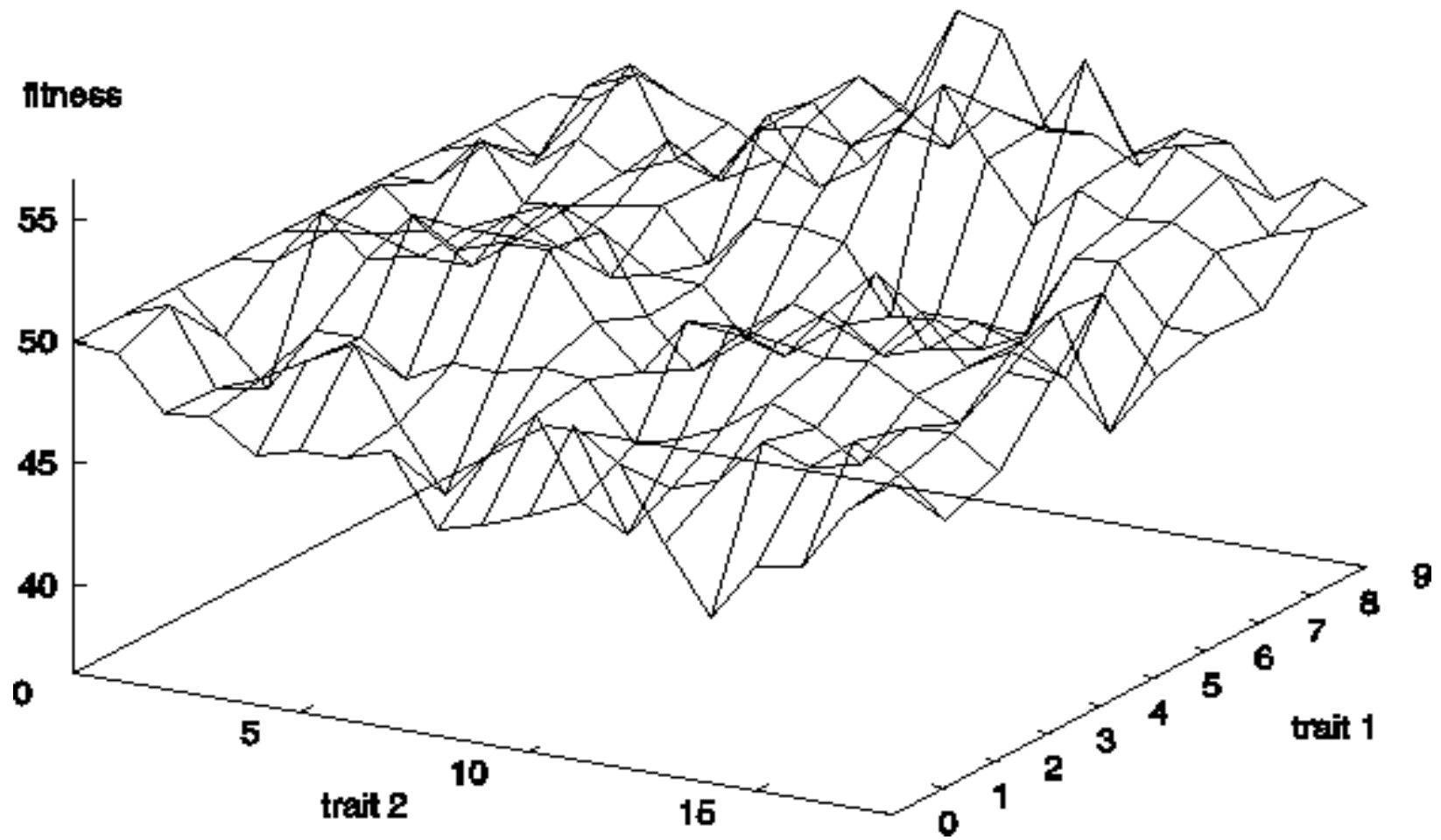
# Example with two traits



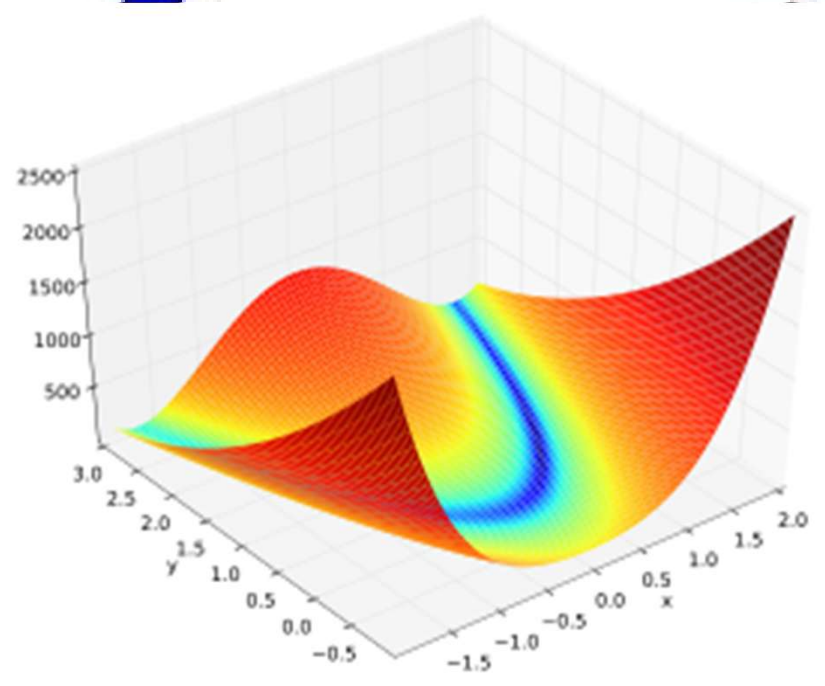
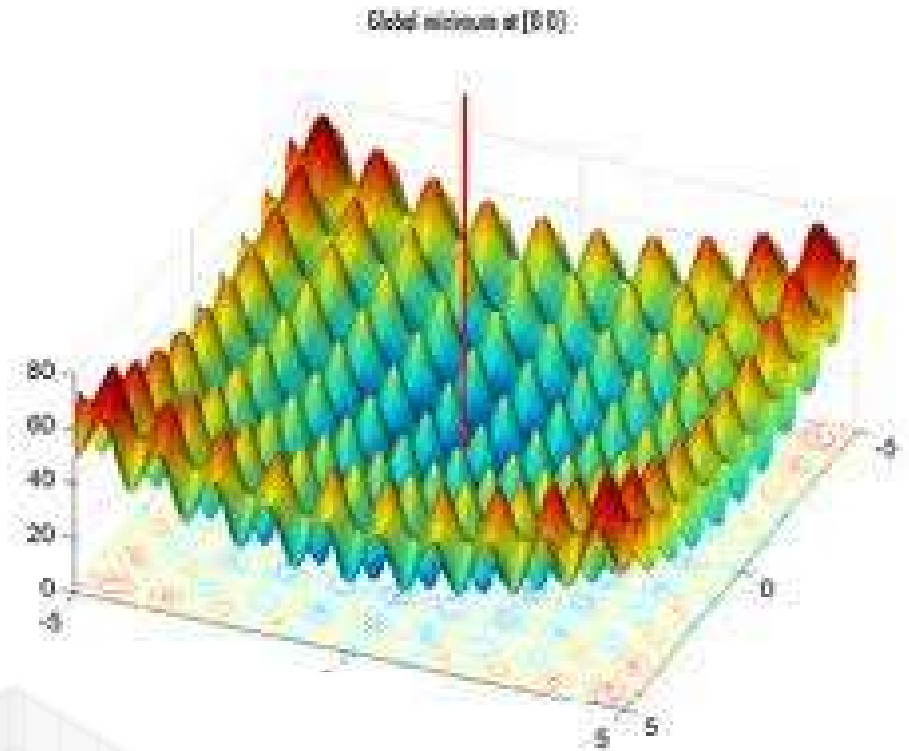
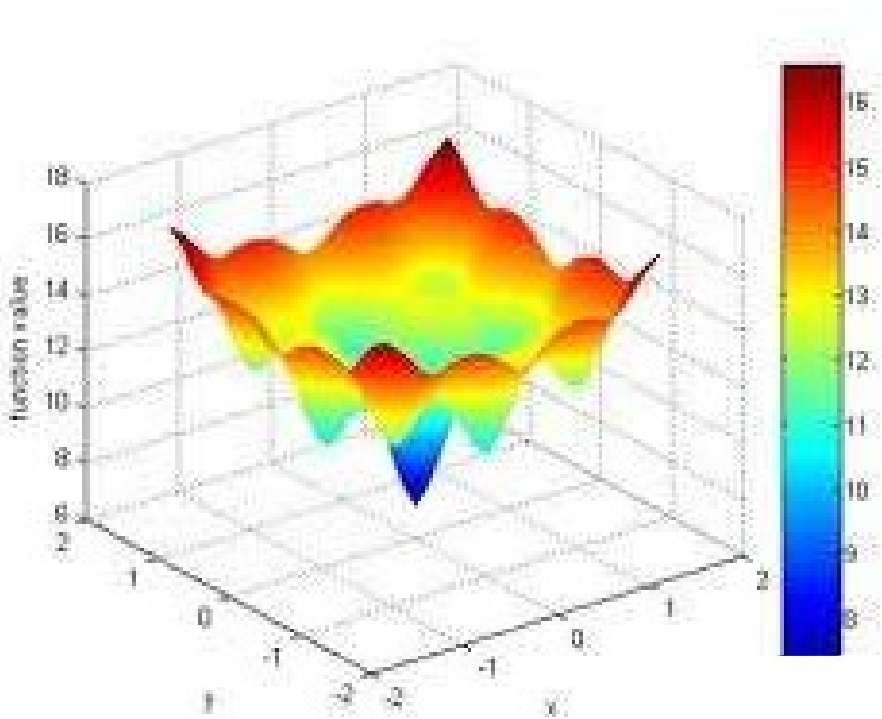
# Adaptive landscape metaphor (cont'd)

- Selection “pushes” population up the landscape
- Genetic drift:
  - random variations in feature distribution (+ or -) arising from sampling error
  - can cause the population “melt down” hills, thus crossing valleys and leaving local optima

# Example with two traits



# Link to optimization



# EAs in a nutshell

- A population of individuals exists in an environment with limited resources
- ***Competition*** for those resources causes selection of those ***fitter*** individuals that are better adapted to the environment
- These individuals act as seeds for the generation of new individuals through recombination and mutation

# EAs in a nutshell

- The new individuals have their fitness evaluated and compete (possibly also with parents) for survival.
- Over time *Natural selection* causes a rise in the fitness of the population

# EAs in a nutshell

- EAs fall into the category of “generate and test” algorithms
- They are stochastic, population-based algorithms
- Variation operators (recombination and mutation) create the necessary diversity and thereby facilitate novelty
- Selection reduces diversity and acts as a force pushing quality

# Brief History: the ancestors

- 1948, Turing:  
proposes “genetical or evolutionary search”
- 1962, Bremermann  
optimization through evolution and recombination
- 1964, Rechenberg  
introduces evolution strategies
- 1965, L. Fogel, Owens and Walsh  
introduce evolutionary programming
- 1975, Holland  
introduces genetic algorithms
- 1992, Koza  
introduces genetic programming

# Adequate problems for EC

- (Hard) combinatorial optimization
- Multi-objective optimization
- Constrained optimization
- Tough (differentiable) objective functions
- Multimodal objective functions
- ...

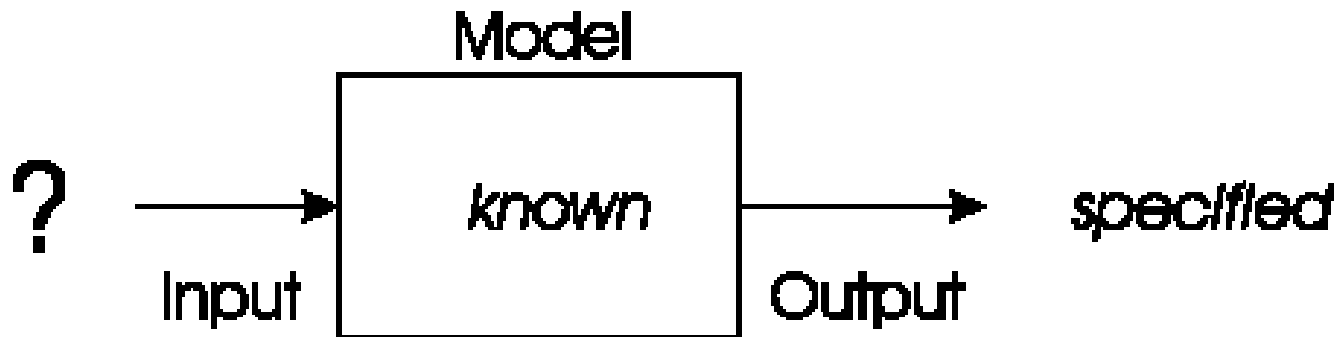
Domains/applications requiring fast response

NP- problems

Requiring (almost) accurate solutions

# Problem type 1 : Optimization

- We have a model of our system and seek inputs that give us a specified goal



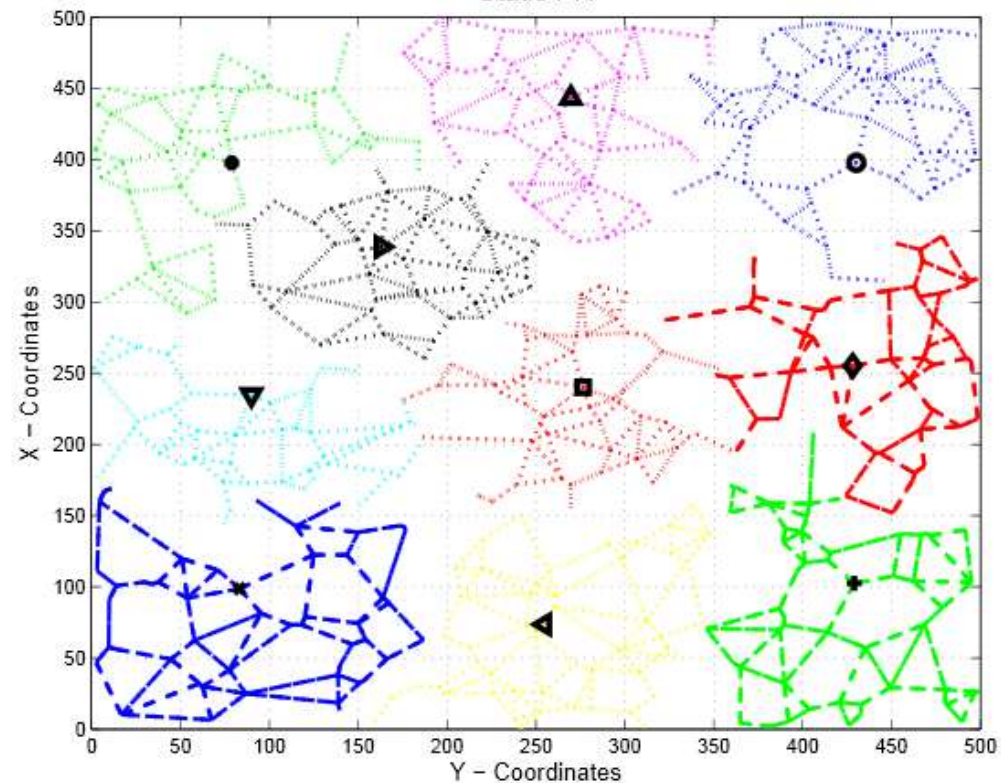
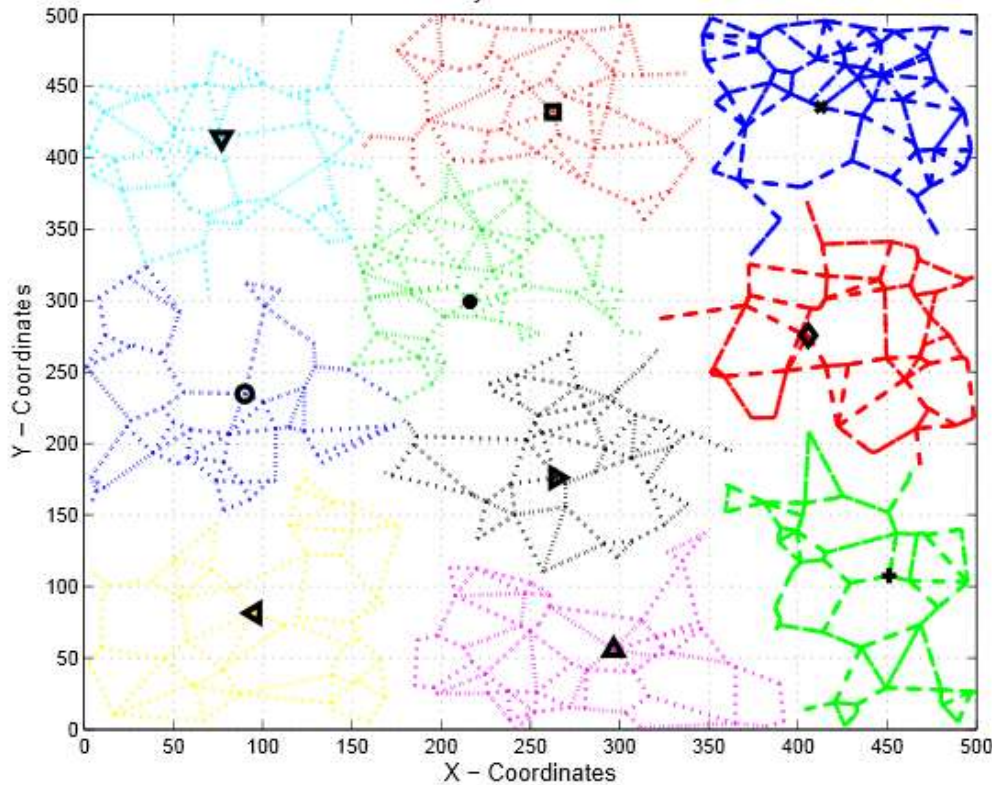
- e.g.
  - time tables for university, call center, or hospital
  - design specifications, etc etc

# Problem type 1 : Optimization

$$\min_{X \in \Pi} \quad f(X) = \max_{k \in K} \max_{i \in X_k} \{d_{c(k),i}\}$$

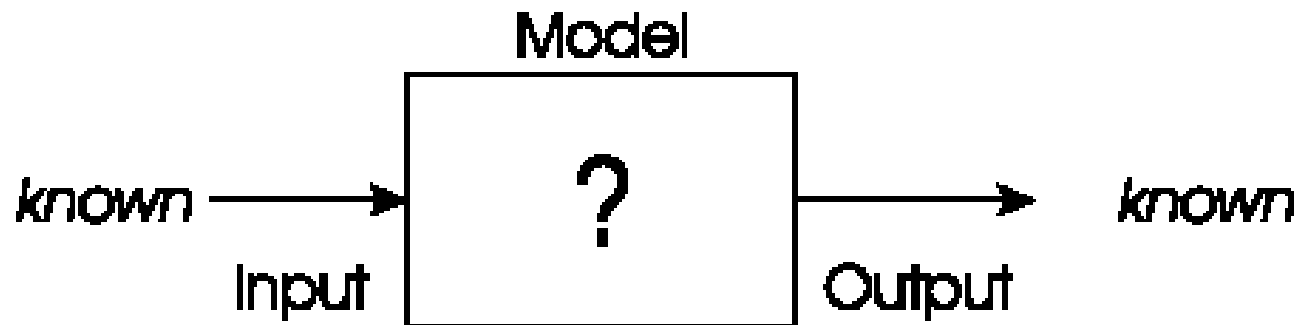
$$\text{subject to } \frac{w^a(X_k)}{\mu^a} \in [1 - \tau^a, 1 + \tau^a] \quad k \in K, a \in A$$

$$G_k = G(V_k, E(V_k)) \text{ is connected} \quad k \in K$$



# Problem types 2: Modelling

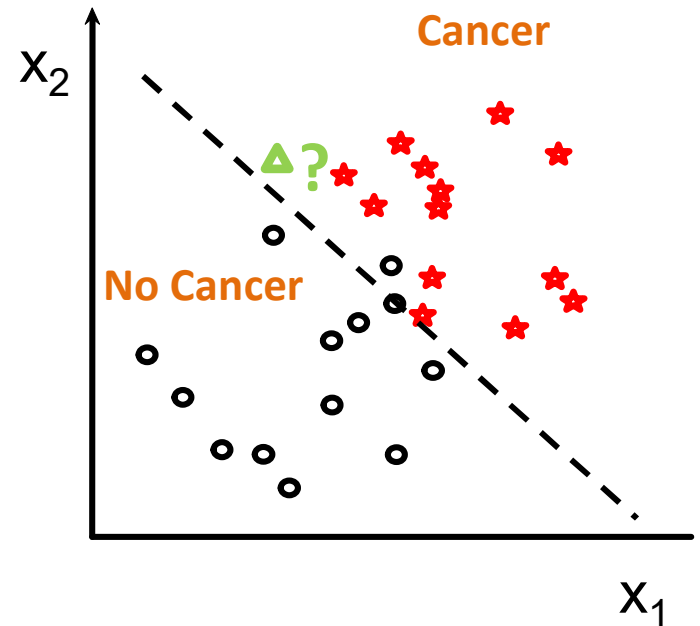
- We have corresponding sets of inputs & outputs and seek model that delivers correct output for every known input



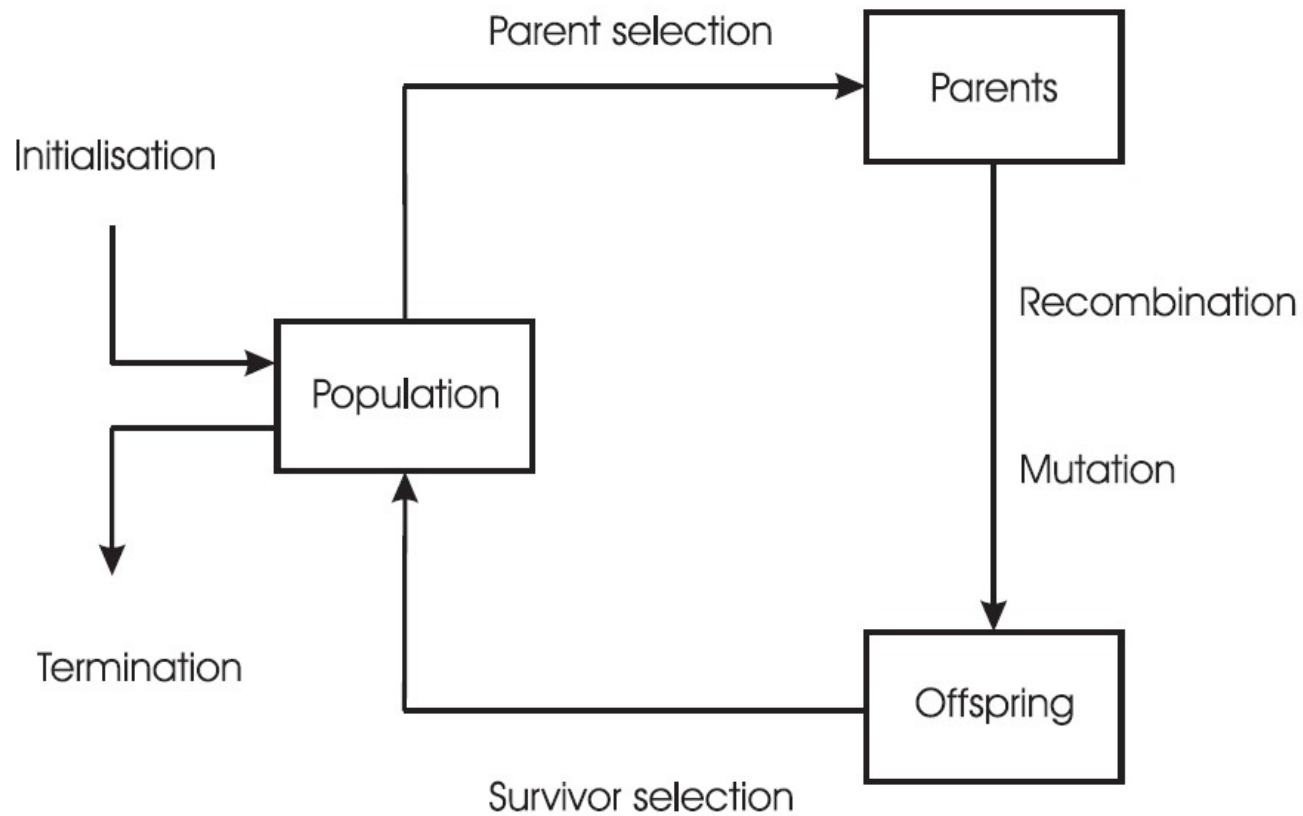
- Evolutionary machine learning
- Genetics-based machine learning

# Pattern classification

- To learn a model able to make predictions regarding a variable of interest, using a set of other variables. E.g., classifying:
  - *Emails as spam vs safe-email*
  - *Tomographies as tumor vs no-tumor*
  - *Image faces as the identity of somebody*
  - *Scanned handwritten text as digits*



# General Scheme of EAs



# Pseudo-code for typical EA

```
BEGIN
  INITIALISE population with random candidate solutions;
  EVALUATE each candidate;
  REPEAT UNTIL ( TERMINATION CONDITION is satisfied ) DO
    1 SELECT parents;
    2 RECOMBINE pairs of parents;
    3 MUTATE the resulting offspring;
    4 EVALUATE new candidates;
    5 SELECT individuals for the next generation;
  OD
END
```

# What are the different types of EAs

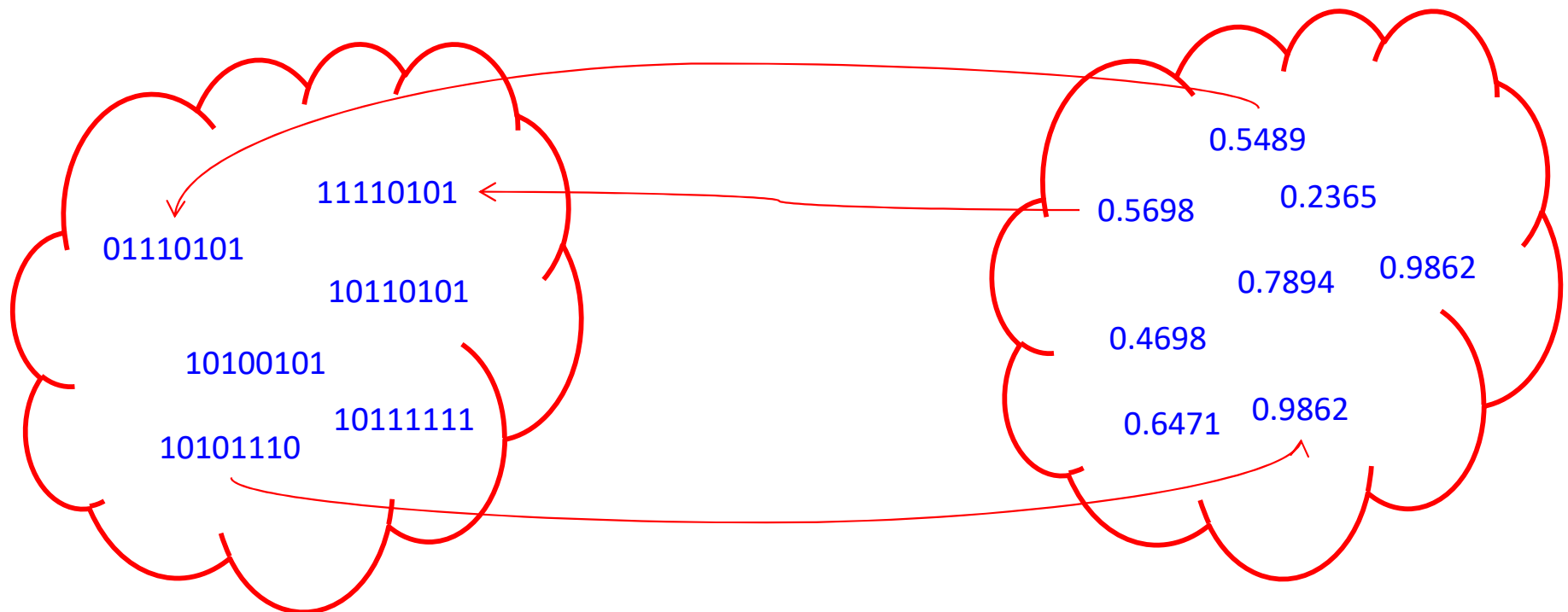
- Historically different flavours of EAs have been associated with different representations
  - Binary strings : Genetic Algorithms
  - Real-valued vectors : Evolution Strategies
  - Finite state Machines: Evolutionary Programming
  - Trees: Genetic Programming

# What are the different types of EAs

- These differences are largely irrelevant, best strategy
  - choose representation to suit problem
  - choose variation operators to suit representation
- Selection operators only use fitness and so are independent of representation

# Representations

- Candidate solutions (**individuals**) exist in *phenotype* space – solutions space
- They are encoded in **chromosomes**, which exist in *genotype* space – search space
  - Encoding : phenotype=> genotype
  - Decoding : genotype=> phenotype



# Representations

- Chromosomes contain **genes**, which are in (usually fixed) positions called **loci** (sing. locus) and have a value (**allele**)

**In order to find the global optimum, every feasible solution must be represented in genotype space**

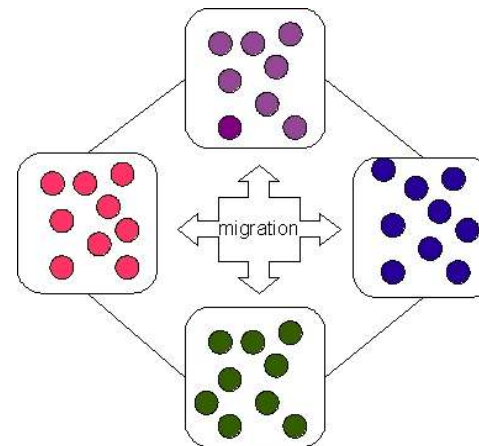
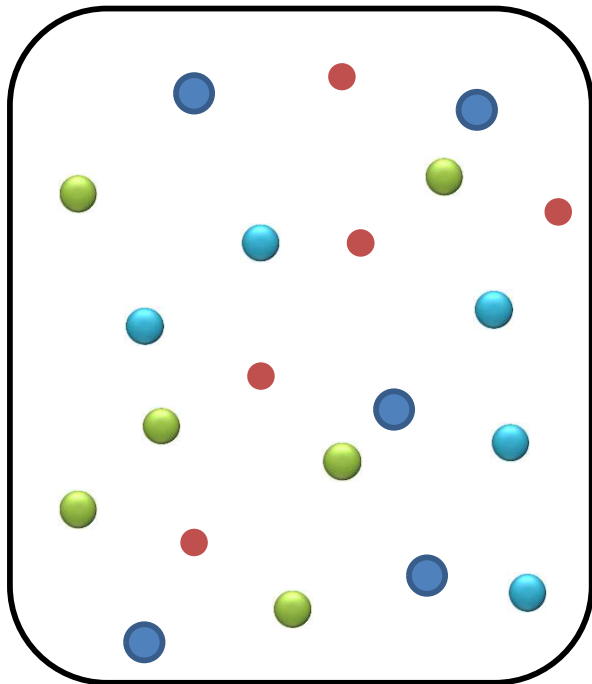
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---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

# Evaluation (Fitness) Function

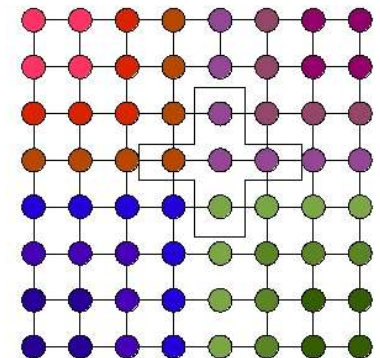
- Represents the requirements that the population should adapt to
- a.k.a. *quality* function or *objective* function
- Assigns a single real-valued fitness to each phenotype which forms the basis for selection
  - So the more discrimination (different values) the better
- Typically we talk about fitness being maximised
  - Some problems may be best posed as minimisation problems, but conversion is trivial

# Population

- Holds (representations of) possible solutions
- Usually has a fixed size and is a *multiset* of genotypes
  - Some sophisticated EAs also assert a spatial structure on the population e.g., a grid.
  - Panmictic or centralized population – global interaction
  - Decentralized population – local interaction



Distributed PGA



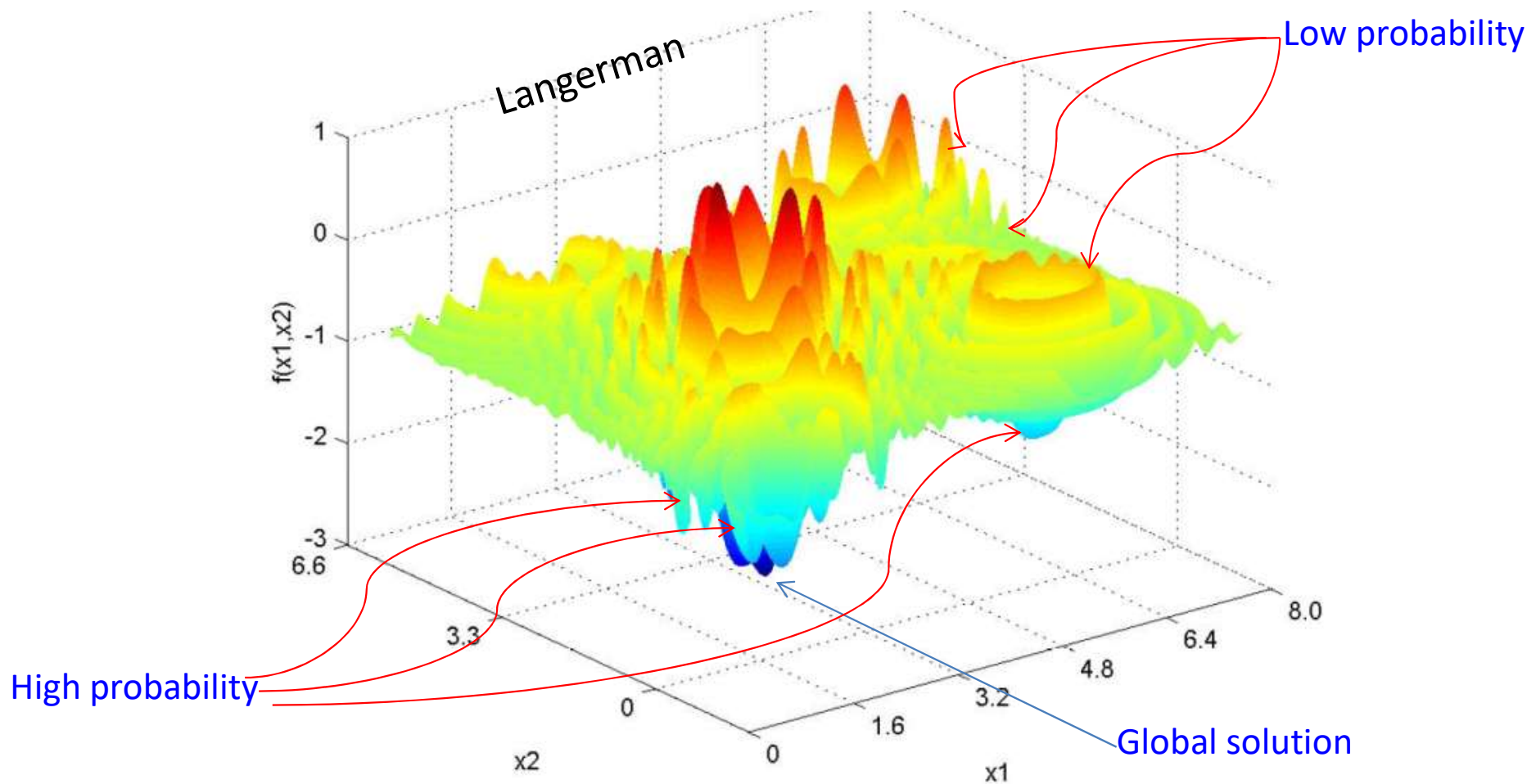
Cellular GA

# Population

- Selection operators usually take whole population into account i.e., reproductive probabilities are *relative to current generation*
- **Diversity** of a population refers to the number of different fitnesses / phenotypes / genotypes present (note not the same thing)
  - Entropy

# Parent Selection Mechanism

- Assigns variable probabilities of individuals acting as parents depending on their fitnesses



# Parent Selection Mechanism

- Usually probabilistic
  - high quality solutions more likely to become parents than low quality
  - but not guaranteed
  - even worst in current population usually has non-zero probability of becoming a parent
- This *stochastic* nature can aid escape from local optima

# Variation Operators

- Role is to generate new candidate solutions
- Usually divided into two types according to their **arity** (number of inputs):
  - Arity 1 : mutation operators
  - Arity >1 : Recombination operators
  - Arity = 2 typically called **crossover**
- There has been much debate about relative importance of recombination and mutation
  - Nowadays most EAs use both
  - Choice of particular variation operators is representation dependant

# Mutation

- Acts on one genotype and delivers another
- Element of randomness is essential and differentiates it from other unary heuristic operators
- Importance ascribed depends on representation and dialect:
  - Binary GAs – background operator responsible for preserving and introducing diversity
  - EP for FSM's/ continuous variables – only search operator
  - GP – hardly used
- May guarantee connectedness of search space and hence convergence proofs

# Recombination

- Merges information from parents into offspring
- Choice of what information to merge is stochastic
- Most offspring may be worse, or the same as the parents
- Hope is that some are better by combining elements of genotypes that lead to good traits
- Principle has been used for millennia by breeders of plants and livestock

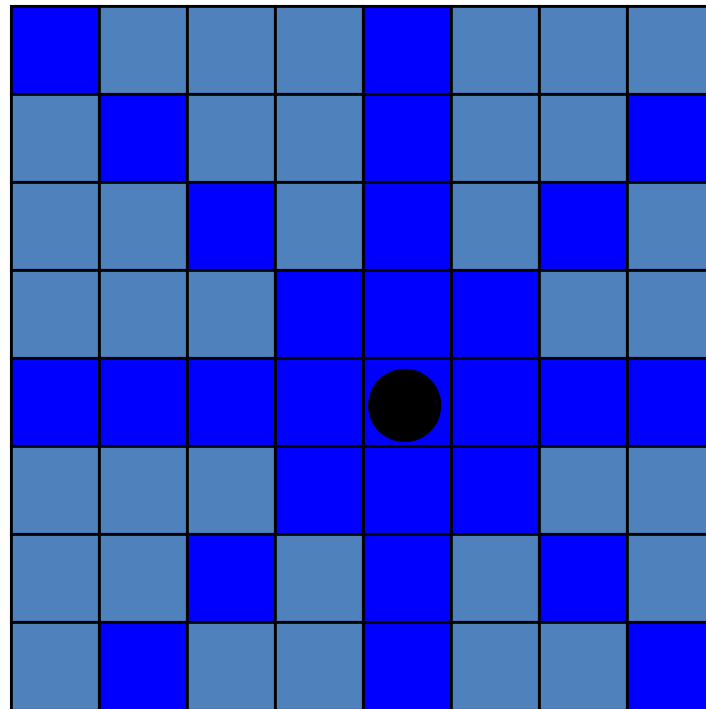
# Survivor Selection

- a.k.a. *Replacement*
- Most EAs use fixed population size so need a way of going from (parents + offspring) to next generation
- Often deterministic
  - Fitness based : e.g., rank parents+offspring and take best
  - Age based: make as many offspring as parents and delete all parents
- Sometimes do combination (elitism)

# Initialization / Termination

- Initialization usually done at random,
  - Need to ensure even spread and mixture of possible allele values
  - Can include existing solutions, or use problem-specific heuristics, to “seed” the population
- Termination condition checked every generation
  - Reaching some (known/hoped for) fitness
  - Reaching some maximum allowed number of generations
  - Reaching some minimum level of diversity
  - Reaching some specified number of generations without fitness improvement

# Example: the 8 queens problem

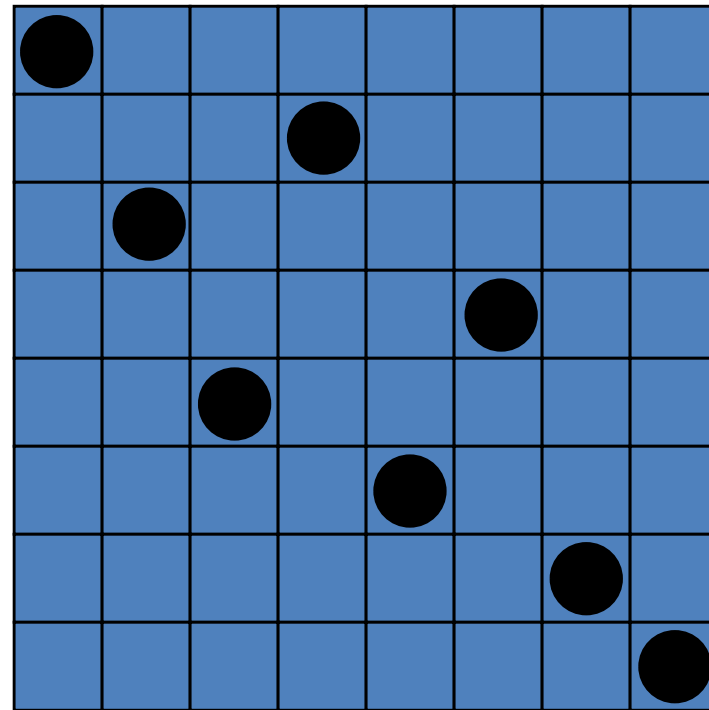


Place 8 queens on an 8x8 chessboard in such a way that they cannot check each other

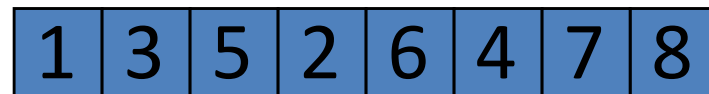
# The 8 queens problem: representation

Phenotype:  
a board configuration

Genotype:  
a permutation of  
the numbers 1 - 8



Obvious mapping



# 8 Queens Problem: Fitness evaluation

- Penalty of one queen:  
the number of queens she can check.
- Penalty of a configuration:  
the sum of the penalties of all queens.
- Note: penalty is to be minimized

# The 8 queens problem: Mutation

Small variation in one permutation, e.g.:

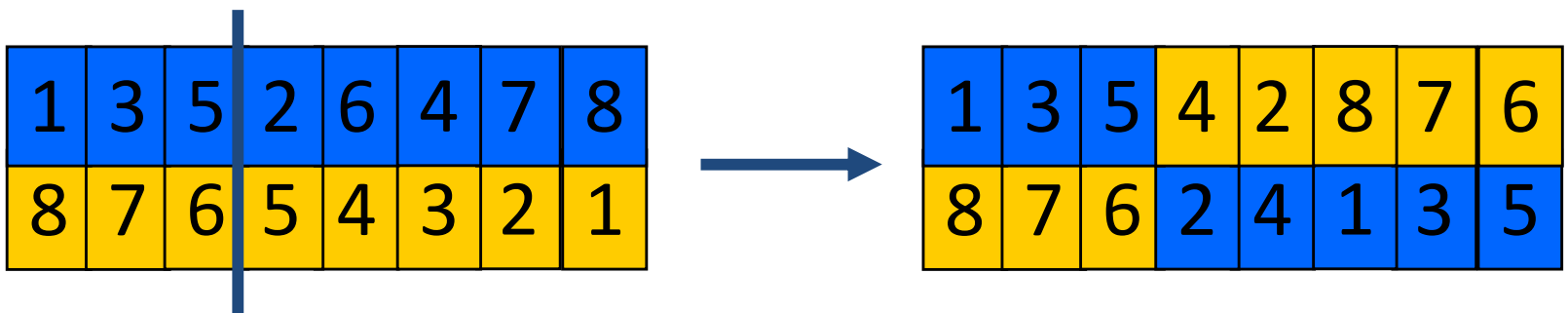
- swapping values of two randomly chosen positions,



# The 8 queens problem: Recombination

Combining two permutations into two new permutations:

- choose random crossover point
- copy first parts into children
- create second part by inserting values from other parent:
  - in the order they appear there
  - beginning after crossover point
  - skipping values already in child



# The 8 queens problem: Selection

- Parent selection:
  - Pick 5 parents and take best two to undergo crossover
- Survivor selection (replacement)
  - When inserting a new child into the population, choose an existing member to replace by:
    - sorting the whole population by decreasing fitness
    - enumerating this list from high to low
    - replacing the first with a fitness lower than the given child

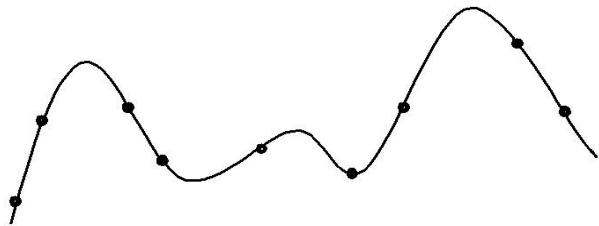
# 8 Queens Problem: summary

Representation	Permutations
Recombination	“Cut-and-crossfill” crossover
Recombination probability	100%
Mutation	Swap
Mutation probability	80%
Parent selection	Best 2 out of random 5
Survival selection	Replace worst
Population size	100
Number of Offspring	2
Initialisation	Random
Termination condition	Solution or 10,000 fitness evaluation

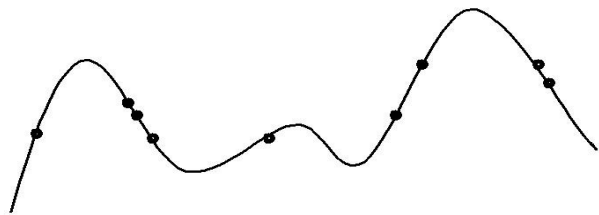
Note that it is ***only one possible*** set of choices of operators and parameters

# Typical behaviour of an EA

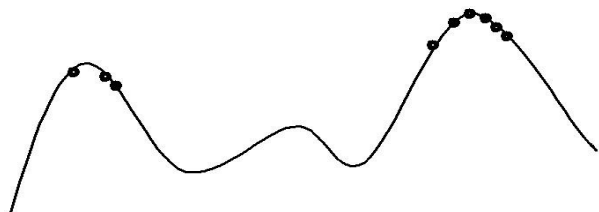
Phases in optimizing on a 1-dimensional fitness landscape



Early phase:  
quasi-random population distribution

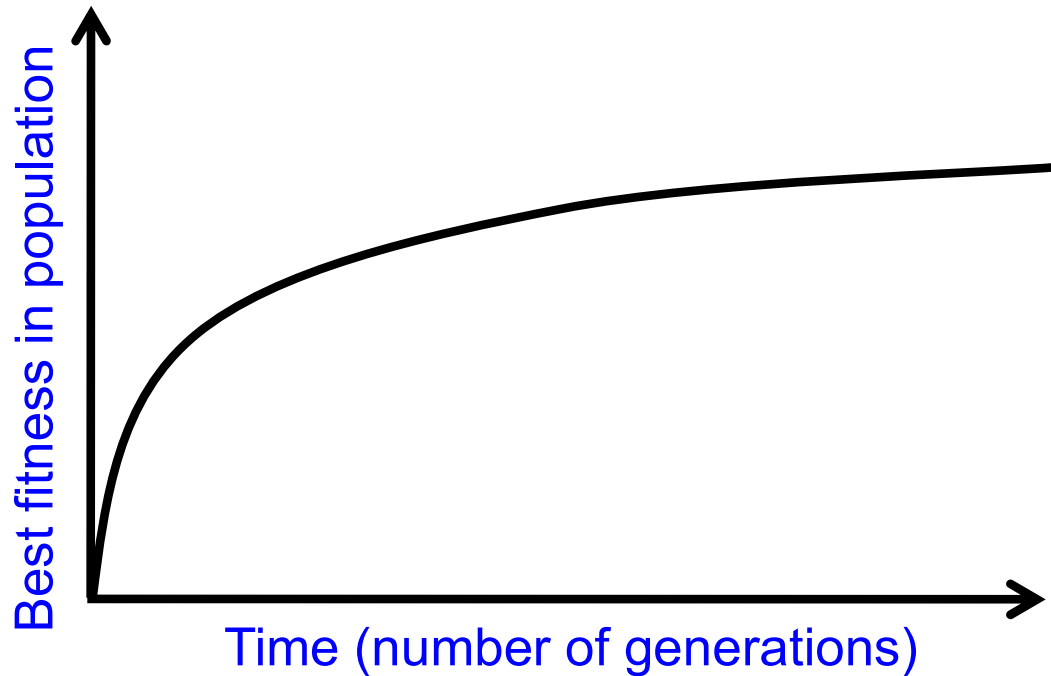


Mid-phase:  
population arranged around/on hills



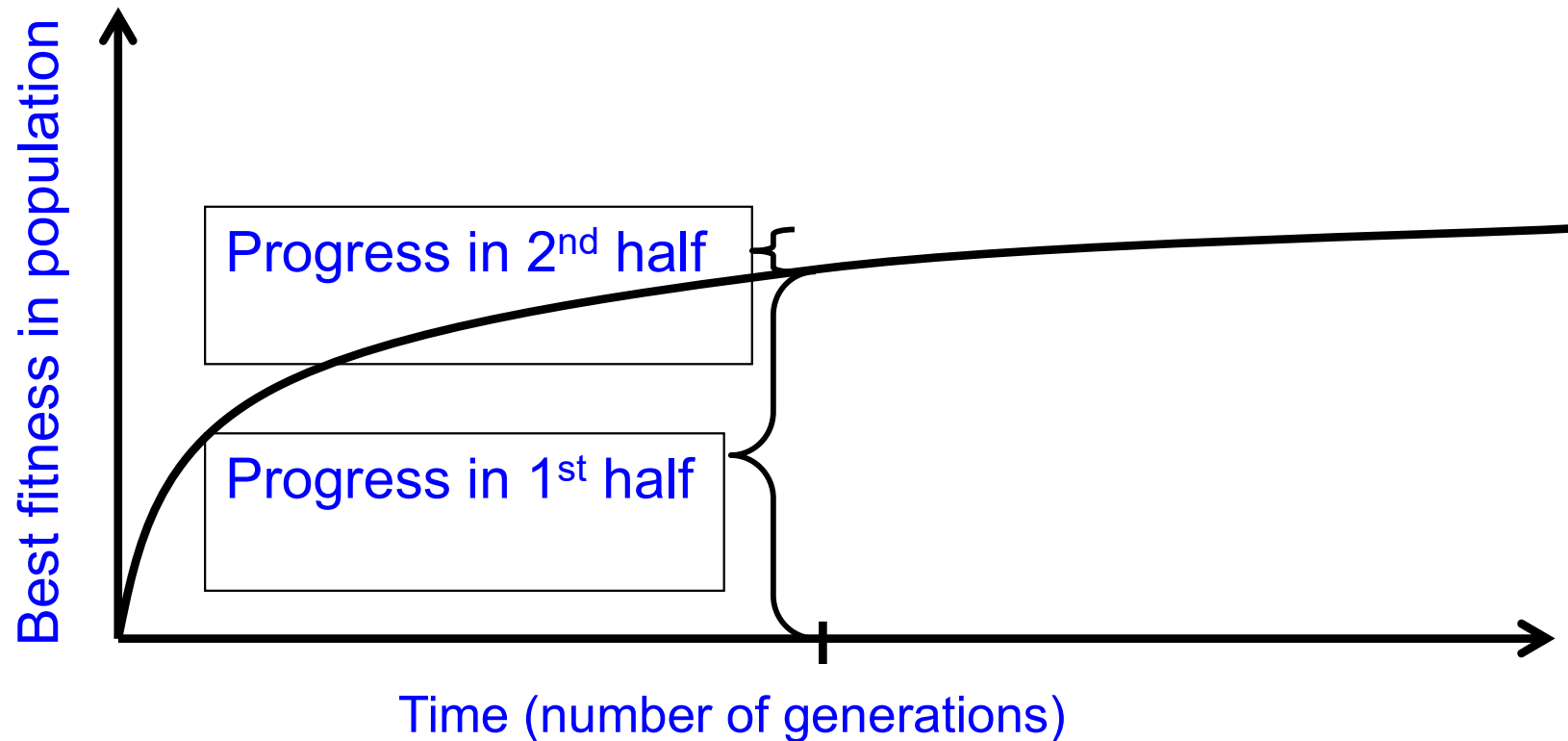
Late phase:  
population concentrated on high hills

# Typical run: progression of fitness



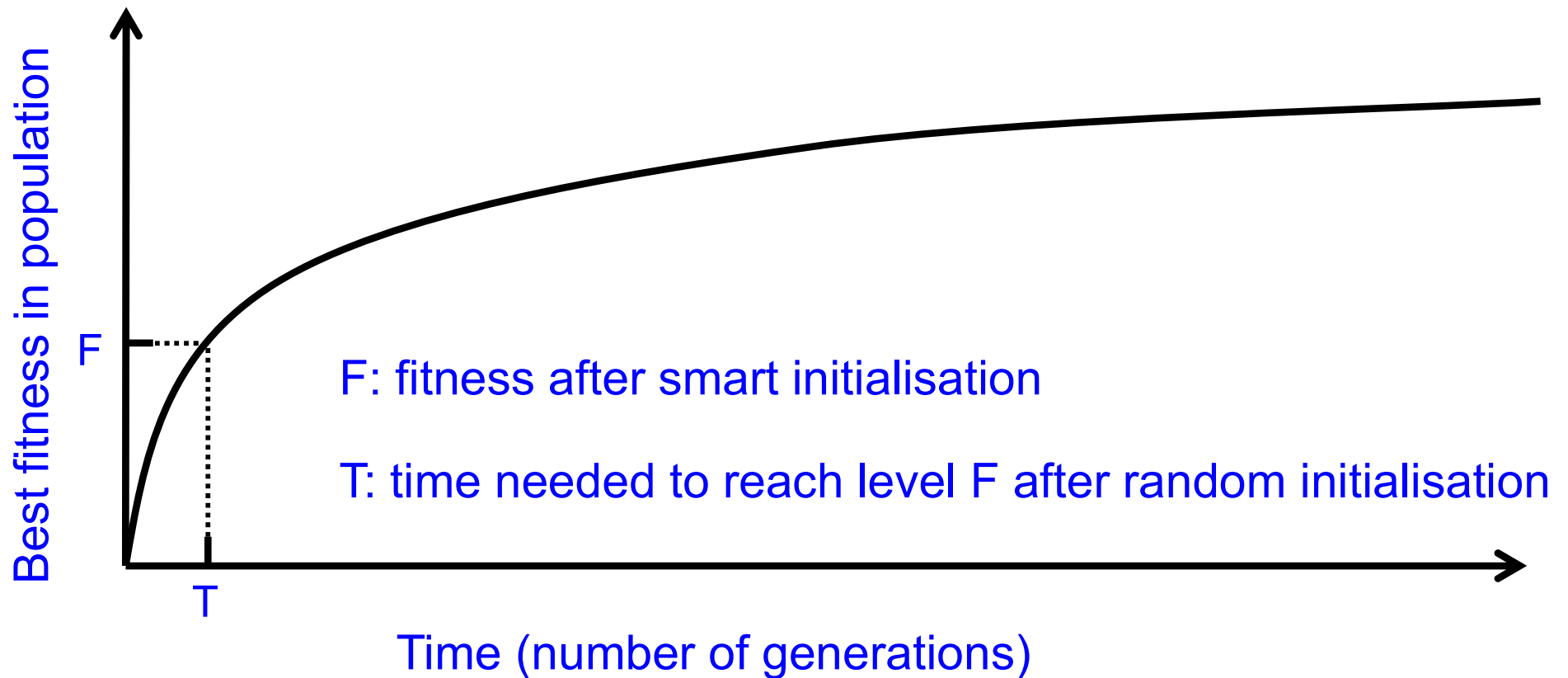
Typical run of an EA shows so-called “anytime behavior”

# Are long runs beneficial?



- Answer:
  - it depends how much you want the last bit of progress
  - it may be better to do more shorter runs

# Is it worth expending effort on smart initialization?



- Answer : it depends:
  - possibly, if good solutions/methods exist.
  - care is needed, see chapter on hybridisation

# Evolutionary Algorithms in Context

- There are many views on the use of EAs as robust problem solving tools
- For most problems a problem-specific tool may:
  - perform better than a generic search algorithm on most instances,
  - have limited utility,
  - not do well on all instances
- Goal is to provide robust tools that provide:
  - evenly good performance
  - over a range of problems and instances

Machine Learning through Genetic Programming

# **GENETIC ALGORITHMS**

- There is no single definitive genetic algorithm, rather algorithms are created from a suite of operators to suit particular applications
- Many of the issues relevant to GAs are also relevant to other evolutionary techniques, those aspects are going to be introduced here.

# GA Quick Overview

- Developed: USA in the 1970's
- Early names: J. Holland, K. DeJong, D. Goldberg
- Typically applied to:
  - discrete optimization
- Attributed features:
  - not too fast
  - good heuristic for combinatorial problems
- Special Features:
  - Traditionally emphasizes combining information from good parents (crossover)
  - many variants, e.g., reproduction models, operators

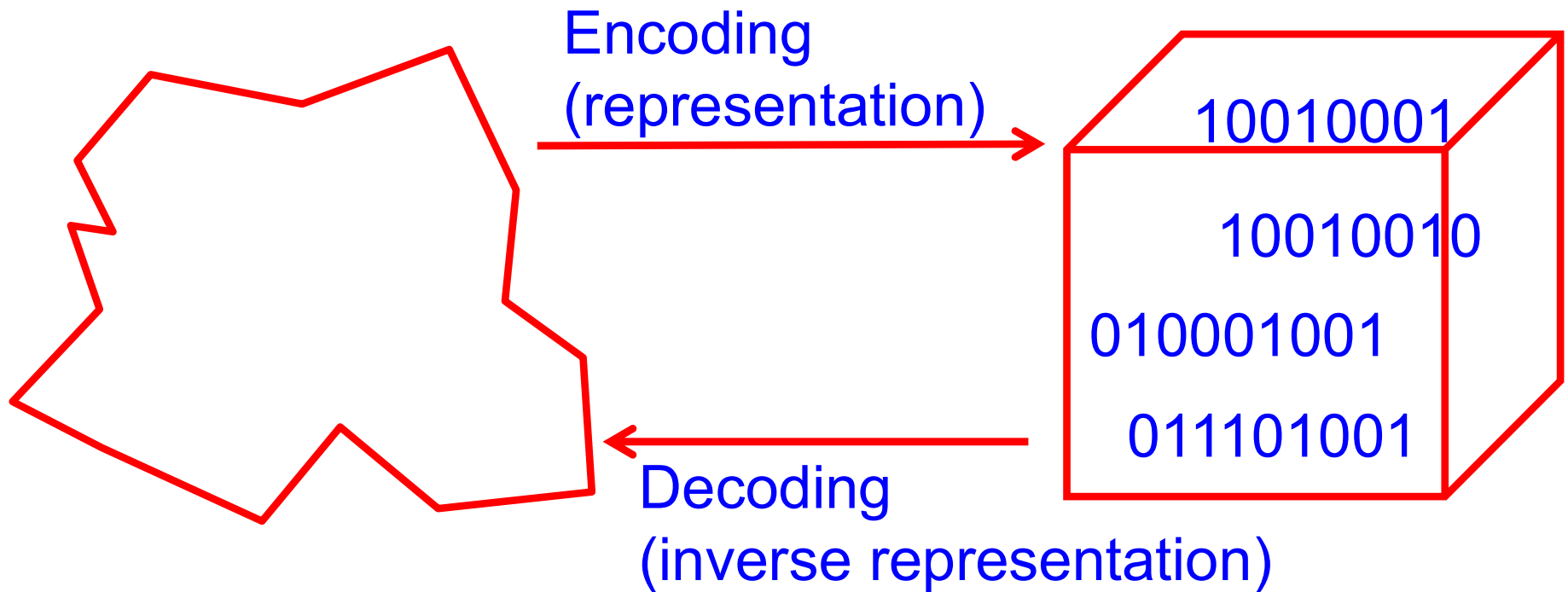
# Genetic algorithms

- Holland's original GA is now known as the simple genetic algorithm (SGA) or canonical GA
- Other GAs use different:
  - Representations
  - Mutations
  - Crossovers
  - Selection mechanisms

# Representation

Phenotype space

Genotype space =  $\{0,1\}^L$



# Representation

- First stage of building any evolutionary algorithm
- Defining the genotype and the mapping from genotype to phenotype
- Getting the representation right is one of the most difficult parts of designing a good EA
  - Good practice and good knowledge of the application domain
- *More common representations are explained but they might not be the best for your application*
  - Mixed representations is a more natural and suitable way of describing and manipulating a solution

# Representation

- Binary
  - It has been mistakenly used almost independently of the problem to be solved
  - It consists simply of a string of binary digits
    - Length of the string
    - Phenotype interpretation
  - Defining genotype – phenotype mapping
    - All bit strings denote a valid solution to the problem
    - All possible solutions can be represented

# Representation

- Binary
  - Problems with Boolean decision variables, genotype-phenotype mapping is natural, but frequently bit-string are used to encode non-binary information
    - Interpret an 80 bit-string as ten 8-bit integer or five 16-bit real numbers
      - Common mistake, better results can be obtained by using integer or real-valued representations

# Representation

- Integer
  - Finding optimal values for a set of variables that all take integer values
    - Evolving a path on a square grid, representation  $\{0,1,2,3\} = \{\text{North, East, South, West}\}$
- Real-valued or floating-point representation
  - Sensible way: having a real values string
  - Genes come from a continuous rather than discrete distribution
  - Precision is limited by implementation, thus reference is made as floating-point numbers

# Representation

- Permutation
  - Many problems decide on the order in which a sequence of events should occur
  - Ordinary GA strings allows number to occur more than once, such sequences do not represent valid permutations
    - Variation operator must preserve this permutation property
  - Two classes of problems
    - Order
      - E.g. Job shop scheduling, task scheduling. Order matters
    - Adjacency
      - E.g. Travelling sales person, find a complete tour of n cities of minimal length. It can be considered that the starting point of the tour is not important: [1,2,3,4],[2,3,4,1],[3,4,1,2],[4,1,2,3] would be equivalent

# SGA reproduction cycle

1. Select parents for the mating pool  
(size of mating pool = population size)
2. Shuffle the mating pool
3. For each consecutive pair apply crossover with probability  $p_c$  , otherwise copy parents
4. For each offspring apply mutation (bit-flip with probability  $p_m$  independently for each bit)
5. Replace the whole population with the resulting offspring



# SGA operators: mutation

- ▶ Alter each gene independently with a probability  $p_m$
- ▶  $p_m$  is called the mutation rate
  - ▶ Typically between  $1/\text{pop\_size}$  and  $1/\text{chromosome\_length}$

parent

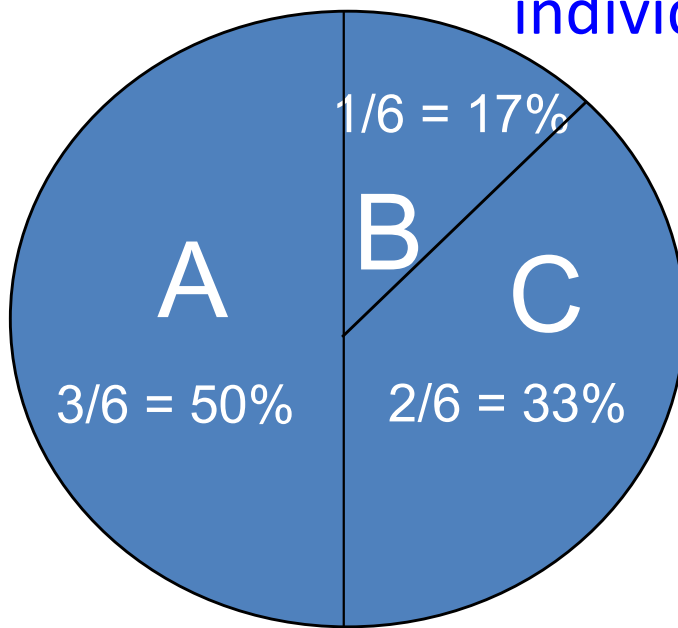
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child

0	1	0	0	1	0	1	1	0	0	0	1	0	1	1	0	0	1
---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---	---

# SGA operators: Selection

- Main idea: better individuals get higher chance
  - Chances proportional to fitness
  - Implementation: roulette wheel technique
    - » Assign to each individual a part of the roulette wheel
    - » Spin the wheel n times to select n individuals



$$\text{fitness}(A) = 3$$

$$\text{fitness}(B) = 1$$

$$\text{fitness}(C) = 2$$



# An example after Goldberg '89 (1)

- Simple problem:  $\max x^2$  over  $\{0,1,\dots,31\}$
- GA approach:
  - Representation: binary code, e.g.  $01101 \leftrightarrow 13$
  - Population size: 4
  - 1-point crossover, bitwise mutation
  - Roulette wheel selection
  - Random initialisation
- We show one generational cycle done by hand

Representation	Bit-strings
Recombination	1-Point crossover
Mutation	Bit flip
Parent selection	Fitness proportional
Survival selection	Generational

# Example $x^2$

String no.	Initial population	$x$ Value	Fitness $f(x) = x^2$	$Prob_i$	Expected count	Actual count
1	0 1 1 0 1	13	169	0.14	0.58	1
2	1 1 0 0 0	24	576	0.49	1.97	2
3	0 1 0 0 0	8	64	0.06	0.22	0
4	1 0 0 1 1	19	361	0.31	1.23	1
Sum			1170	1.00	4.00	4
Average			293	0.25	1.00	1
Max			576	0.49	1.97	2

$$Prob_i = f_i / \sum f_j$$

$$\text{Expected count} = f_i / \bar{f}$$

# Example $x^2$

- Crossover

String no.	Mating pool	Crossover point	Offspring after xover	$x$ Value	Fitness $f(x) = x^2$
1	0 1 1 0   1	4	0 1 1 0 0	12	144
2	1 1 0 0   0	4	1 1 0 0 1	25	625
2	1 1   0 0 0	2	1 1 0 1 1	27	729
4	1 0   0 1 1	2	1 0 0 0 0	16	256
Sum					1754
Average					439
Max					729

# Example $x^2$

- Mutation

String no.	Offspring after xover	Offspring after mutation	$x$ Value	Fitness $f(x) = x^2$
1	0 1 1 0 0	<span style="border: 1px solid red;">1</span> 1 1 0 0	28	<span style="border: 1px solid red;">784</span>
2	1 1 0 0 1	1 1 0 0 1	25	625
2	1 1 0 1 1	1 1 0 1 1	27	729
4	1 0 0 0 0	1 0 <span style="border: 1px solid red;">1</span> 0 0	20	400
Sum				2538
Average				<span style="border: 1px solid red;">634.5</span>
Max				784

- Mutation rate e.g. 0.001

# SGA technical summary tableau

Representation	Binary strings
Recombination	N-point or uniform
Mutation	Bitwise bit-flipping with fixed probability
Parent selection	Fitness-Proportionate
Survivor selection	All children replace parents
Speciality	Emphasis on crossover

# The simple GA

- Has been subject of many (early) studies
  - still often used as benchmark for novel GAs
- Shows many shortcomings, e.g.
  - Representation is too restrictive
  - Mutation & crossovers only applicable for bit-string & integer representations
  - Selection mechanism sensitive for converging populations with close fitness values
  - Generational population model (step 5 in SGA reproductive cycle) can be improved with explicit survivor selection

# Brief History: the ancestors

- 1948, Turing:  
proposes “genetical or evolutionary search”
- 1962, Bremermann  
optimization through evolution and recombination
- 1964, Rechenberg  
introduces evolution strategies
- 1965, L. Fogel, Owens and Walsh  
introduce evolutionary programming
- 1975, Holland  
introduces genetic algorithms
- 1992, Koza  
introduces genetic programming

Machine Learning through Genetic Programming

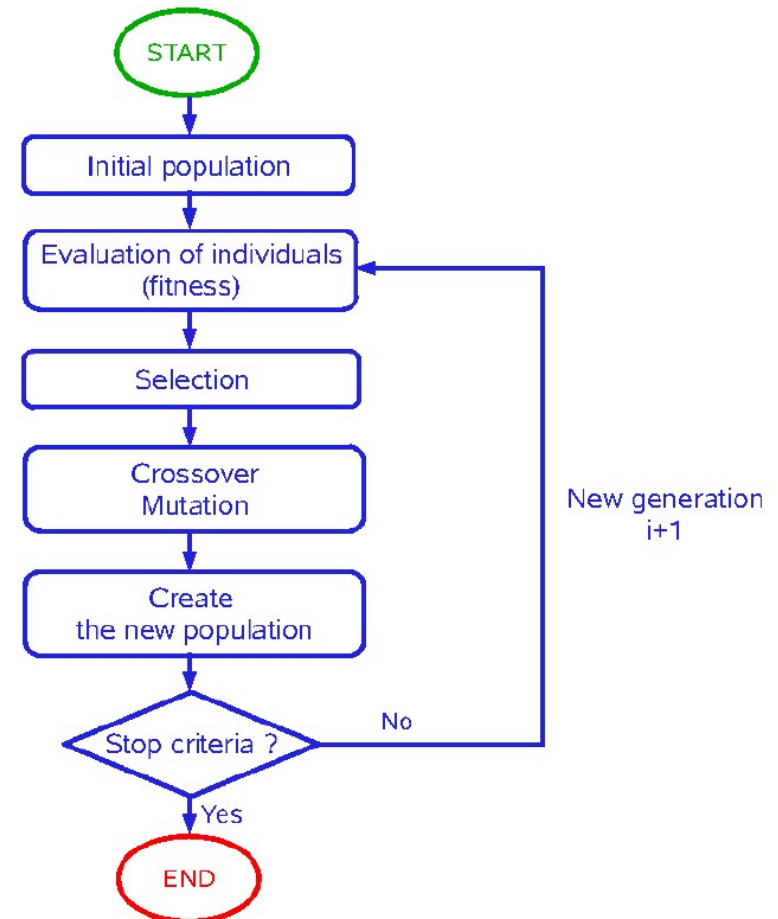
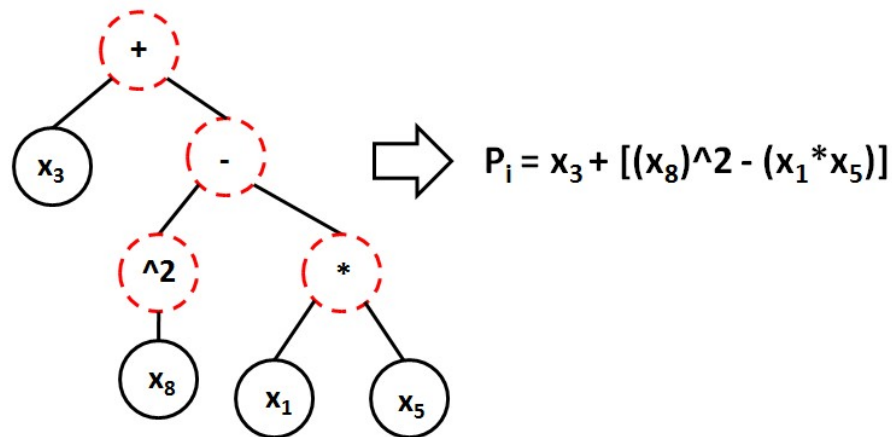
# **GENETIC PROGRAMMING**

# Brief History 1: the ancestors

- 1948, Turing:  
proposes “genetical or evolutionary search”
- 1962, Bremermann  
optimization through evolution and recombination
- 1964, Rechenberg  
introduces evolution strategies
- 1965, L. Fogel, Owens and Walsh  
introduce evolutionary programming
- 1975, Holland  
introduces genetic algorithms
- 1992, Koza  
introduces genetic programming

# Main differences with other EA's

- GP: standard EA with tree-based representation



# Main differences with other EA's

- Most other EAs target optimization/simulation problems, whereas in GP the common target is a machine learning task



# GP quick overview

- Developed: USA in the 1990's
- Early names: J. Koza
- Typically applied to:
  - machine learning tasks (prediction, classification...)
- Attributed features:
  - competes with neural nets and alike
  - needs huge populations (thousands)
  - slow
- Special:
  - non-linear chromosomes: trees, graphs
  - mutation possible but not necessary (disputed!)

# GP technical summary tableau

---

Representation

Tree structures

Recombination

Exchange of subtrees

Mutation

Random change in trees

Parent selection

Fitness proportional

Survivor selection

Generational replacement

---

# Introductory example: credit scoring

- Bank wants to distinguish good from bad loan applicants
- Model needed that matches historical data

ID	No of children	Salary	Marital status	OK?
ID-1	2	45000	Married	0
ID-2	0	30000	Single	1
ID-3	1	40000	Divorced	1
...	...	...	...	...

# Introductory example: credit scoring

- A possible model:

IF (NOC = 2) AND (S > 80000) THEN good ELSE bad

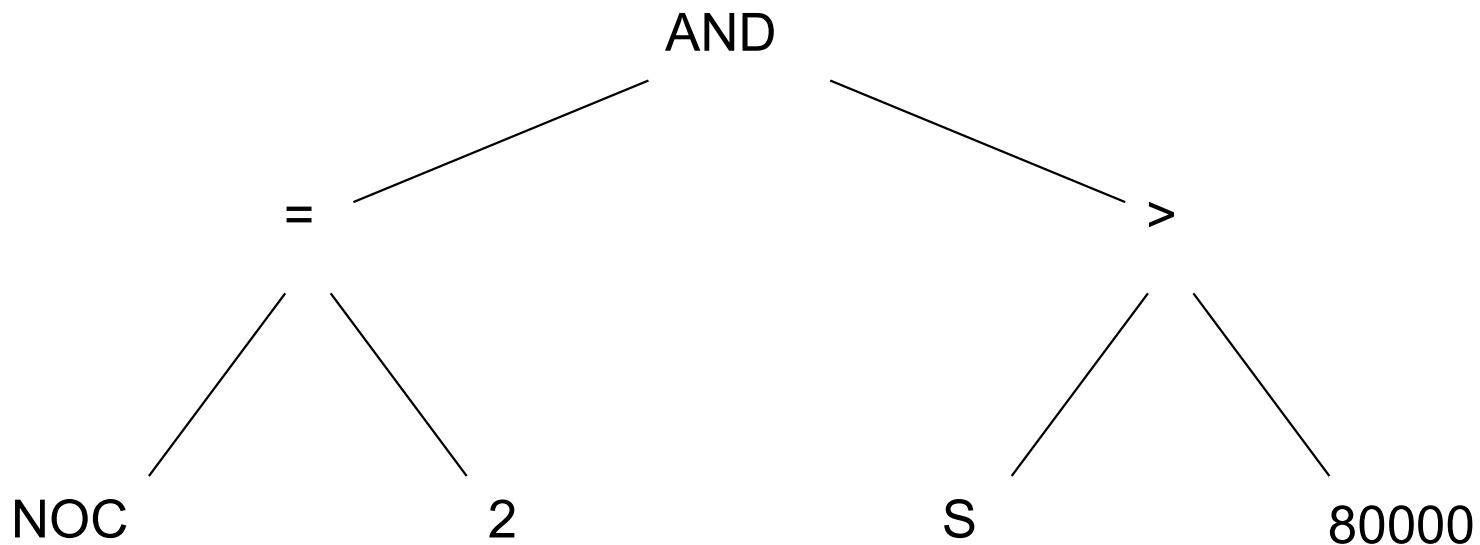
- In general:

IF formula THEN good ELSE bad

- Only unknown is the right formula, hence
- Our search space (phenotypes) is the set of formulas
- Natural fitness of a formula: percentage of well classified cases of the model it stands for
- Natural representation of formulas (genotypes) is: parse trees

# Introductory example: credit scoring

IF (NOC = 2) AND (S > 80000) THEN good ELSE bad  
can be represented by the following tree



GP: is used to search for the best tree (classifier)

# Tree based representation

- Trees are a universal form, e.g. consider

- Arithmetic formula  $2 \cdot \pi + \left( (x + 3) - \frac{y}{5 + 1} \right)$

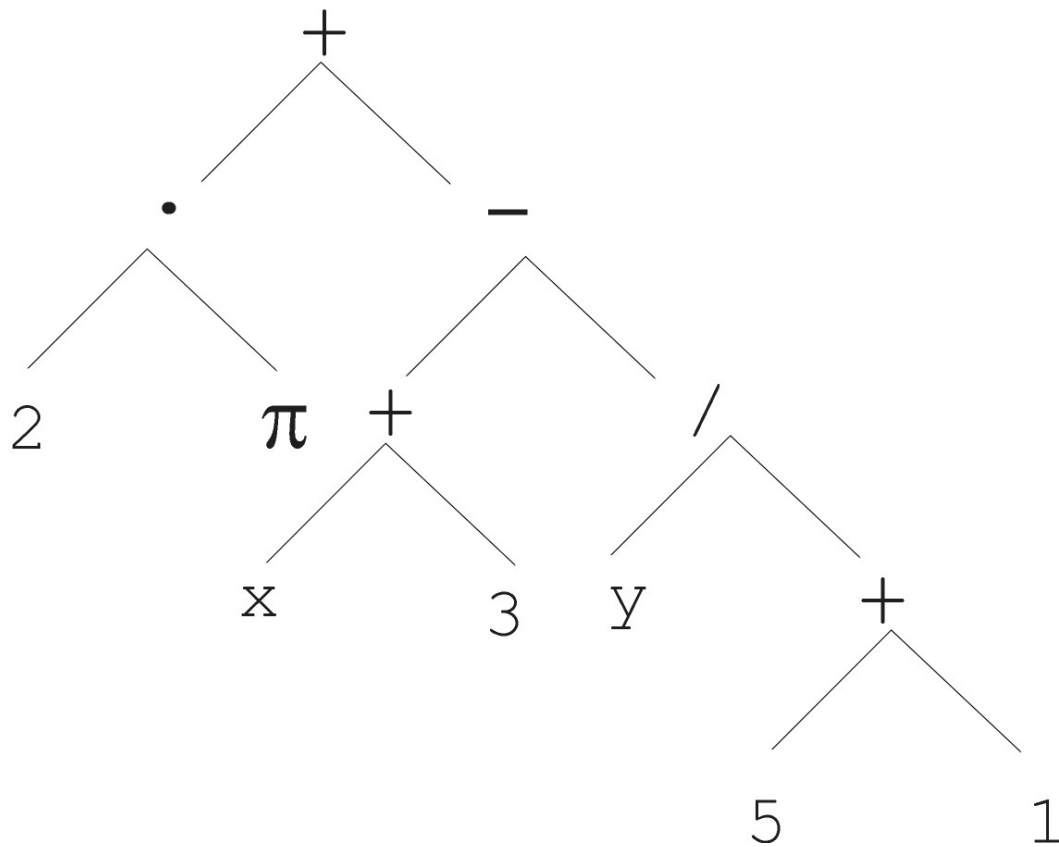
- Logical formula  $(x \wedge \text{true}) \rightarrow ((x \vee y) \vee (z \leftrightarrow (x \wedge y)))$

- Program

```
i = 1;
while (i < 20)
{
    i = i + 1
}
```

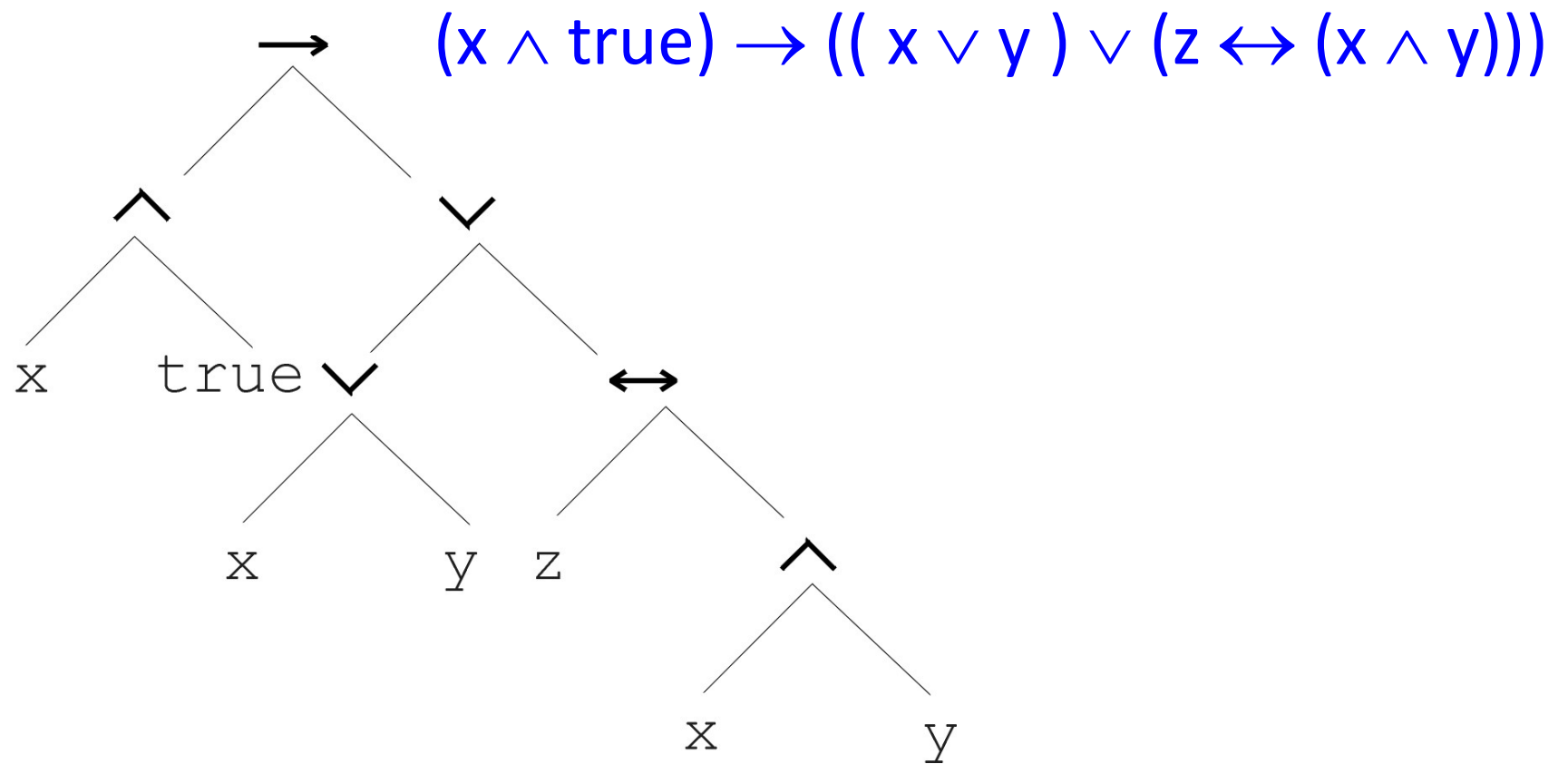
GP: is used to search for the best tree (classifier)

# Tree based representation

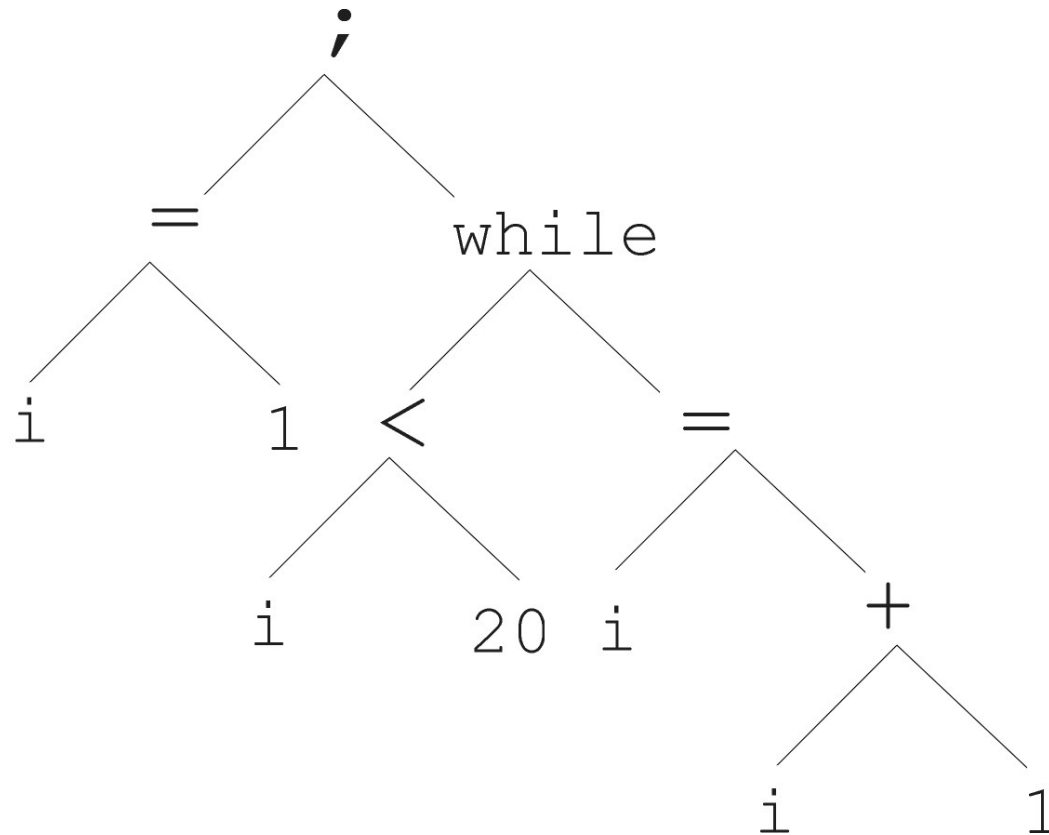


$$2 \cdot \pi + \left( (x + 3) - \frac{y}{5 + 1} \right)$$

# Tree based representation



# Tree based representation



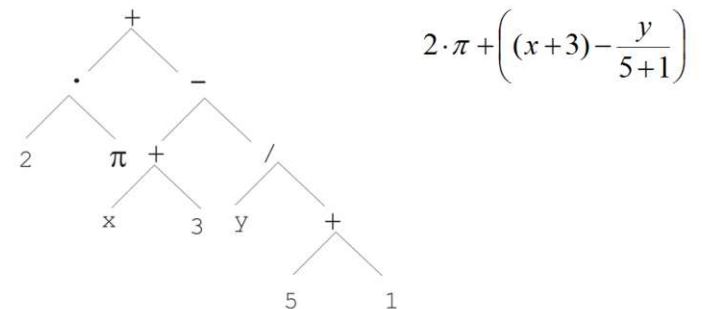
```
i = 1;  
while (i < 20)  
{  
    i = i + 1  
}
```

# Tree based representation

- In GA, ES, EP chromosomes are linear structures (bit strings, integer string, real-valued vectors, permutations)
- Tree shaped chromosomes are non-linear structures
- In GA, ES, EP the size of the chromosomes is fixed
- Trees in GP may vary in depth and width

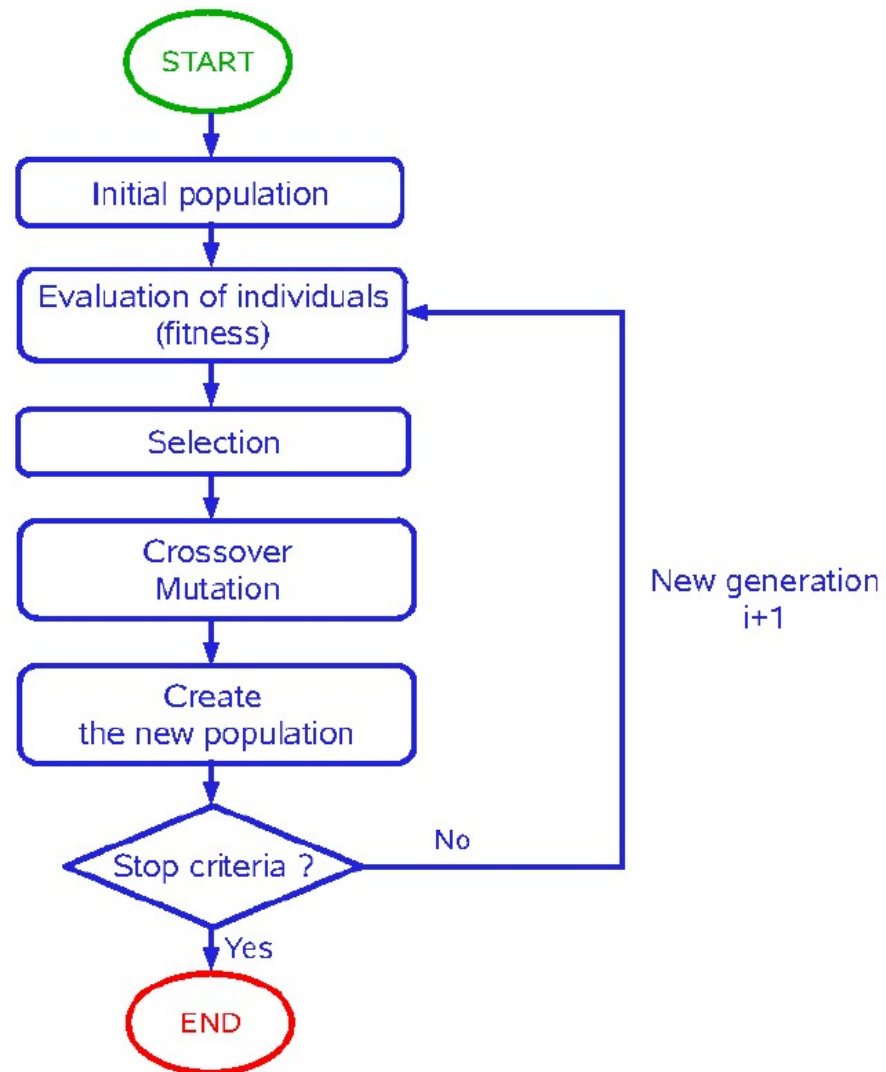
# Tree based representation

- Symbolic expressions can be defined by
  - Terminal set  $T$
  - Function set  $F$  (with the arities of function symbols)
- Adopting the following general recursive definition:
  1. Every  $t \in T$  is a correct expression
  2.  $f(e_1, \dots, e_n)$  is a correct expression if  $f \in F$ ,  $\text{arity}(f)=n$  and  $e_1, \dots, e_n$  are correct expressions
  3. There are no other forms of correct expressions
- In general, expressions in GP are not typed (closure property: any  $f \in F$  can take any  $g \in F$  as argument)



$$2 \cdot \pi + \left( (x+3) - \frac{y}{5+1} \right)$$

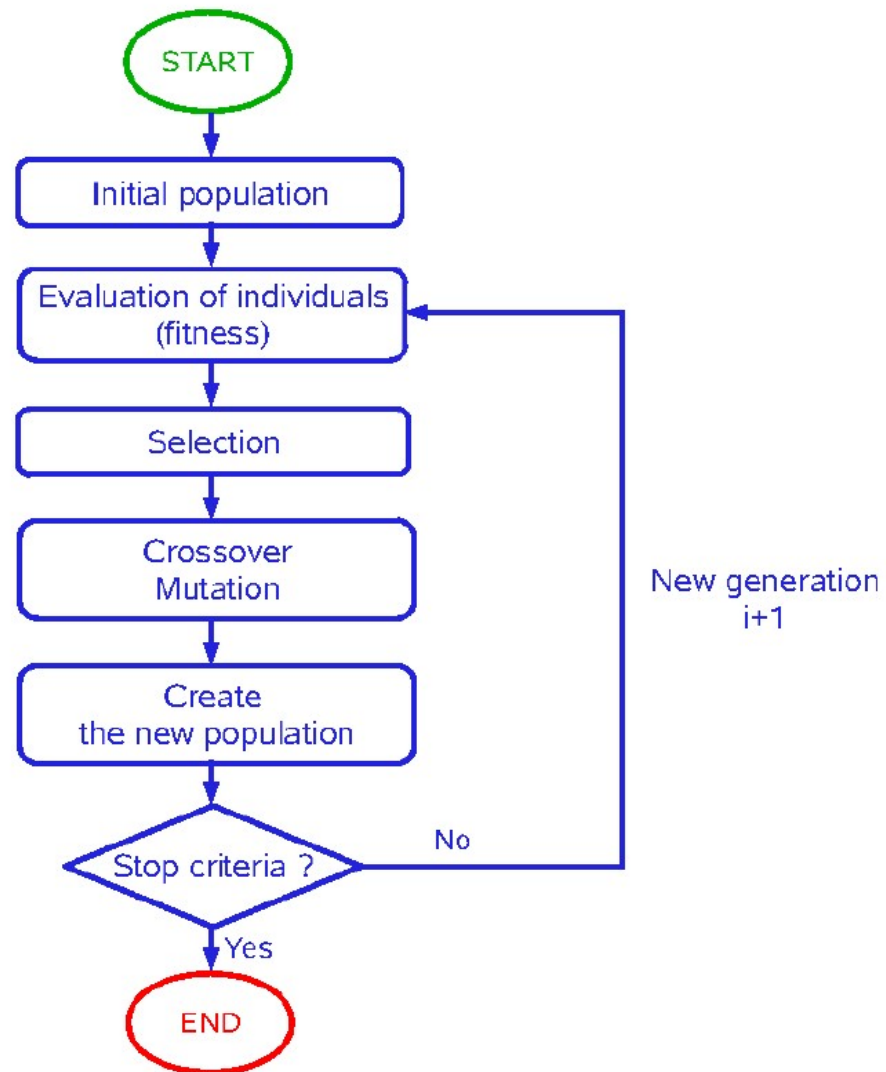
# Generic EA



# Initialization

- Maximum initial depth of trees  $D_{\max}$  is set
- Full method (each branch has depth =  $D_{\max}$ ):
  - nodes at depth  $d < D_{\max}$  randomly chosen from function set  $F$
  - nodes at depth  $d = D_{\max}$  randomly chosen from terminal set  $T$
- Grow method (each branch has depth  $\leq D_{\max}$ ):
  - nodes at depth  $d < D_{\max}$  randomly chosen from  $F \cup T$
  - nodes at depth  $d = D_{\max}$  randomly chosen from  $T$
- Common GP initialisation: ramped half-and-half, where grow & full method each deliver half of initial population

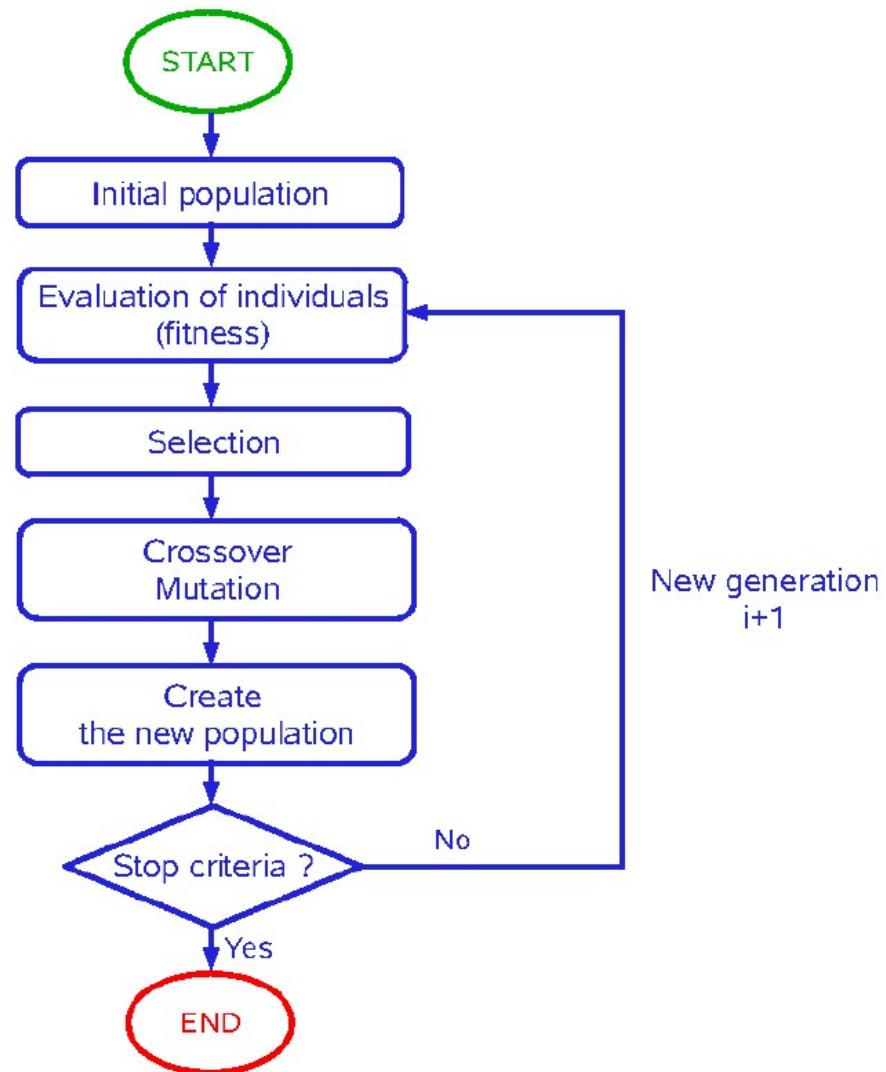
# Generic EA



# Selection

- Parent selection typically fitness proportionate
- Over-selection in very large populations
  - rank population by fitness and divide it into two groups:
  - group 1: best  $x\%$  of population, group 2 other  $(100-x)\%$
  - 80% of selection operations chooses from group 1, 20% from group 2
  - for pop. size = 1000, 2000, 4000, 8000  $x = 32\%, 16\%, 8\%, 4\%$
  - motivation: to increase efficiency, %'s come from rule of thumb
- Survivor selection:
  - Typical: generational scheme
  - Recently steady-state is becoming popular for its elitism

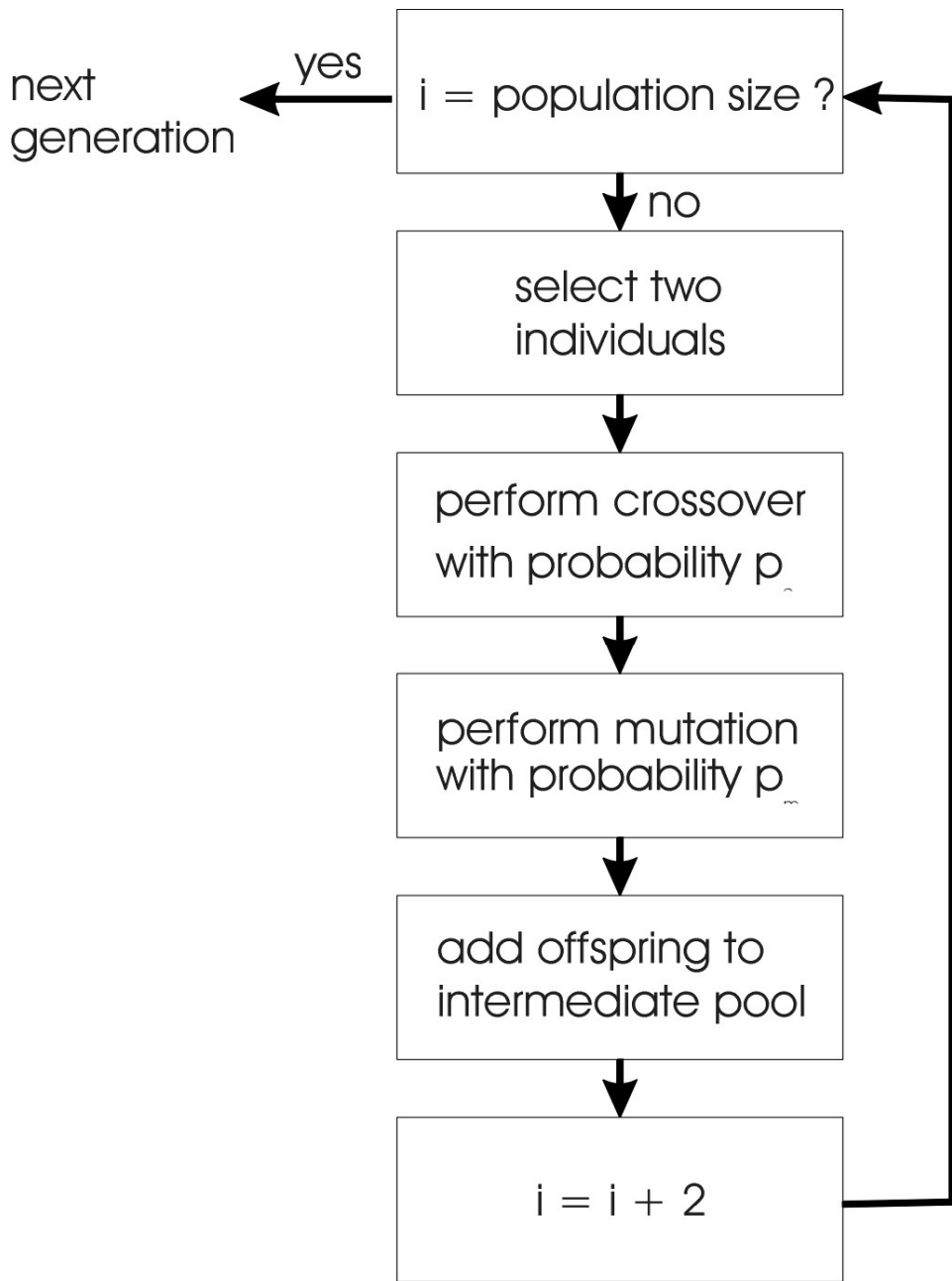
# Generic EA



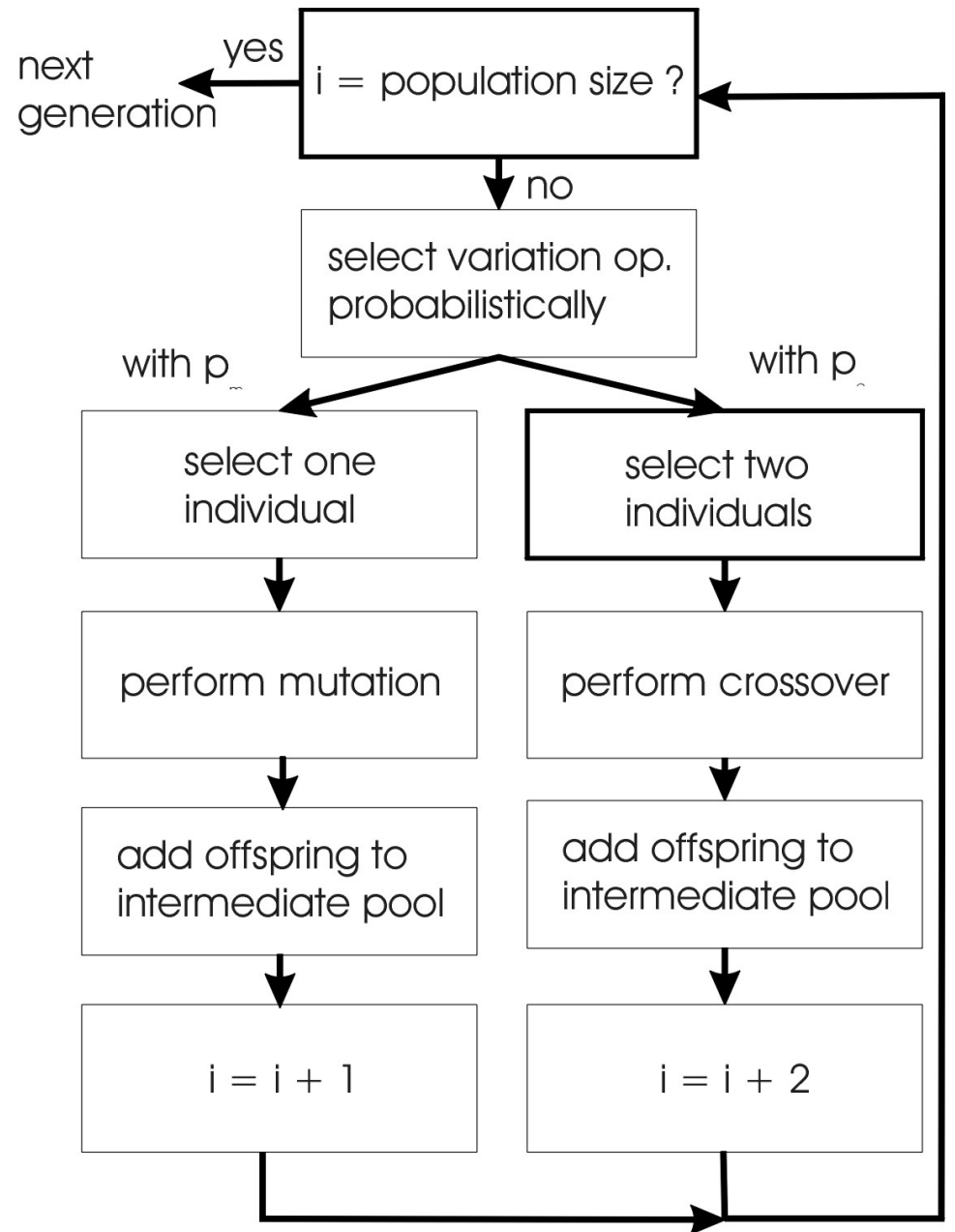
# Offspring creation scheme

## Compare

- GA scheme using crossover AND mutation sequentially (be it probabilistically)
- GP scheme using crossover OR mutation (chosen probabilistically)



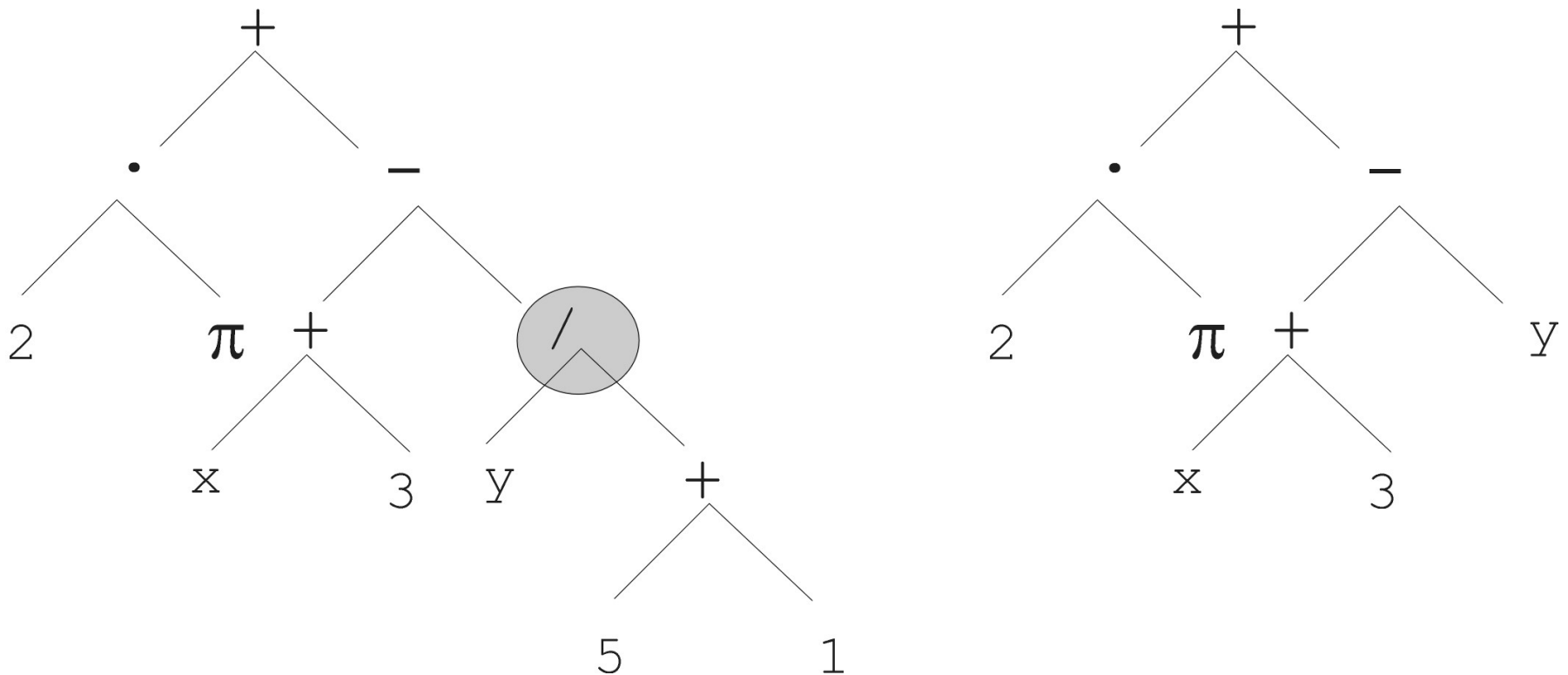
GA flowchart



GP flowchart

# Mutation

- Most common mutation: replace randomly chosen subtree by randomly generated tree

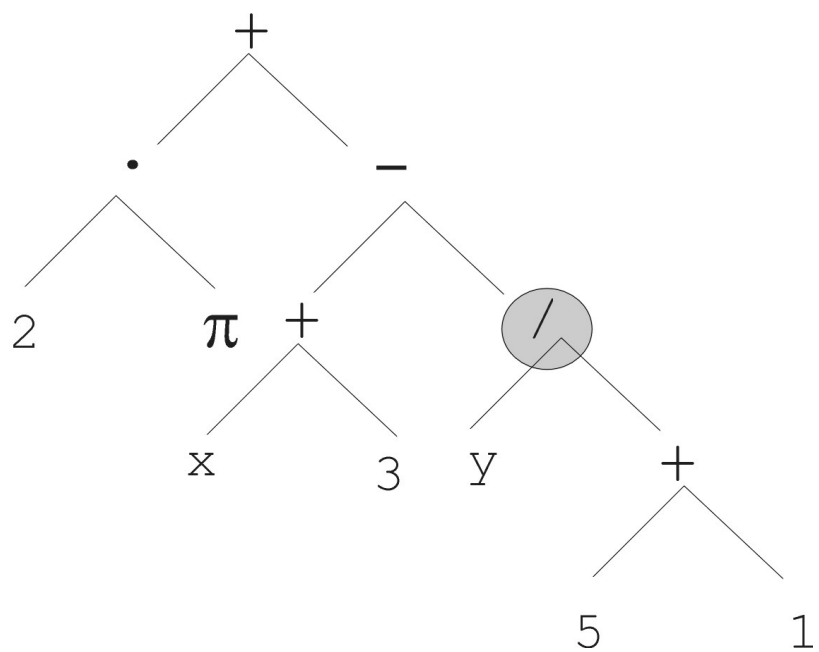


# Mutation cont'd

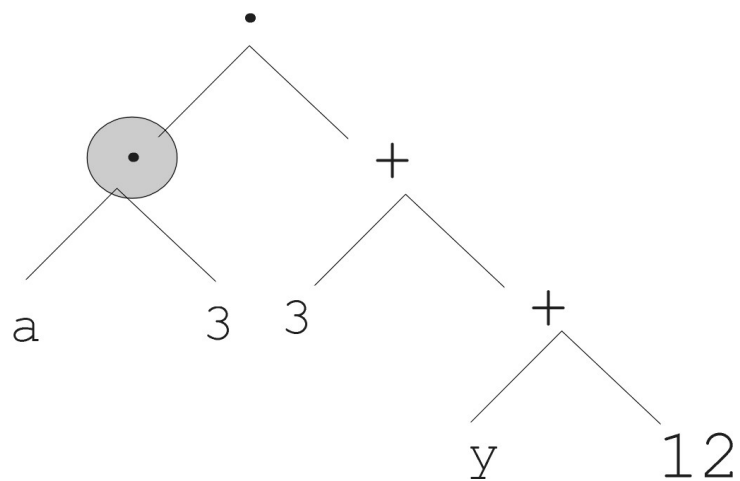
- Mutation has two parameters:
  - Probability  $p_m$  to choose mutation vs. recombination
  - Probability to choose an internal point as the root of the subtree to be replaced
- Remarkably  $p_m$  is advised to be 0 (Koza'92) or very small, like 0.05 (Banzhaf et al. '98)
- The size of the child can exceed the size of the parent

# Recombination

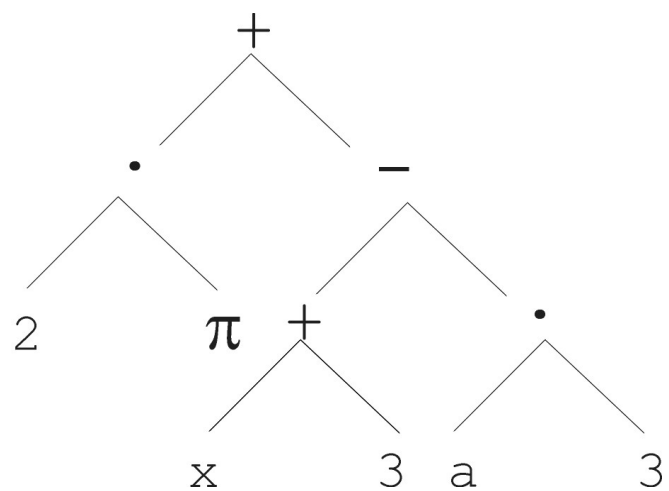
- Most common recombination: exchange two randomly chosen subtrees among the parents
- Recombination has two parameters:
  - Probability  $p_c$  to choose recombination vs. mutation
  - Probability to choose an internal point within each parent as crossover point
- The size of offspring can exceed that of the parents



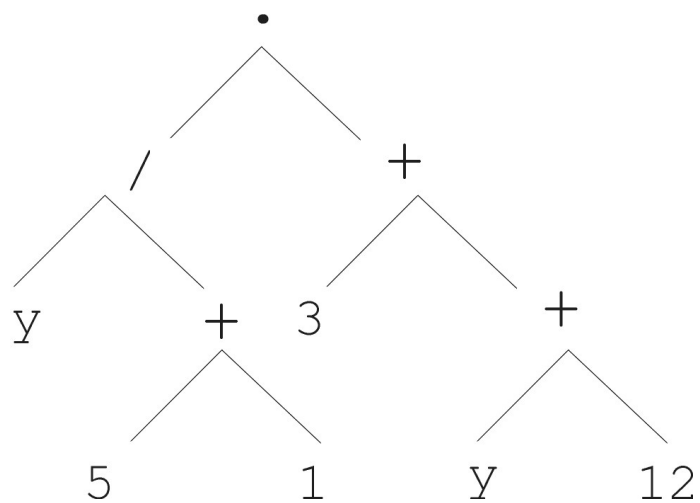
Parent 1



Parent 2



Child 1



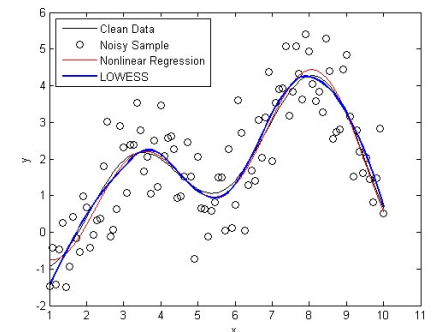
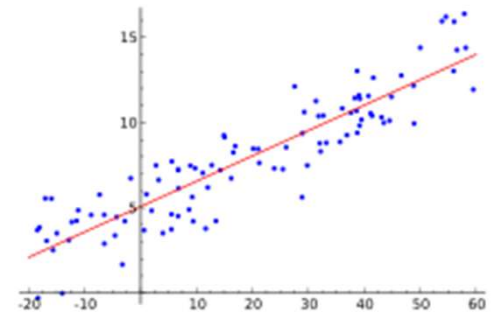
Child 2

# Problems involving “physical” environments

- Trees for data fitting vs. trees (programs) that are “really” executable
- Execution can change the environment → the calculation of fitness
- Example: robot controller
- Fitness calculations mostly by simulation, ranging from expensive to extremely expensive (in time)
- But evolved controllers are often to very good

# Example application: symbolic regression

- Given some points in  $\mathbf{R}^2$ ,  $(x_1, y_1), \dots, (x_n, y_n)$
- Find function  $f(x)$  s.t.  $\forall i = 1, \dots, n : f(x_i) = y_i$
- Possible GP solution:
  - Representation by  $F = \{+, -, /, \sin, \cos\}$ ,  $T = \mathbf{R} \cup \{x\}$
  - Fitness is the error 
$$err(f) = \sum_{i=1}^n (f(x_i) - y_i)^2$$
  - All operators standard
  - pop.size = 1000, ramped half-half initialisation
  - Termination: n “hits” or 50000 fitness evaluations reached (where “hit” is if  $|f(x_i) - y_i| < 0.0001$ )



# Bloat

- Bloat = “survival of the fattest”, i.e., the tree sizes in the population are increasing over time
- Ongoing research and debate about the reasons
- Needs countermeasures, e.g.
  - Prohibiting variation operators that would deliver “too big” children
  - Parsimony pressure: penalty for being oversized

# Discussion

Is GP:

The art of evolving computer programs ?

Means to automated programming of  
computers?

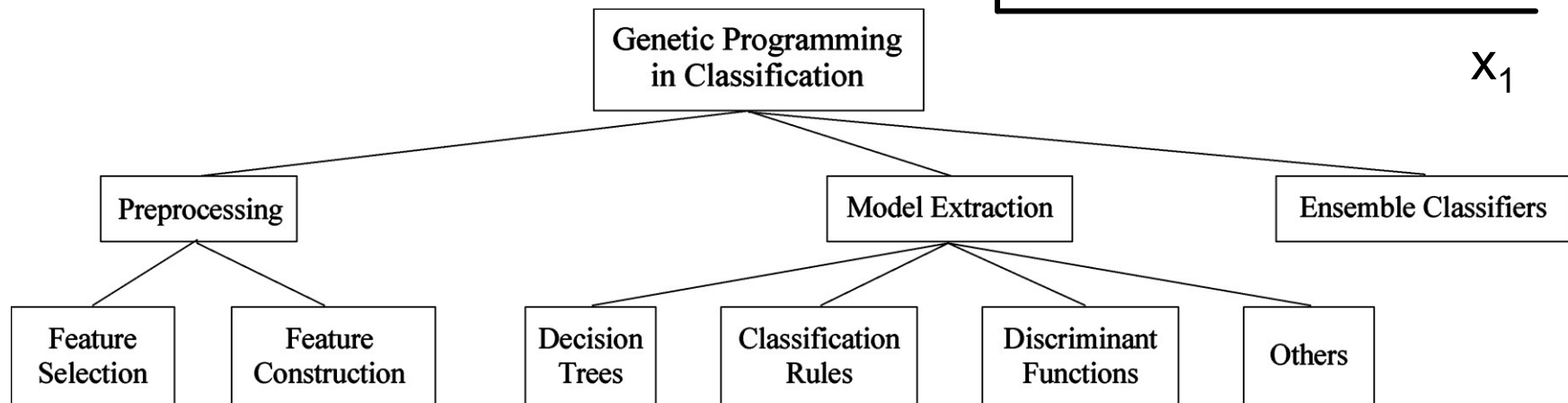
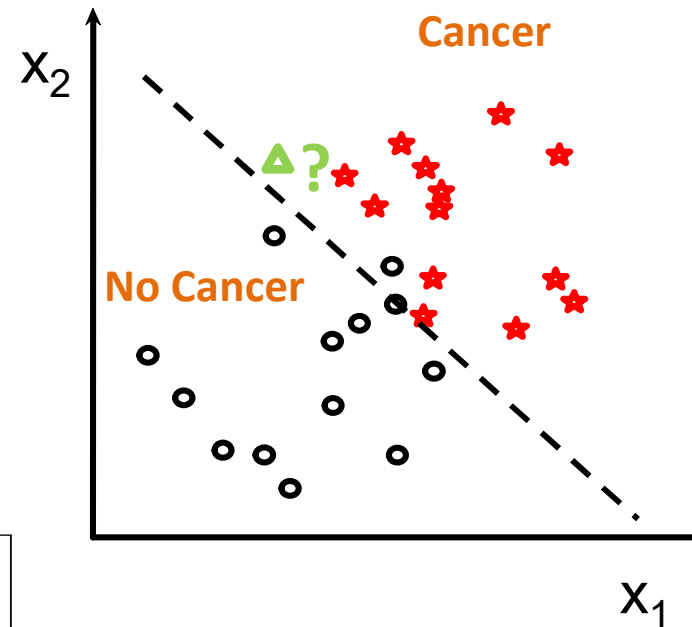
GA with another representation?

Machine Learning through Genetic Programming

# **GENETIC PROGRAMMING FOR CLASSIFICATION**

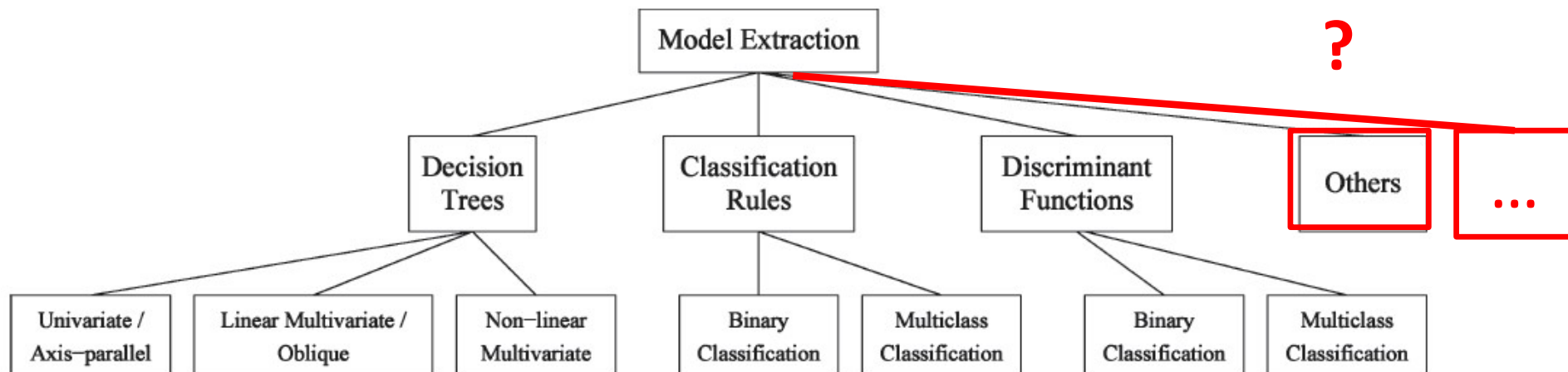
# GP for classification

- **Problem:** to learn a classification model from data.
  - Appropriate for other ML tasks.



# GP for classification

- **Problem:** to learn a classification model from data

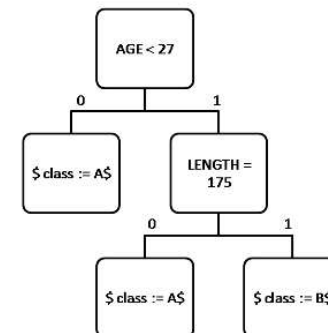
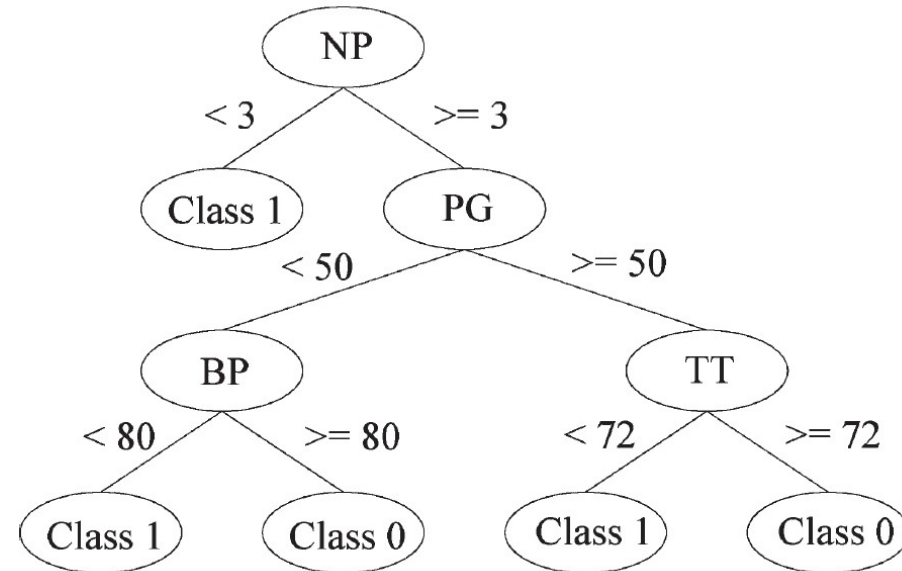


# GP for classification

- **General idea:** Design a GP where each individual represents a classifier (or a part of it). Defining a fitness function that evaluates the quality of the classifier.

# GP for classification

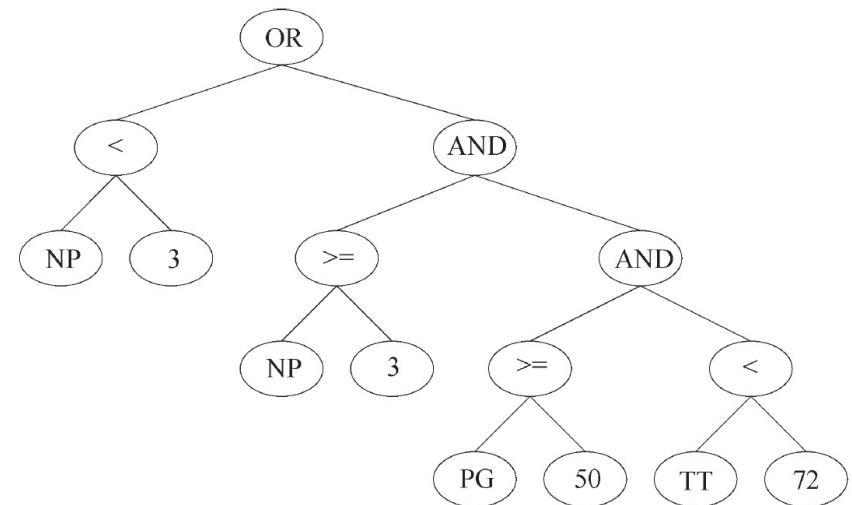
- **Decision trees:** A natural way to induce classifiers via GP
  - Typically one individual encodes a classifier (DT)
  - Internal nodes test the value of an expression on the attributes
  - Edges of IN are labeled with distinct outcomes
  - Each leaf node has a class label associated



Type of decision trees (approached with GP): axis parallel, oblique, nonlinear

# GP for classification

- **Rule-based systems:**  
Simple and easily interpretable way to represent knowledge
  - Two components: *antecedent* and *consequent*
  - Two main paradigms:
    - Individual=rule
    - Individual=set of rules

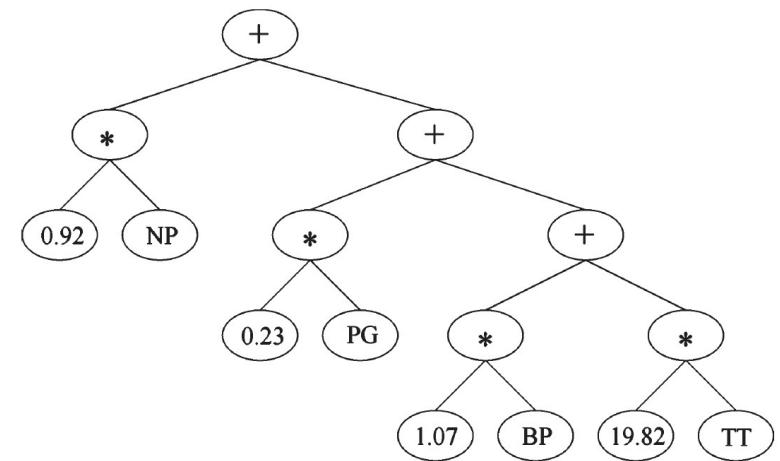


IF ((NP < 3)  
OR ((NP ≥ 3) AND (PG ≥ 50) AND (TT < 72)))  
THEN Class 1.

Binary vs. Multiclass

# GP for classification

- **Discriminant functions:** A discriminative mathematical expression
  - The evaluation of the mathematical expression indicates the class (threshold, usually 0)



$$0.92*NP + 0.23*PG + 1.07*BP + 19.82*TT$$

Binary vs. Multiclass

Machine Learning through Genetic Programming

# **APPLICATIONS**

Representation learning

Automatic generation of classification prototypes

Ensemble generation

Term-weighting scheme learning

# SOME APPLICATIONS OF GP ON MACHINE LEARNING PROBLEMS

Representation learning

Automatic generation of classification prototypes

Ensemble generation

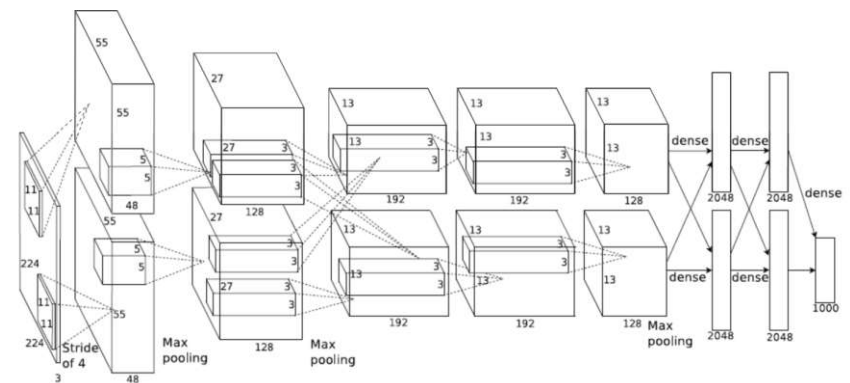
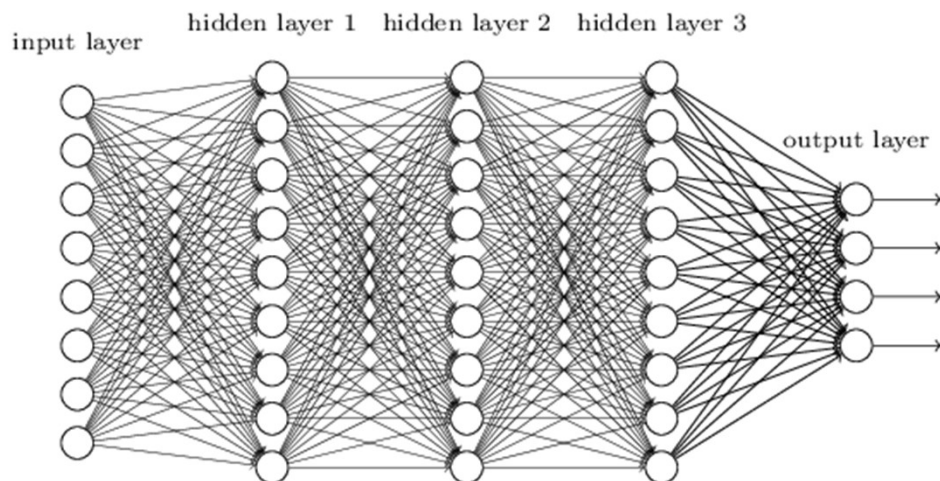
Term-weighting scheme learning

# SOME APPLICATIONS OF GP ON MACHINE LEARNING PROBLEMS

Lino Rodriguez-Coayahuitl, Alicia Morales-Reyes, Hugo Jair Escalante. **Towards Deep Representation Learning with Genetic Programming**. Accepted to EuroGP 2018

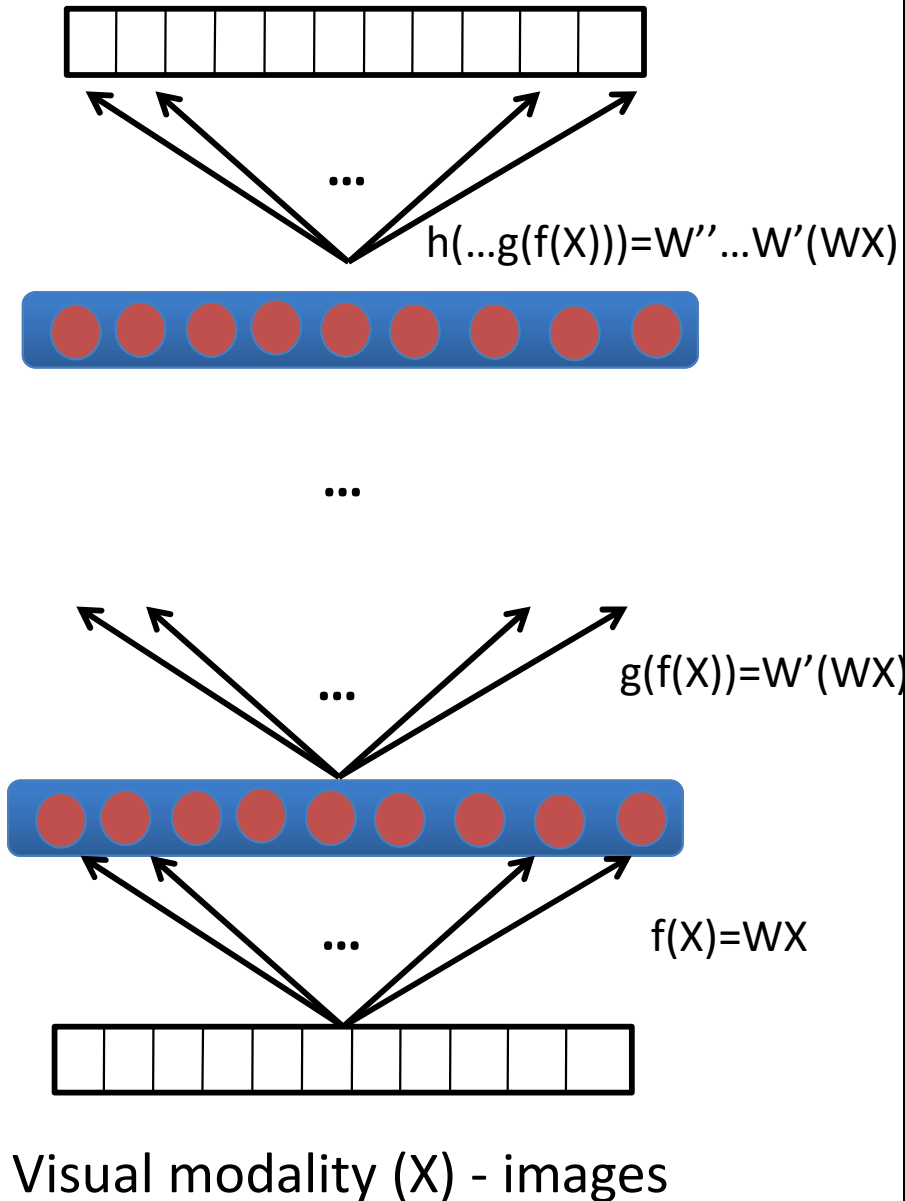
# Deep Genetic Programming

- Deep learning is the state of the art methodology for most computer vision (and NLP) tasks
- The methodology consists of iteratively training NNs with multiple layers using big data!
- Idea: Learning deep models with EC!



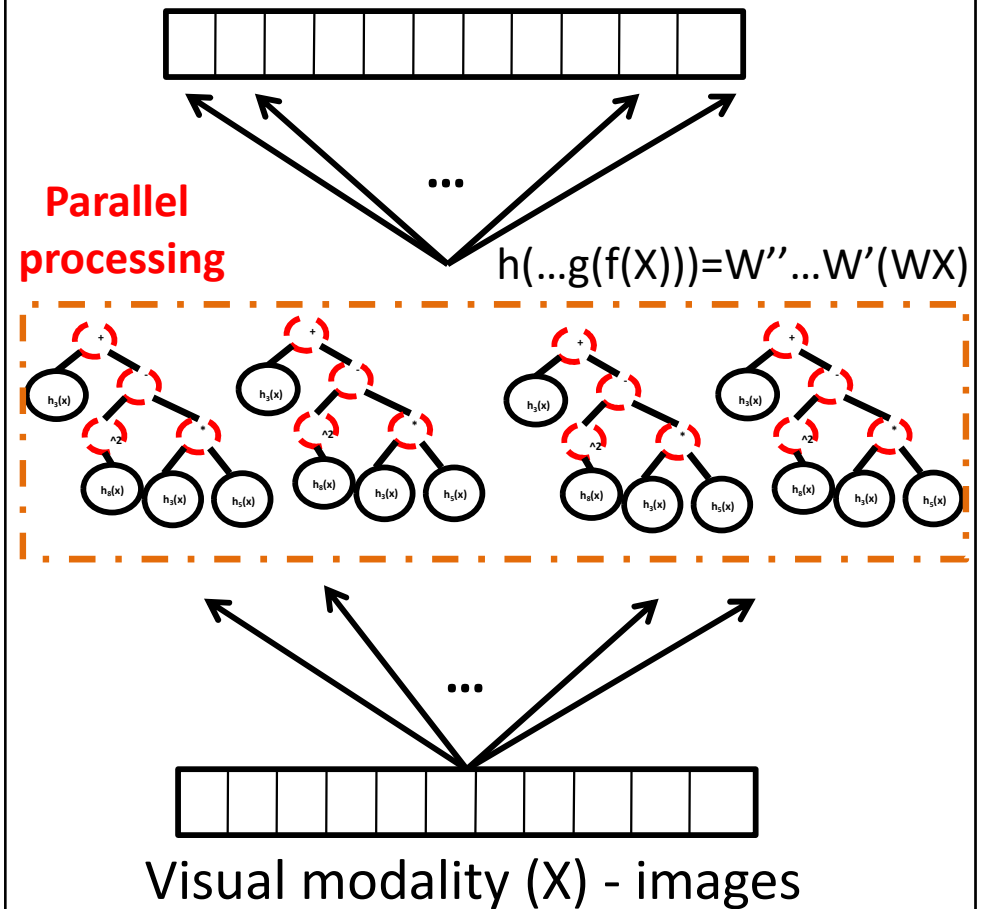
## Standard deep learning

Textual modality (Y) - Captions



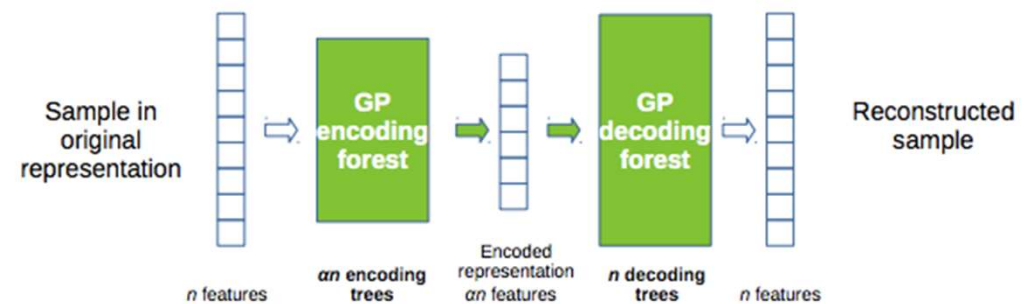
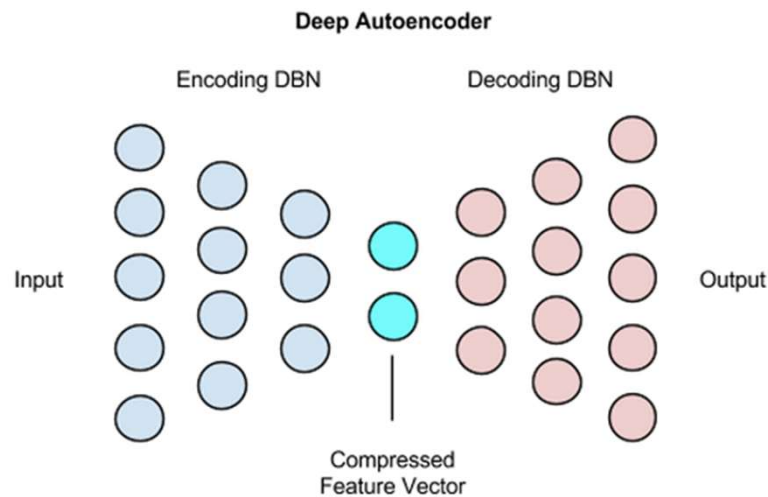
## Proposal: deep learning through parallel genetic programming

Textual modality (Y) - Captions



# Deep Genetic Programming

- Our first results

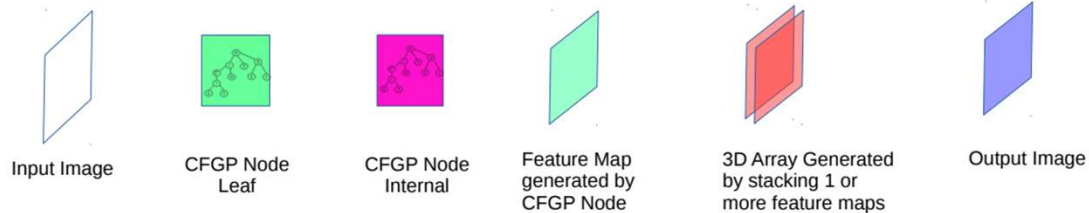
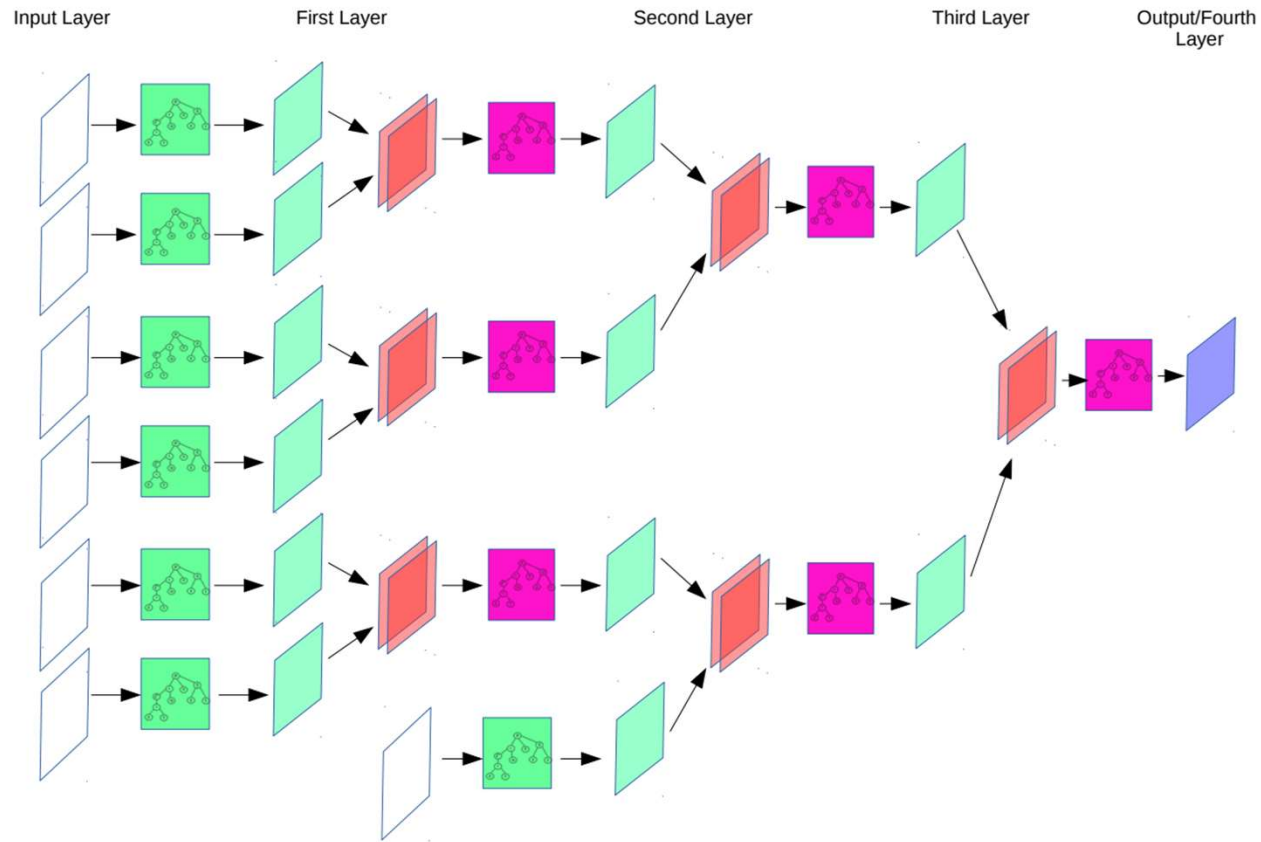


Lino Rodriguez-Coayahuitl, Alicia Morales-Reyes, [Hugo Jair Escalante](#). Towards Deep Representation Learning with Genetic Programming. Accepted, EuroGP 2018

# Initial results – Deep genetic programming

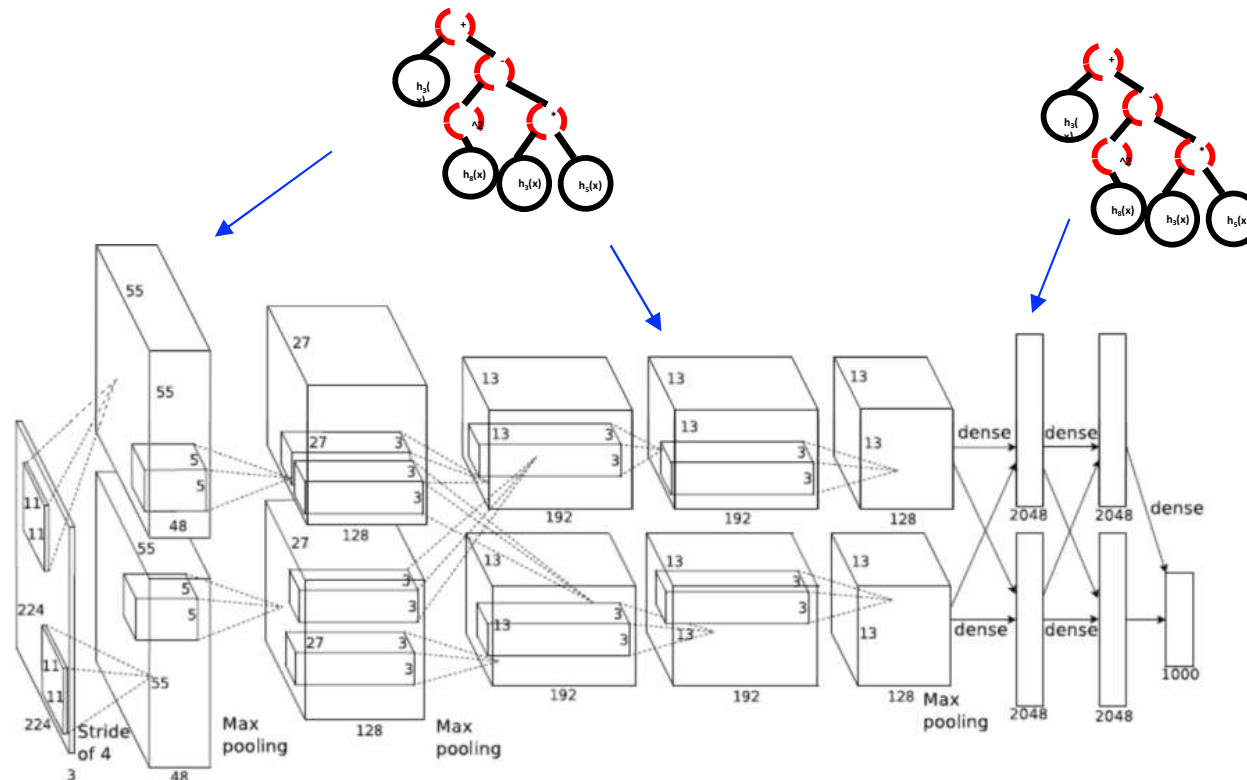


# Convolutional GP



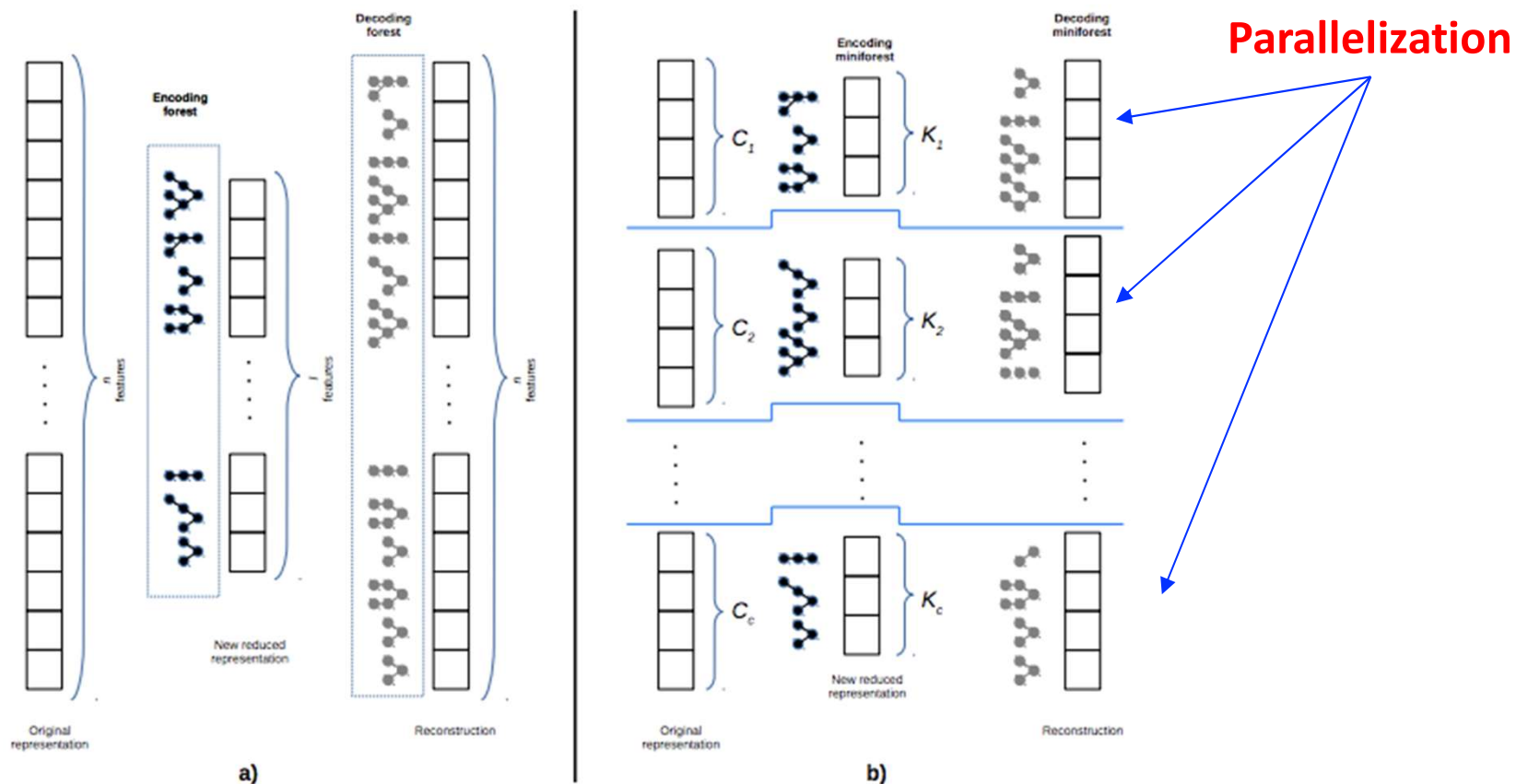
# Open projects on deep genetic programming

- Evolutionary learning of layers in deep convolutional networks
- Hybrid Deep Net-GP: Efficient, effective fine tuning



# Open projects on deep genetic programming

- Parallel GP for deep representation learning
- Exploit massive parallelization capabilities of GPUs to accelerate the learning process



Representation learning

Automatic generation of classification prototypes

Ensemble generation

Term-weighting scheme learning

# SOME APPLICATIONS OF GP ON MACHINE LEARNING PROBLEMS

Representation learning

Automatic generation of classification prototypes

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# SOME APPLICATIONS OF GP ON MACHINE LEARNING PROBLEMS

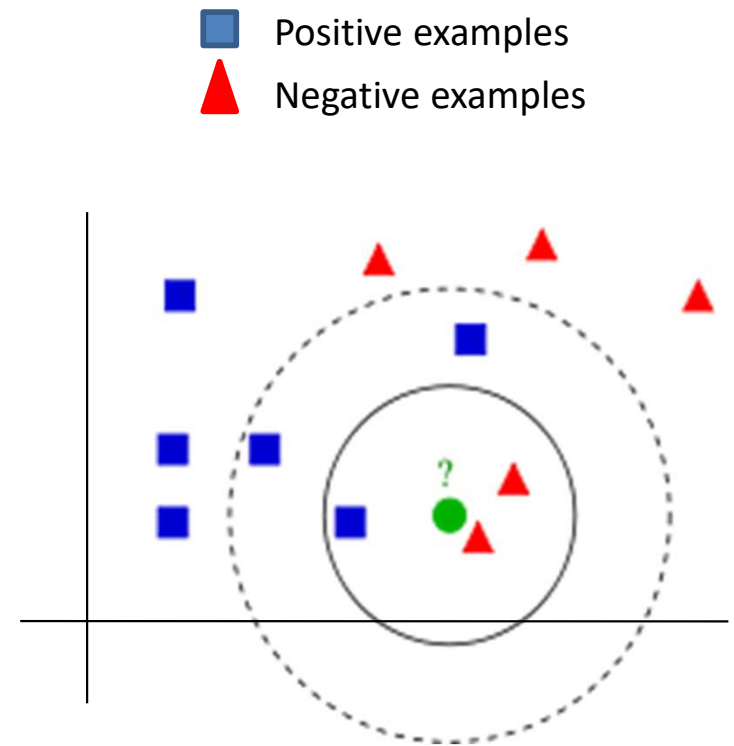
H. J. Escalante, K. Mendoza, M. Graff, A. Morales-Reyes. **Genetic Programming of Prototypes for Pattern Classification**. IbPRIA 2013: 6th Iberian Conference on Pattern Recognition and Image Analysis, Madeira, Portugal. June 5-7, 2013

H. J. Escalante, M. Graff, A. Morales-Reyes. **PGGP: Prototype Generation via Genetic Programming**. *Applied Soft Computing*, 2016

# Genetic programming of classification prototypes

- **Problem:** Given a labeled data set of a classification task to select a (**small**) subset of instances such that the classification performance of a particular classifier (KNN) is not degraded significantly
- **Naïve approach:** take as prototype of class  $C_i$  to the average of instances that belong to class  $C_i$

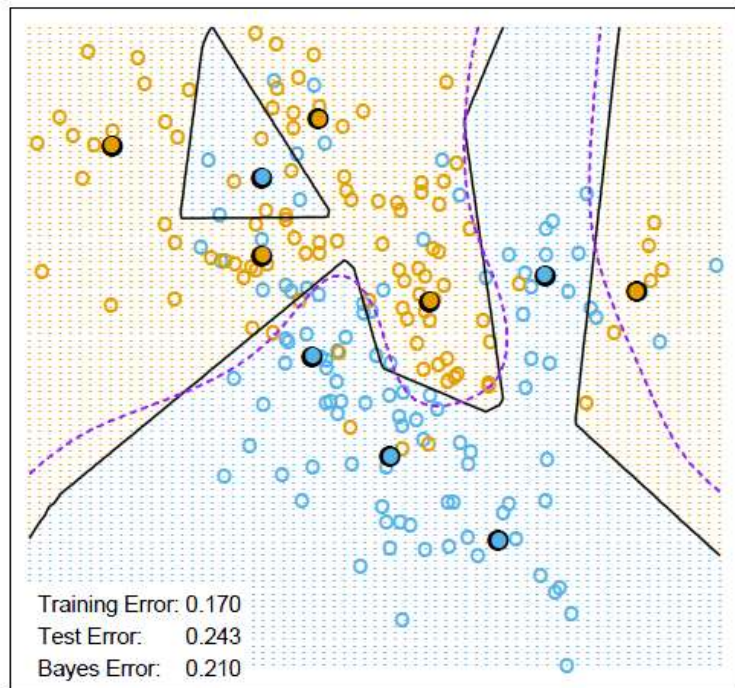
$$\mathbf{p}_i = \frac{1}{N_i} \sum_{\mathbf{x}_j: y_j = C_i} \mathbf{x}_j$$



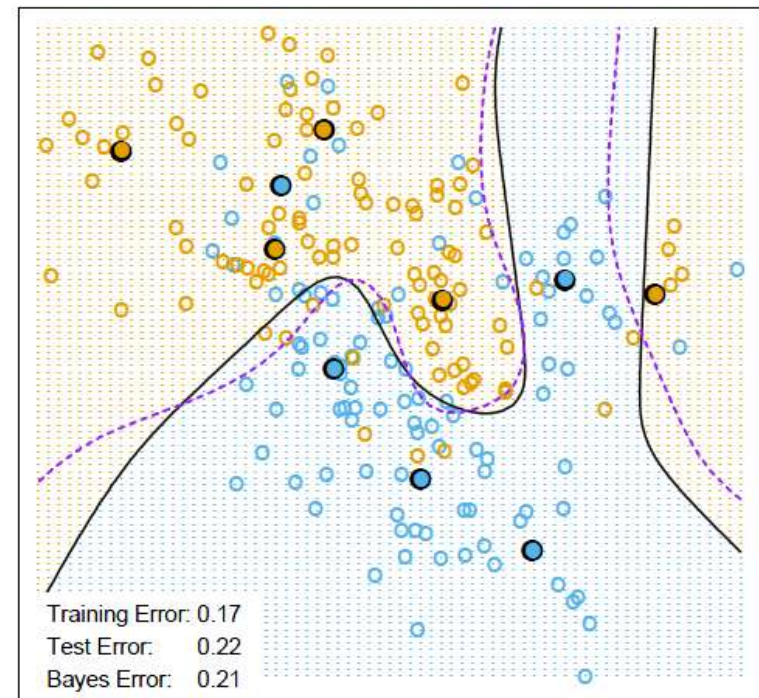
# Genetic programming of classification prototypes

- Prototype generation:

K-means - 5 Prototypes per Class



Gaussian Mixtures - 5 Subclasses per Class



# Genetic programming of classification prototypes

- **Proposed solution:** using GP to learn how to combine instances of the same class to generate prototypes

Naïve approach

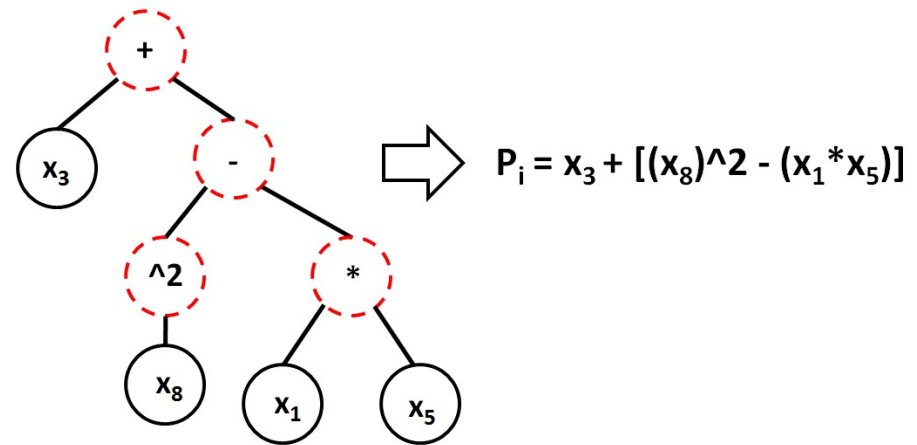
$$\mathbf{p}_i = \frac{1}{N_i} \sum_{\mathbf{x}_j : y_j == C_i} \mathbf{x}_j$$

Genetic program

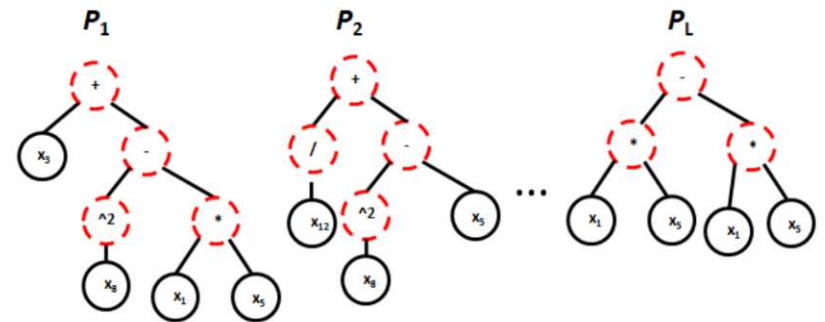
$$\mathbf{p}_i = \boxed{f(\mathbf{x}_j)}, \quad ? \quad \mathbf{x}_j : y_j == C_i$$

# Genetic programming of classification prototypes

- Each tree codifies the prototype for a particular class



- An individual is a set of prototypes (a set of trees)



# Genetic programming of classification prototypes

- Standard GP,
  - Two-crossover operators
  - Mutation
  - New (mitosis) operator

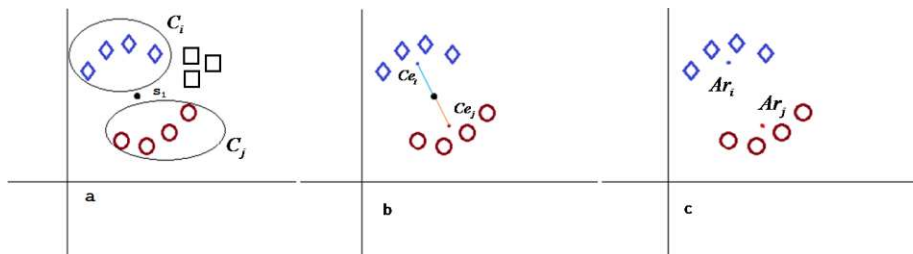
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**Algorithm 2** Overview of the ( $GP^2$ ) algorithm.

---

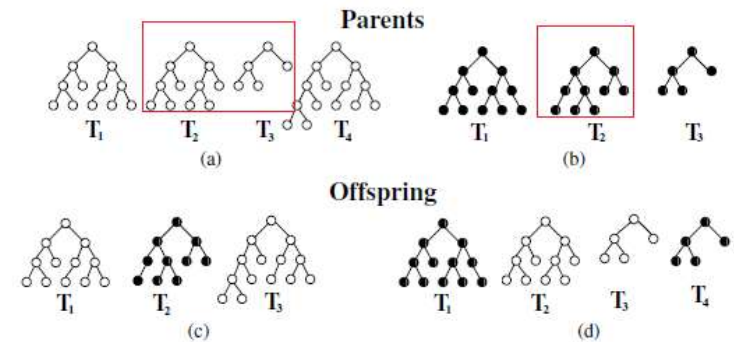
**Require:** Training data set  $T = \{(x_1, y_1), \dots, (x_N, y_N)\}$ ;  
 Set  $S = \{\}$ ;  
 for  $i = 1 \rightarrow k$  do  
     Split training data ( $T$ ) into development ( $D$ ) and validation ( $V$ ) sets;  
     {where  $T = D \cup V, D \cap V = \emptyset$ };  
      $U \leftarrow GPGP(D, V)$ ;  
      $S = S \cup U$   
 end for  
 return  $S$

---

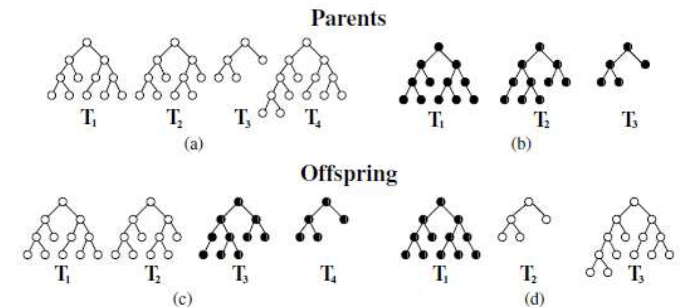


**Mitosis**

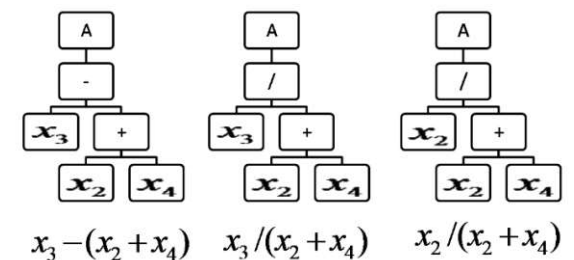
## Crossover 1



## Crossover 2

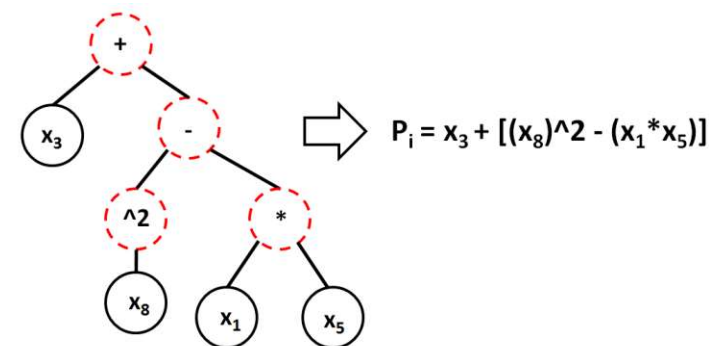


## Mutation



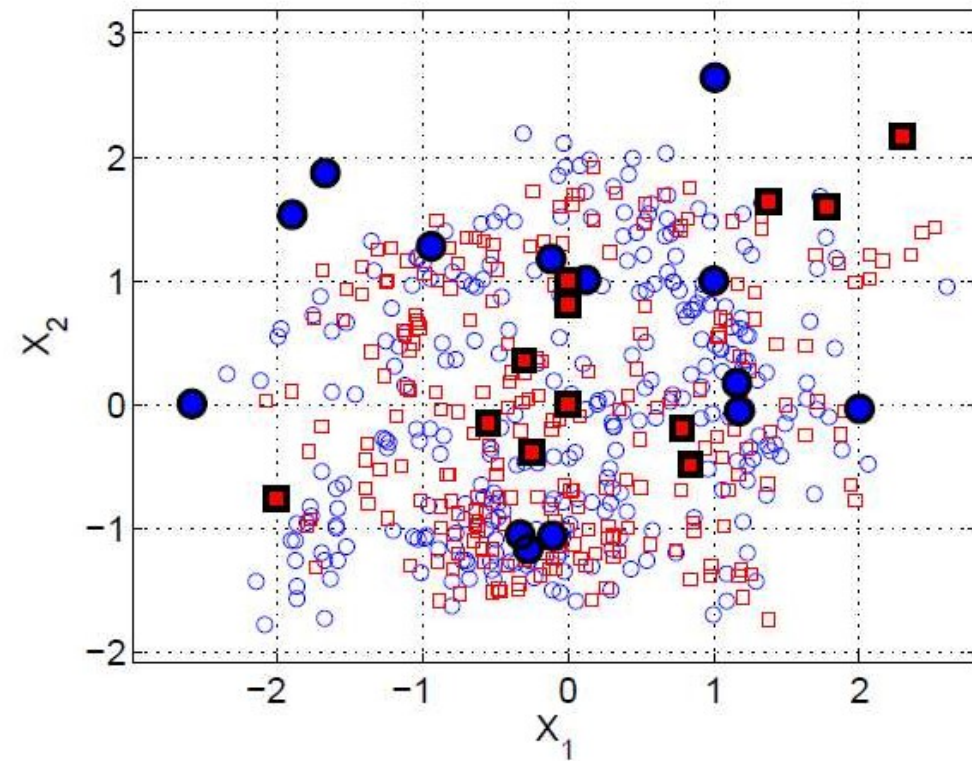
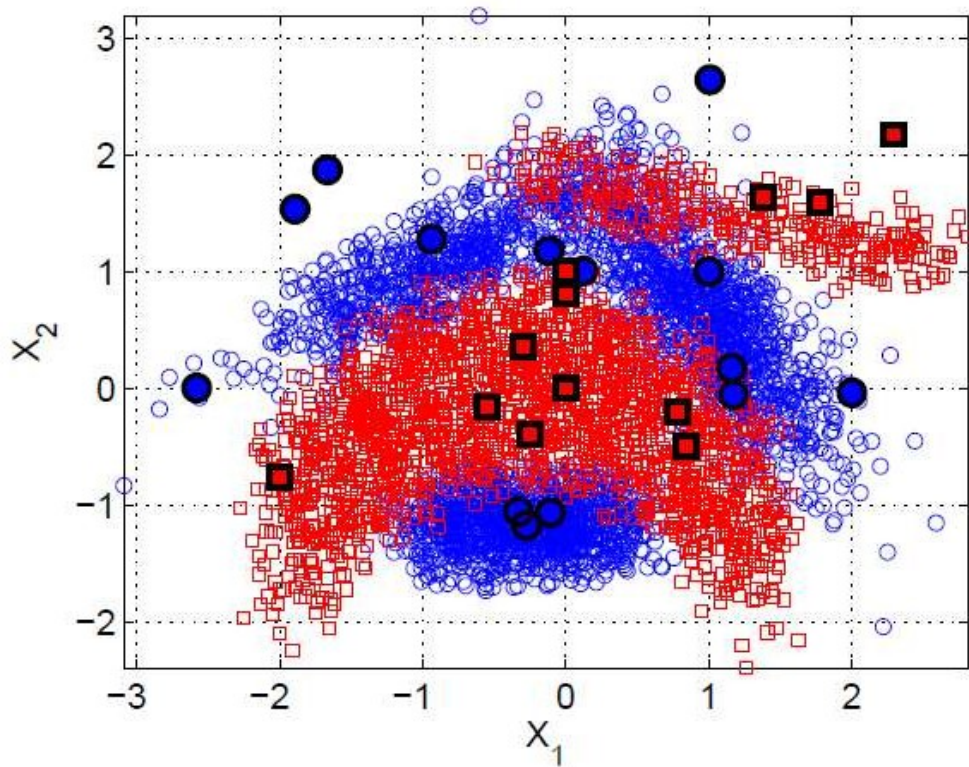
# Genetic programming of classification prototypes

- **Fitness function:** accuracy in a validation set
- **Terminals:** all of the instances in the training set (except those used in the validation set)
- **Function set:** \*, /, +, -, ^2, sqrt



# Genetic programming of classification prototypes

- Sample solution:



# Genetic programming of classification prototypes

- Sample prototypes:

```
sum([0.0232, -0.12],sum([-0.0097, -0.0883],abs(abs(sum(x(4632,:),x(1884,:))))))
    sum([-0.17, -0.068],sum([-0.22, -0.23],sin(cos(my-power(x(1557,:))))))
        sum(x(64,:),sin(cos(my-power(x(1557,:))))))
sum([-0.23, -0.18],sum([-0.29, 0.036],sum([-0.060, 0.031],abs(abs(sum(x(4632,:),x(1884,:)))))))
    sum([-0.29, 0.036],sum([-0.06, 0.031],abs(abs(sum(x(4632,:),x(1884,:))))))
        abs(x(4686,:))
            minT(x(2412,:),x(351,:))
sum(abs(cos(tan(x(1224,:))))),my-power-3(mult(mult(x(2296,:),x(2250,:)),sin(x(1456,:))))
```

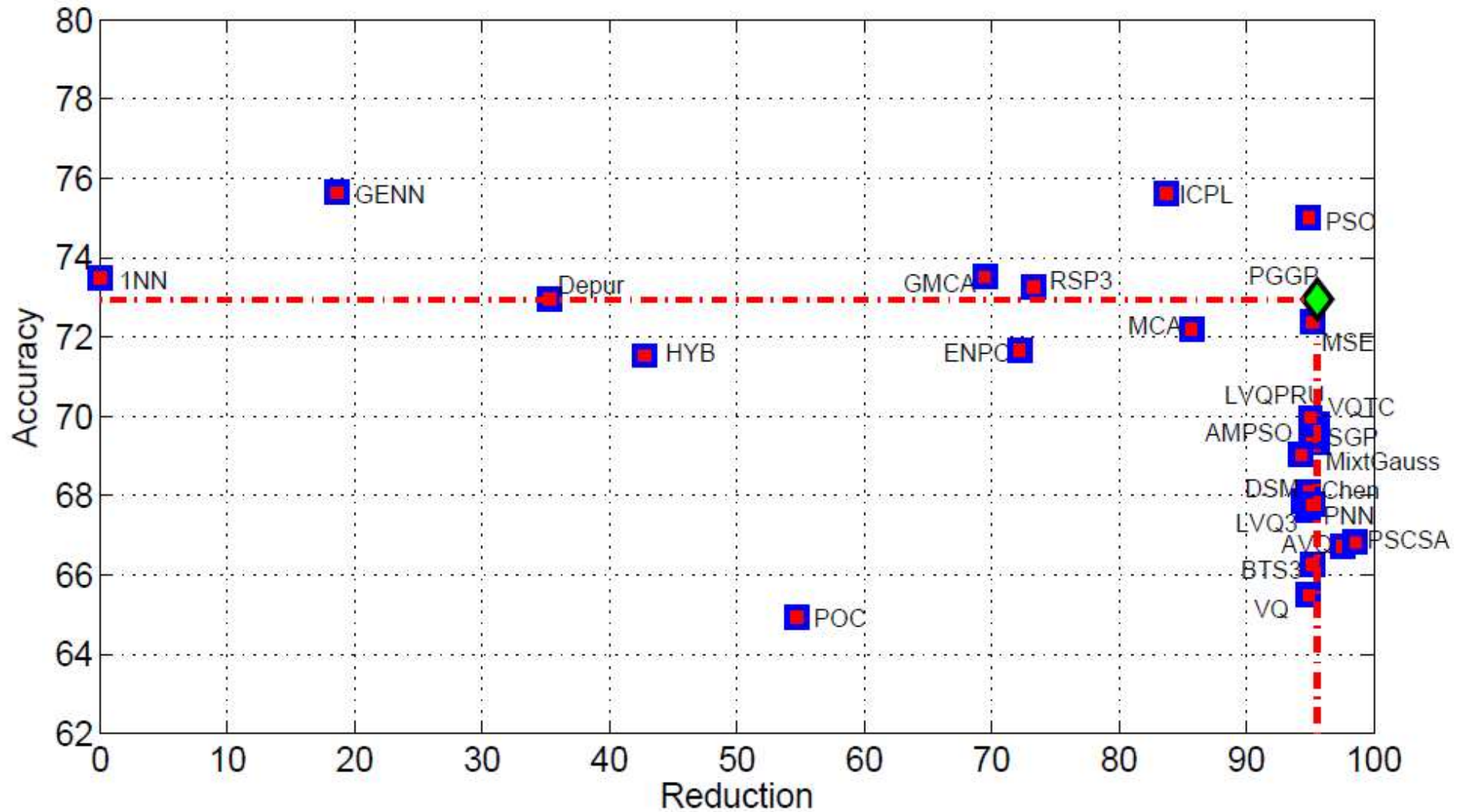
# Genetic programming of classification prototypes

- Results: comparison with 24 other methods in a benchmark of 59 data sets for classification

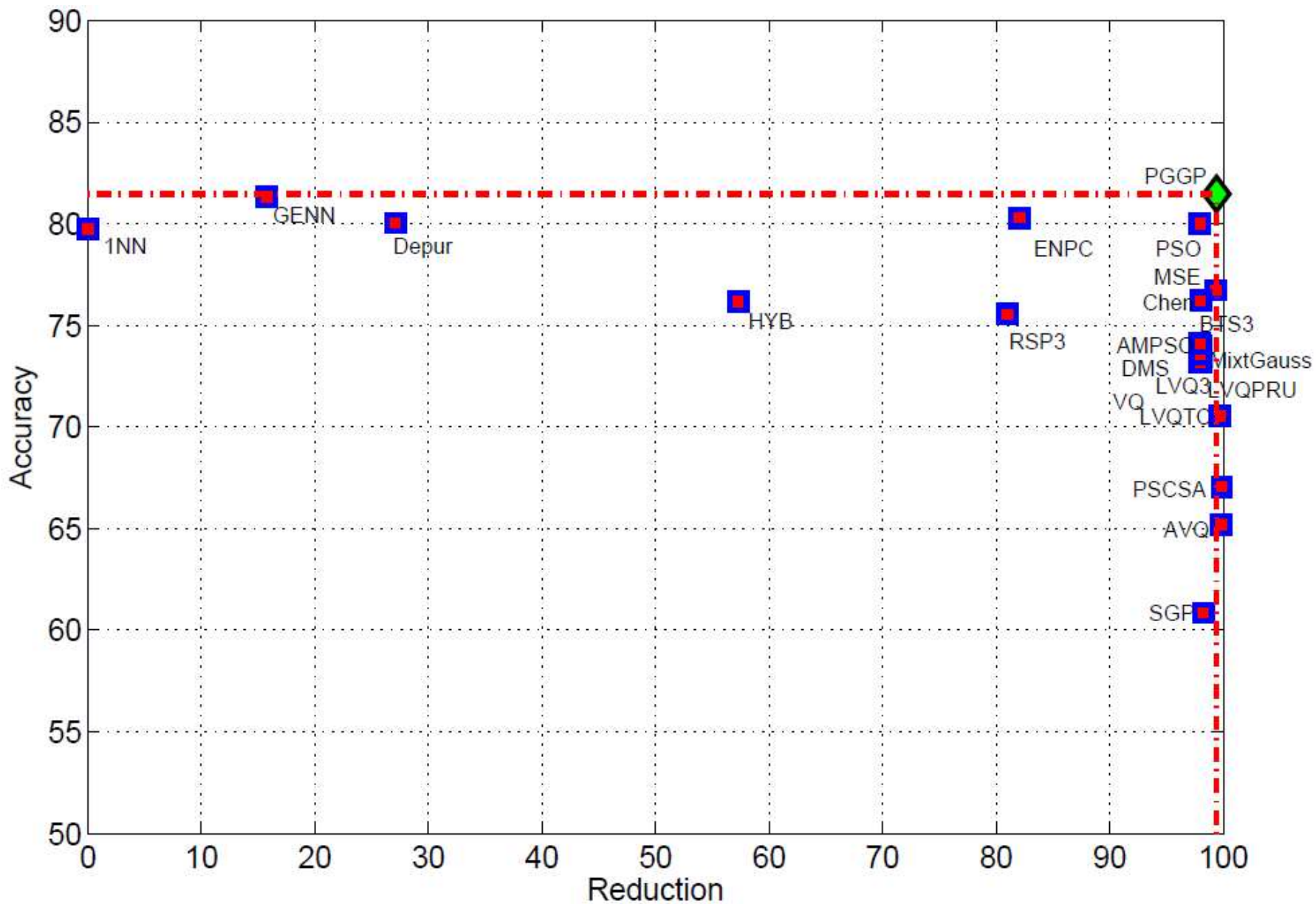
Measure	Test accuracy			Training set reduction		
	All	Small	Large	All	Small	Large
PGGP	74.54%±5.18	72.95%±16.25	<b>81.47%±20.01</b>	96.81%	95.58%	99.42%
GENN	<b>78.48%±18.57</b>	<b>75.64%±15.45</b>	81.33%±21.70	17.19%	18.62%	15.76%
PSCSA	66.94%±20.39	66.82%±18.74	67.07%±22.05	<b>99.23%</b>	<b>98.58%</b>	<b>99.88%</b>
1NN	77.04%±19.44	73.48%±16.64	80.60%±22.24	0%	0%	0%

<http://sci2s.ugr.es/pgtax/code.php>

# Accuracy vs reduction (small)

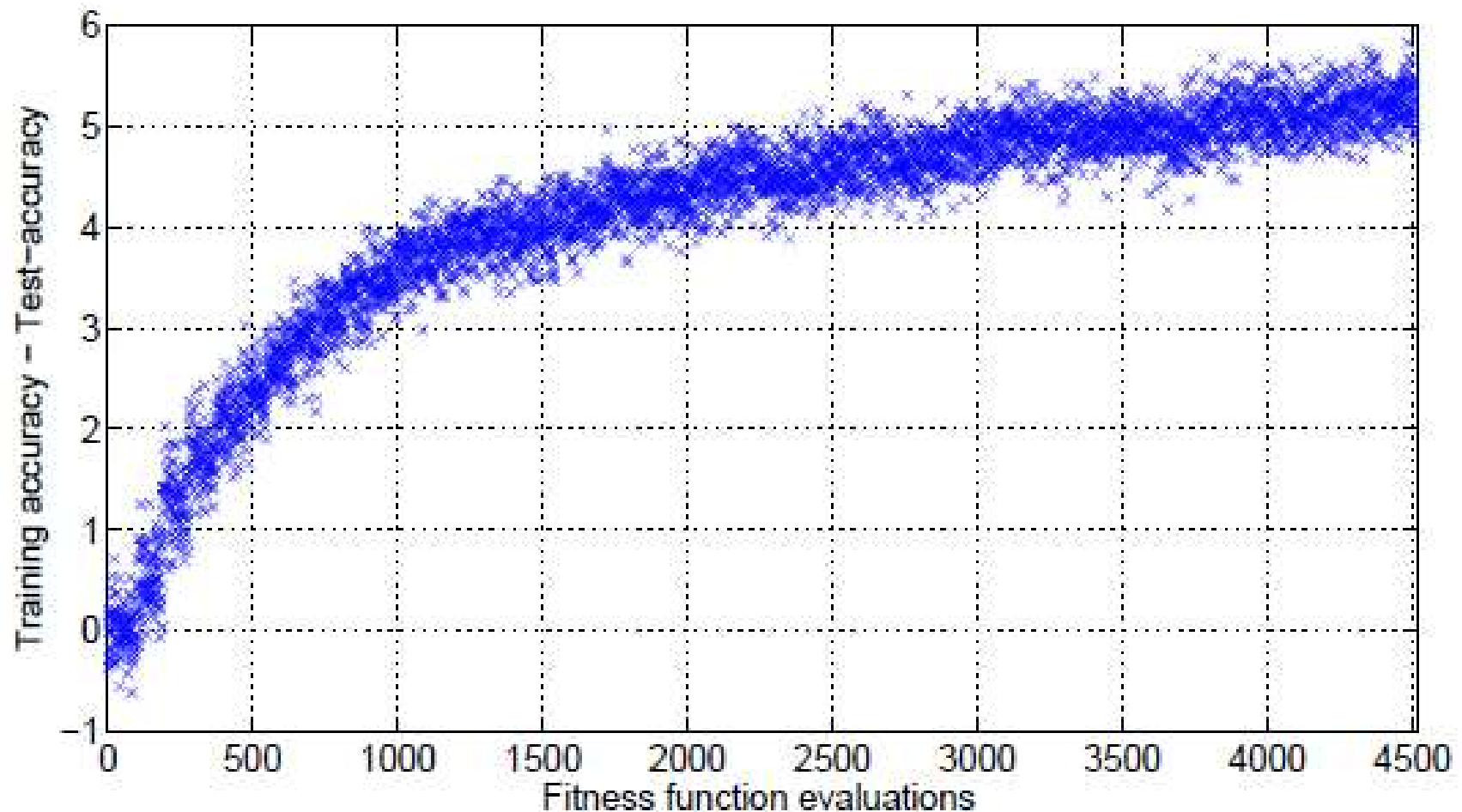


# Accuracy vs reduction (large)



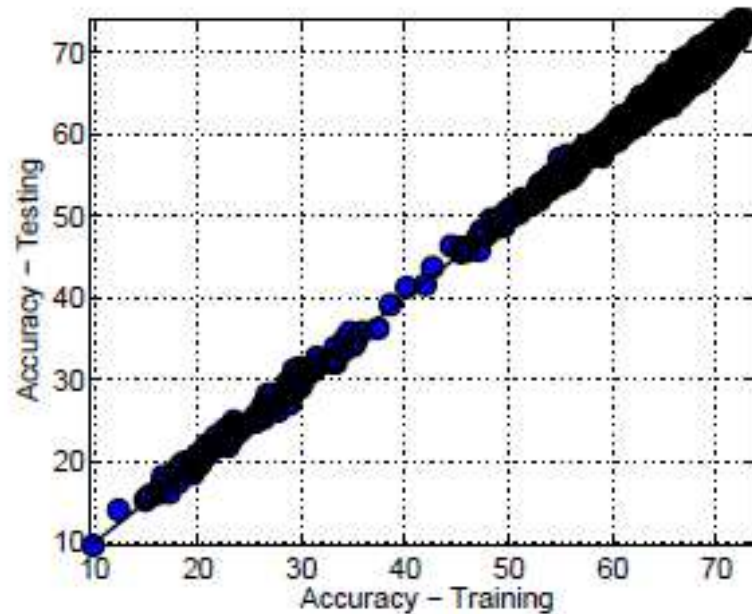
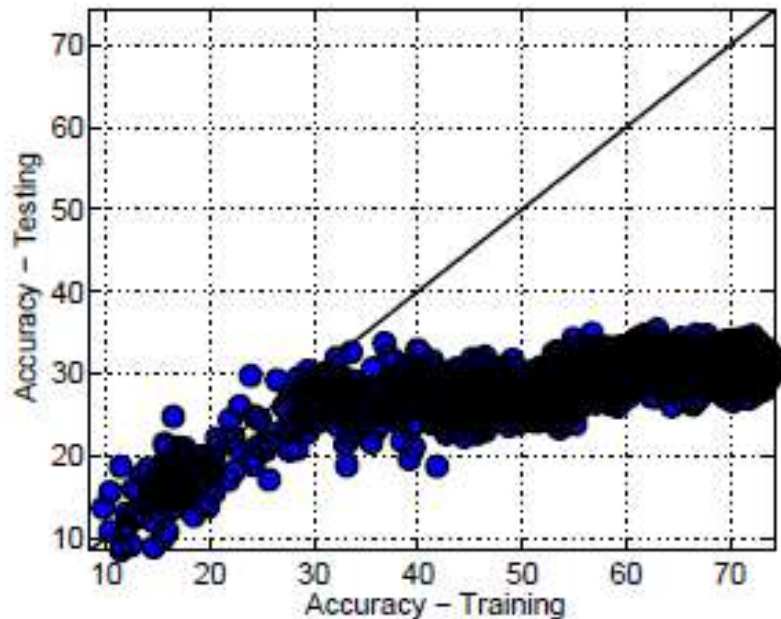
# Genetic programming of classification prototypes

- Overfitting:



# Genetic programming of classification prototypes

- Overfitting:



- Training set accuracy vs. Test set accuracy for the autos (205 instances and 6 classes) and car (1728 instances and 4 classes) data sets.

# Genetic programming of classification prototypes

- Promising results with GP
- Too much work to do yet!
  - Overfitting is one of the main issues
  - Computationally expensive
  - Conflicting objectives
- Extensions:
  - Multi-objective prototype generation
  - Simultaneous generation of features and prototypes

Representation learning

Automatic generation of classification prototypes

Ensemble generation

Term-weighting scheme learning

# SOME APPLICATIONS OF GENETIC PROGRAMMING IN MACHINE LEARNING

H. J. Escalante, N. Acosta, A. Morales, A. Gago. **Genetic Programming of Heterogeneous Ensembles for Classification**, Progress in Pattern Recognition, Image Analysis, Computer Vision and Applications,, CIARP, Havana, Cuba, November 20-23, Proceedings, Part I, LNCS 8258, pp. 9—16, Springer, 2013.

N. Acosta, A. Morales, H. J. Escalante, A. Gago. **Learning to Assemble Classifiers via Genetic Programming**. International Journal of Pattern Recognition and Artificial Intelligence, 2014.

# Introduction

- Ensembles classification principle:
  - Combining classifiers models to improve overall performance
- Homogeneous ensembles
  - Combine outputs of the same classifier trained in different data
- Heterogeneous ensembles
  - Combining classifiers of different nature such as decision trees, neural networks, etcetera
- Normally, combination of classifiers' outputs is carried out by voting or linear combination of scores.

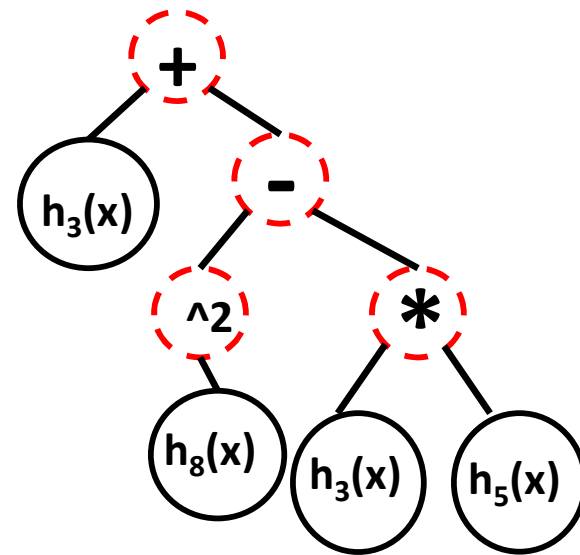
Can we do it better than that?

# Introduction

- An evolutionary algorithm is proposed to learn a fusion function that combines the outputs of heterogeneous classifiers in order to maximize the accuracy of the ensemble
  - Genetic programming
    - A population of fusion functions is evolved

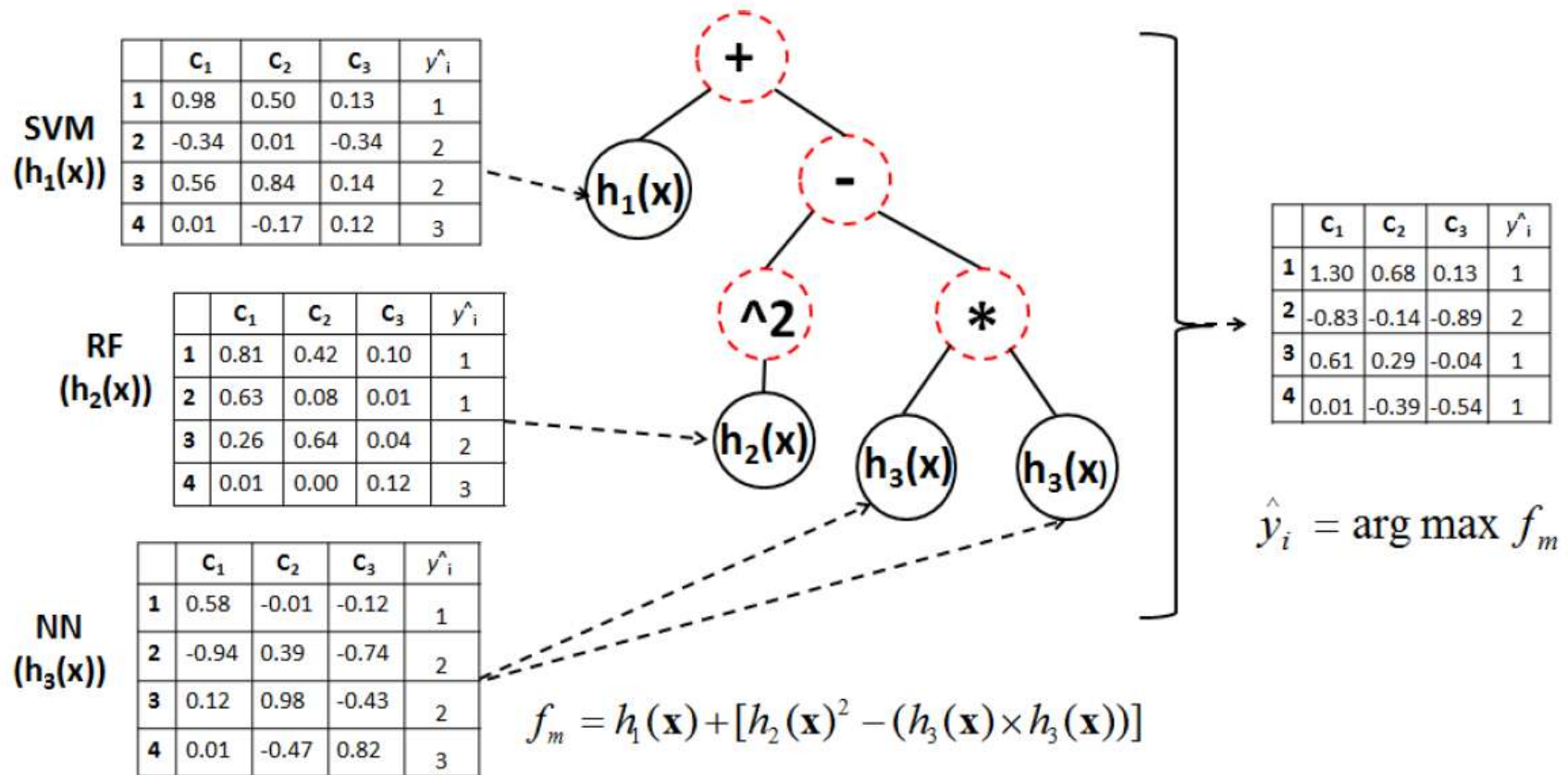
# Genetic programming of ensembles

- GP encodes solutions using trees
  - Nodes are classification models with constants (incorporating a weighting factor)
  - Non-leaf nodes are operators

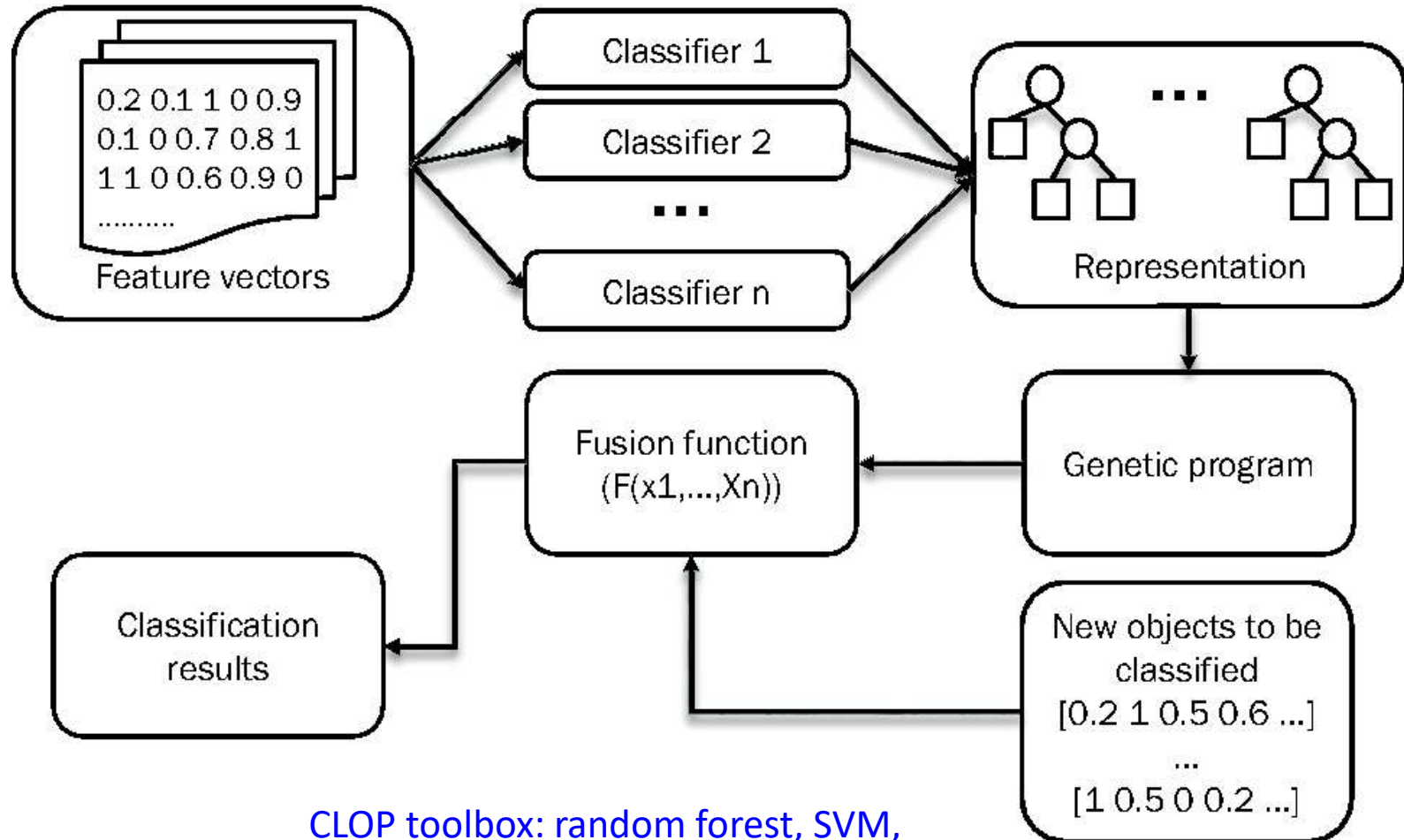


$$f_m = h_3(\mathbf{x}) + [h_8(\mathbf{x})^2 - (h_3(\mathbf{x}) \times h_5(\mathbf{x}))]$$

# Genetic programming of ensembles



# Genetic programming of ensembles



CLOP toolbox: random forest, SVM, Logistic, linear kriging, non-linear kriging, 1NN, 3NN, Naïve Bayes, gkriging, NN

# Experimental results

- GP configuration
  - GPLAP framework
  - Standard crossover and mutation operators
  - Population initialization: ramped-half-and-half
  - Population size 50 individuals
  - 100 generations
  - 10 runs
- Experimental data
  - UCI- data sets
  - SCEF – object recognition problem
    - 6244 image-regions
    - 737 attributes
    - 10 classes
    - Dataset division
      - 3615 testing
      - 2629 training

# Experimental results - SCEF

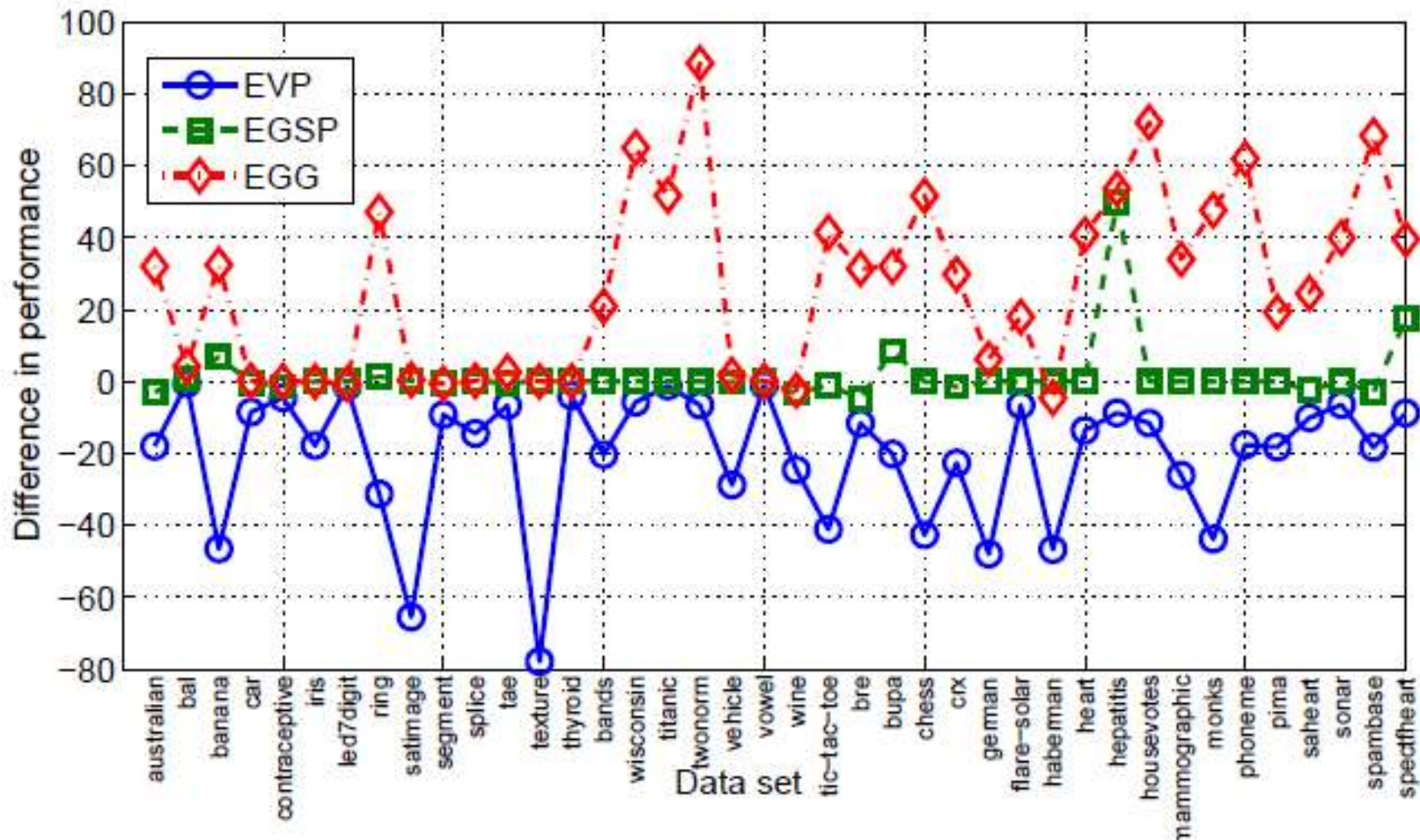
Table 2. Results (%) obtained by individual classifiers in terms of accuracy/ $f_1$  measure over SCEF data set.

	RF	SVM	Klogistic	Kridge-l	Kridge-n	1NN	3NN	N.Bayes	Gkridge	Neural N
Acc.	<b>90.70</b>	55.10	70.60	13.64	74.70	69.30	69.10	26.50	20.60	55.80
$f_1$	<b>79.30</b>	49.90	62.80	2.400	63.10	60.10	57.40	21.60	3.421	37.70

Table 3. Results (%) obtained by different strategies over SCEF data set when optimizing accuracy (top) and  $f_1$  (bottom). AVE: raw fusion; GPE-a: GP uses only sums; GPE: proposed GP.

	AVE	AVE-Top5	GPE-a	GPE-a-Top5	GPE	GPE-Top5
Acc.	31.50	81.40	90.80(0.001)	91.10(0.002)	<b>92.30(0.002)</b>	91.20(0.001)
$f_1$ .	27.2	71.90	80.40(0.001)	80.40(0.001)	<b>85.30(0.003)</b>	80.55(0.003)

# Experimental results - UCI



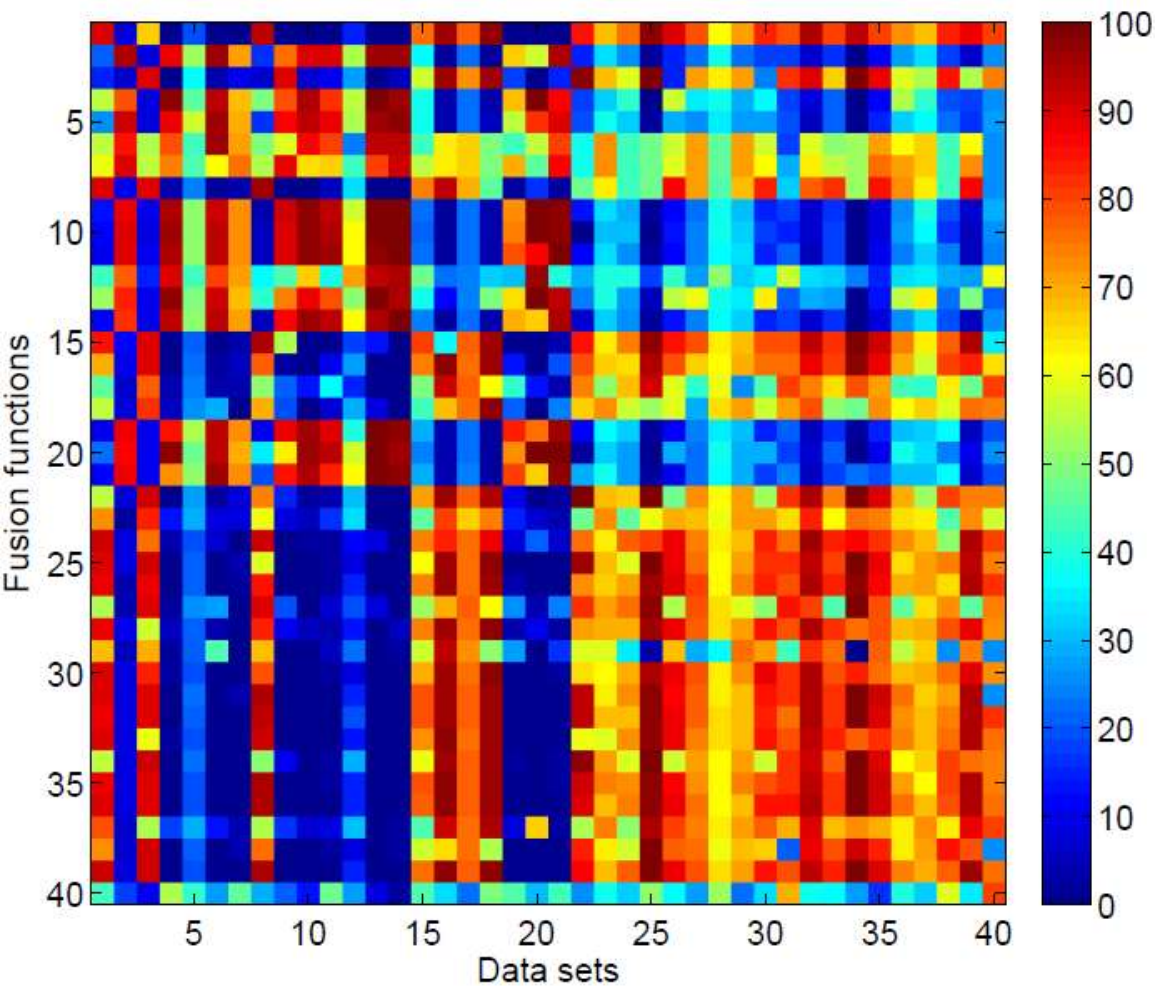
	B-Classifier	EVP	EGSP	EGG
Acc.	61.01(25.18)	40.23(27.91)	62.68(24.45)	85.75(12.21)
$f_1$ .	63.50(26.32)	31.06(29.00)	62.91(26.71)	84.49(14.94)

# Experimental results - UCI

Table 4. Average and standard deviation performances for B-Classifier: best classifier; AVE: raw fusion; GPE-a: GP using only sums; GPE: proposed GP.

	B-Classifier	AVE	GPE-a	GPE
Acc.	61.01(25.18) <sub>(1,0,-)</sub>	40.23(27.91) <sub>(-, -, -)</sub>	62.68(24.45) <sub>(0,1,-)</sub>	<b>85.75(12.21)</b> <sub>(1,1,1)</sub>
$f_1$ .	63.50(26.32) <sub>(1,0,-)</sub>	31.06(29.00) <sub>(-, -, -)</sub>	62.91(26.71) <sub>(0,1,-)</sub>	<b>84.49(14.94)</b> <sub>(1,1,1)</sub>

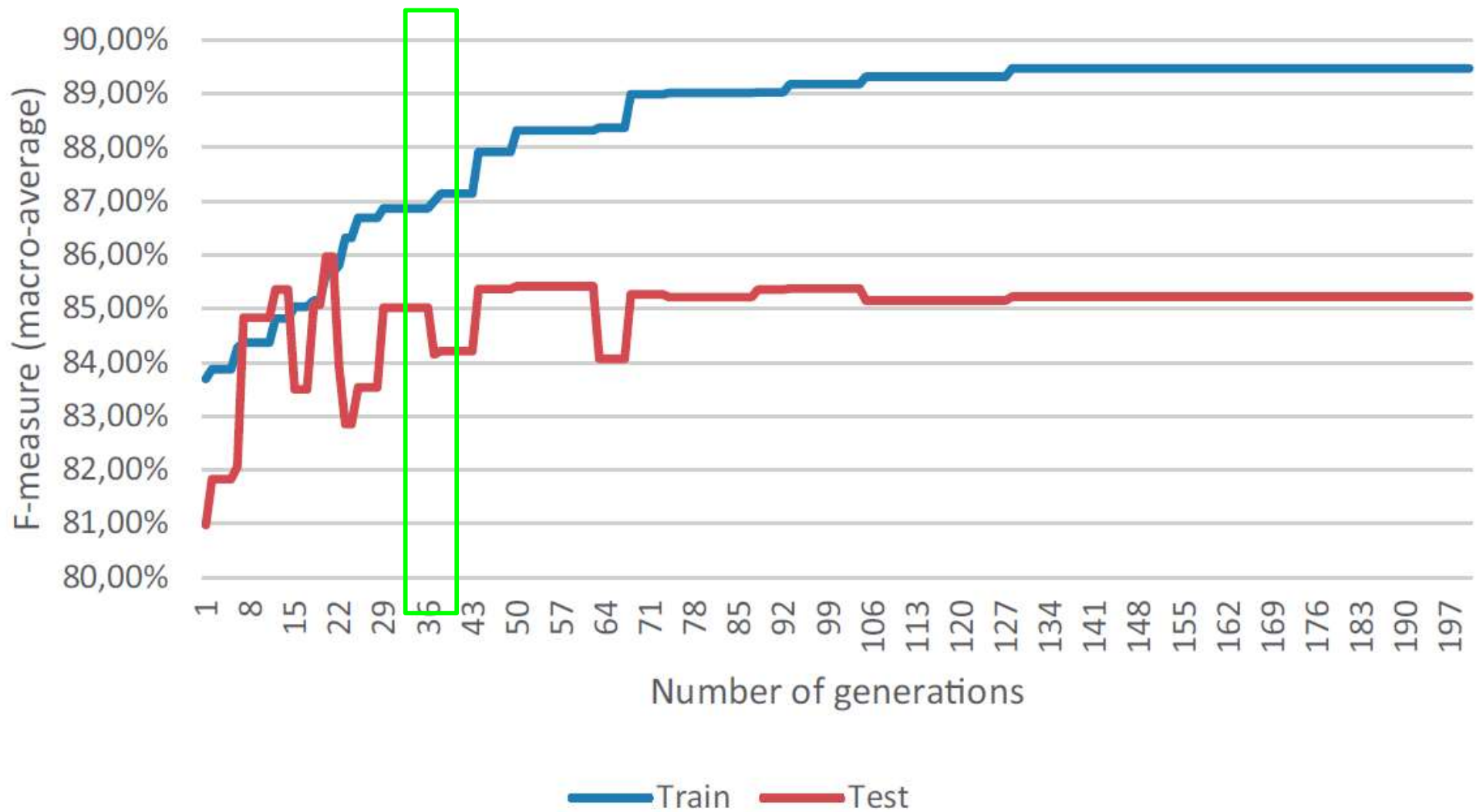
# Experimental results - UCI



- Generalization of learned functions

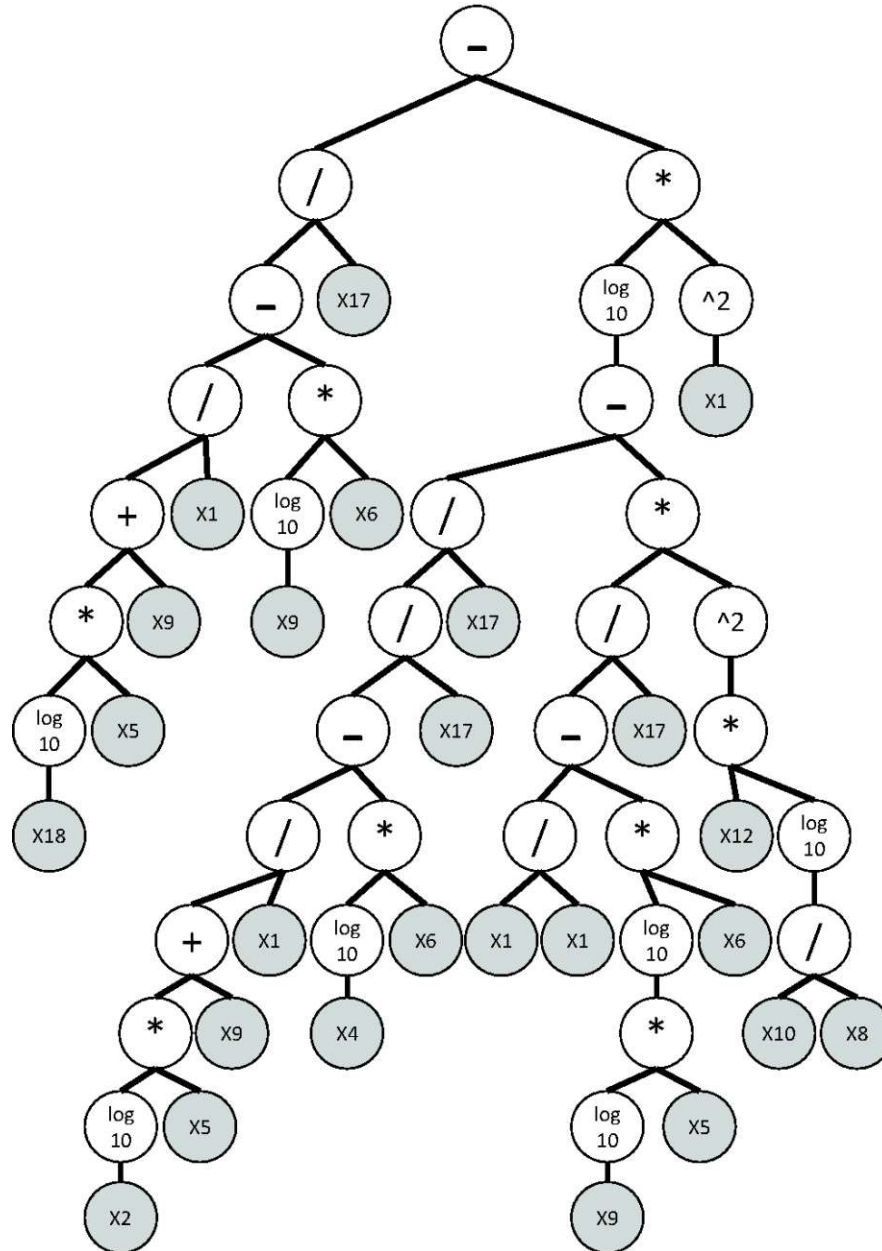
ID	Measure	Accuracy	f-measure
1	Perf. Best classifier	59.70	62.12
2	Perf. when using the ad-hoc weight	87.35	86.87
3	Avg. performance overall data sets	48.81	43.51
4	Maximum performance	97.08	97.47
5	Avg. number of improved data sets	17.22	15.22

# Experimental results: overfitting?



# Experimental results

- Individual example after 200 generations



# Conclusions

- GP to build heterogeneous ensembles has shown to be an effective way to improve their performance
- Both performance metrics were improved when ensembles use all considered classifiers
- Varying some configuration GP parameters allows to modify the overall ensemble performance
  - Population size
  - Number of generations

Representation learning

Automatic generation of classification prototypes

Ensemble generation

Term-weighting scheme learning

# SOME APPLICATIONS OF GP ON MACHINE LEARNING PROBLEMS

H. J. Escalante, M. García-Limón, A. Morales, M. Graff, M. Montes-y-Gómez, E. Morales. **Learning term-weighting schemes for text classification.** *Submitted, October 6, 2014*

M. García-Limón, H. J. Escalante, M. Montes-y-Gómez, A. Morales, E. Morales. **Genetic programming of text representations.** *GECCO Comp'14, pp. 1459-1460, (Late-breaking abstract, Oral presentation), Vancouver, Canada, July, 12-17, 2014.*

**11<sup>o</sup> TALLER DE  
TECNOLOGÍAS  
DEL LENGUAJE HUMANO**  
Octubre 16-17 Tonantzintla, Puebla

**ORGANIZACIÓN Y ESTRUCTURACIÓN DE LA  
RED TEMÁTICA EN  
TECNOLOGÍAS DEL LENGUAJE**  
*REUNIÓN GENERAL*

# Aprendizaje de Esquemas de Pesado para la Clasificación de Textos

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Instituto Nacional de Astrofísica, Óptica y  
Electrónica



Hugo Jair Escalante, Mauricio García-Limón, Alicia Morales, Mario Graff, Manuel Montes-y-Gómez, Eduardo Morales. Learning term-weighting schemes for text classification. *Submitted, October 6, 2014*

# Información textual

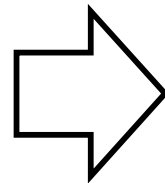
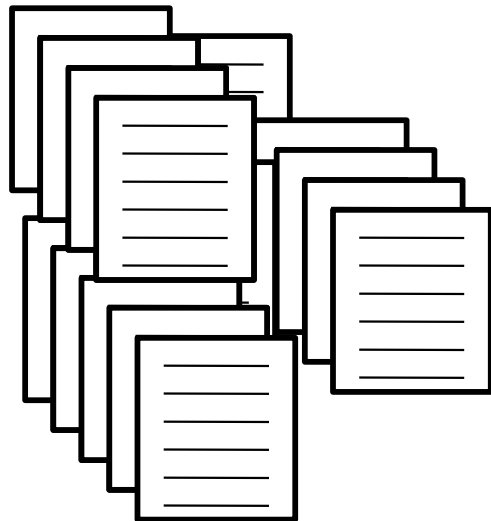
- Crecimiento considerable de información textual disponible electrónicamente
- Incapacidad de los seres humanos para procesar tanta información en tiempos razonables
- Minería de textos: “el proceso de derivar información de alta calidad a partir del texto”



<http://www.qmee.com>

# Clasificación de textos (TC)

- La asignación de categorías predefinidas a documentos de texto.
- **Categorías:** dependen del objeto de interés que se quiera modelar, e.g., contenido/temática, estilo de escritura, polaridad, etc.



Documents (e.g., news articles)

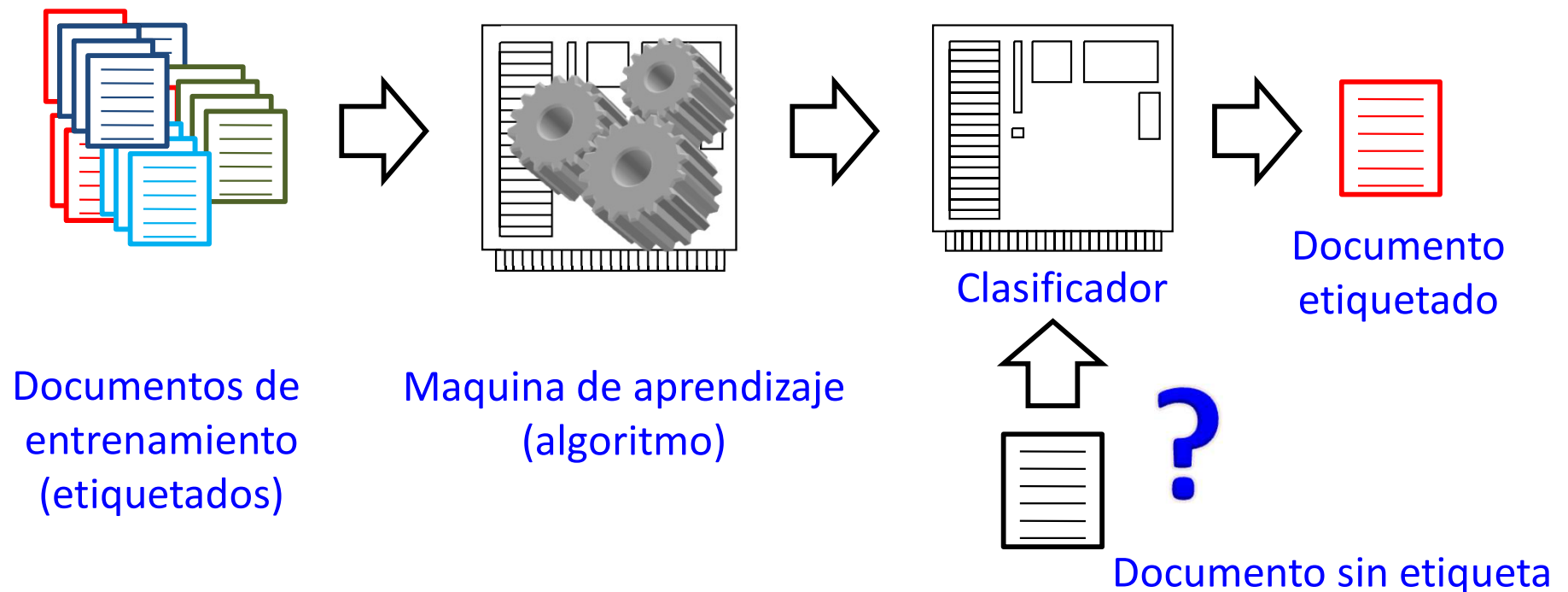
Categories/classes  
(e.g., sports, religion, economy)

# Clasificación de textos

- Muy probablemente, TC es el tópico más estudiado dentro de las tecnologías del lenguaje humano:
  - Se puede considerar un problema resuelto en ciertos escenarios: e.g., clasificación de noticias y filtrado de spam
- Sin embargo, muchas variantes son problemas abiertos; igualmente, tareas actuales pueden verse como TC y están lejos de ser resueltas:
  - Cross-domain, multilingüe, ...
  - Perfilado de autores, atribución de autoría, minería de opiniones, detección de sarcasmo, ...

# Clasificación de textos

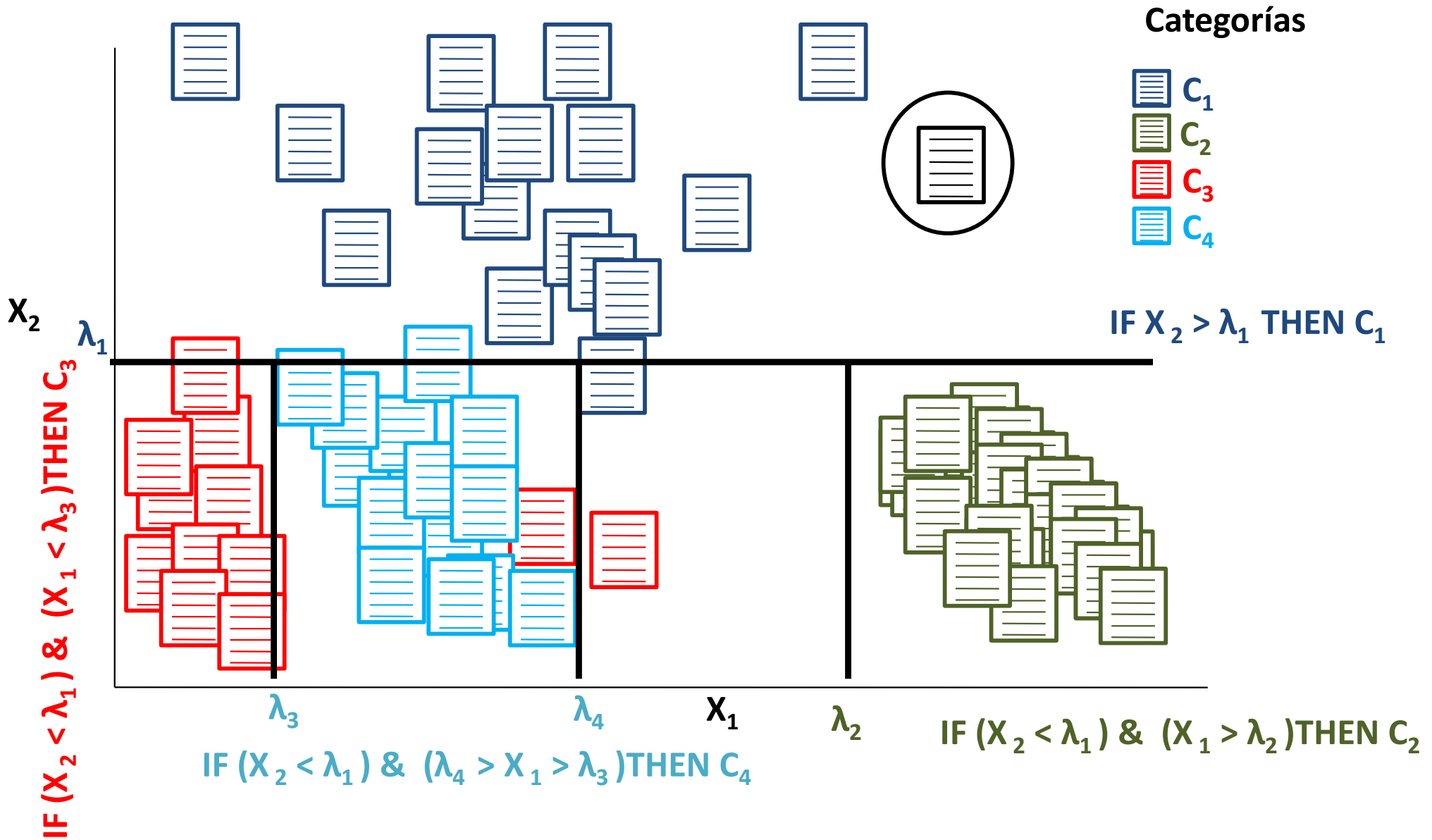
- Si bien la clasificación de textos es un proceso que requiere de procesamiento de alto nivel semántico y herramientas lingüísticas, el enfoque estadístico ha probado ser muy competitivo en muchos escenarios:



# Clasificación de textos

- Se asume que los documentos pueden ser representados como puntos en un espacio (VSM)
- Se usan modelos de aprendizaje computacional para hacer inferencia sobre nuevos documentos

# Clasificación de textos



# Representación de documentos (VSM)

Términos en el vocabulario  
(Unidades básicas, expresando el *contenido del documento*)

Documentos en el corpus  
(un vector/fila por documento)

	$t_1$	$t_1$	...	$t_{ V }$
$d_1$				
$d_2$				
:		$w_{i,j}$		
$d_m$				

**V:** vocabulario del corpus (*i.e.*,  
todos los términos diferentes que  
ocurren en el corpus)

Peso indicando la contribución del  
Término  $j$  en el documento  $i$ .

¿Qué términos son *buenos* atributos?

¿Cómo extraerlos/identificarlos?

¿Cómo estimar el peso?



# Representación de documentos

- **Esquemas no Supervisados:** Son los esquemas tradicionales, propuestos para recuperación de información, e.g., *tf*, *tf-idf*, *Booleano*, etc.
- **Esquemas Supervisados:** Son esquemas que incorporan información discriminativa, diseñados particularmente para clasificación, e.g., *tf-ig*, *tf-chi<sup>2</sup>*, etc.

Acronym	Name	Formula	Description	Ref.
<i>B</i>	Boolean	$x_{i,j} = \mathbf{1}_{\{\#(t_i, d_j) > 0\}}$	Indicates the prescense/abscense of terms	[2]
<i>TF</i>	Term-Frequency	$x_{i,j} = \#(t_i, d_j)$	Accounts for the frequency of occurrence of terms	[2]
<i>TF-IDF</i>	TF - Inverse Document Frequency	$x_{i,j} = \#(t_i, d_j) \times \log\left(\frac{N}{df(t_j)}\right)$	An TF scheme that penalizes the frequency of terms across the collection	[2]
<i>TF-IG</i>	TF - Information Gain	$x_{i,j} = \#(t_i, d_j) \times IG(t_j)$	TF scheme that weights term occurrence by its information gain across the corpus.	[11]
<i>TF-CHI</i>	TF - Chi-square	$x_{i,j} = \#(t_i, d_j) \times CHI(t_j)$	TF scheme that weights term occurrence by its $\chi^2$ statistic	[11]
<i>TF-RF</i>	TF - Relevance Frequency	$x_{i,j} = \#(t_i, d_j) \times \log\left(2 + \frac{TP}{\max(1, TN)}\right)$	TF scheme that weights term occurrence by its $\chi^2$ statistic	[10]

# Aprendizaje de Esquemas de Pesado

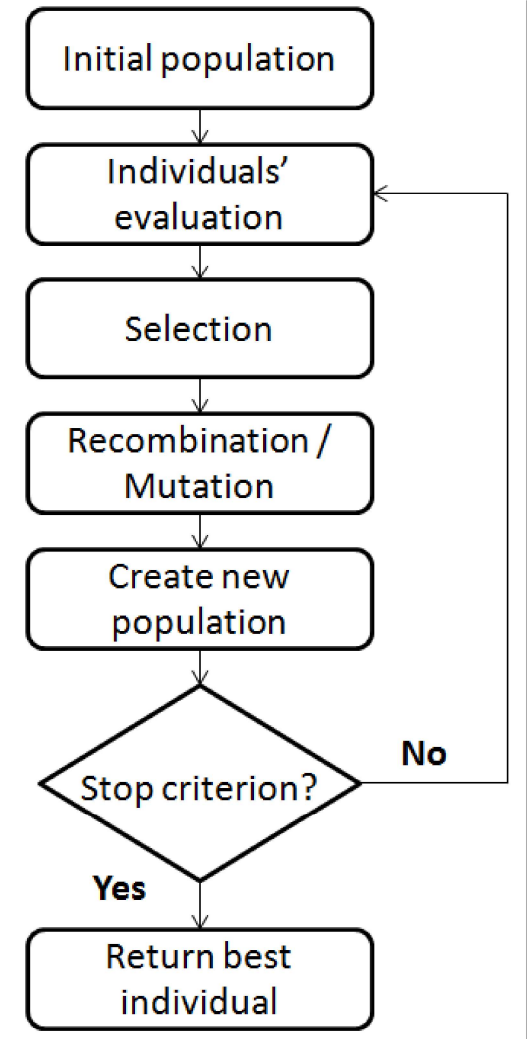
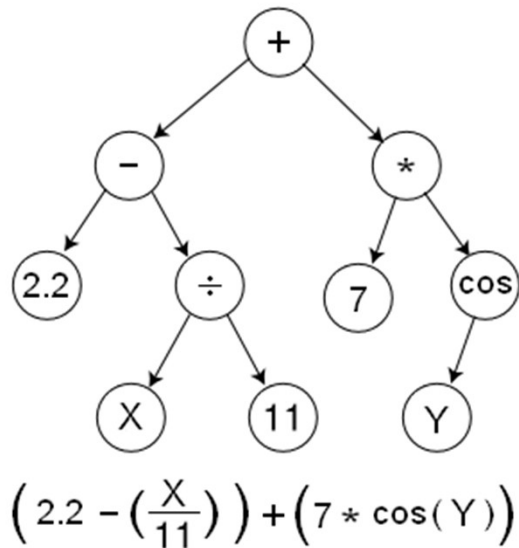
- Problemática:
  - Esquemas de pesado se han propuesto manualmente,
  - Casi siempre se usan esquemas no-supervisados,
  - Se usa un mismo esquema de pesado para casi todas las tareas.
- ¿Es posible generar de forma automática esquemas de pesado para TC, con los que se obtengan mejores resultados que con esquemas estándar?

# Aprendizaje de Esquemas de Pesado

- **Idea:** proveer a un método de aprendizaje con primitivas para generar esquemas de pesado y aprender esquemas de pesado ad-hoc para la clasificación de textos
- **Implementación usando programación genética (PG):** Codificar esquemas de pesado como arboles y usar PG para encontrar el esquema que maximiza la precisión de clasificación en datos de entrenamiento.

# PG- panorama general

- Algoritmo evolutivo donde los individuos pueden ser estructuras de datos complejas (e.g., arboles, grafos, etc.)



# Aprendizaje de esquemas de pesado con PG

Variable	Meaning
W <sub>1</sub>	$N$ , Constant matrix, the total number of training documents.
W <sub>2</sub>	$\ V\ $ , Constant matrix, the number of terms.
W <sub>3</sub>	$CHI$ , Matrix containing in each row the vector of $\chi^2$ weights for the terms.
W <sub>4</sub>	$IG$ , Matrix containing in each row the vector of information gain weights for the terms.
W <sub>5</sub>	$TF - IDF$ , Matrix with the TF-IDF term weighting scheme.
W <sub>6</sub>	$TF$ , Matrix containing the TF term-weighting scheme.
W <sub>7</sub>	$FGT$ , Matrix containing in each row the global term-frequency for all terms.
W <sub>8</sub>	$TP$ , Matrix containing in each row the vector of true positives for all terms.
W <sub>9</sub>	$FP$ , Matrix containing in each row the vector of false positives.
W <sub>10</sub>	$TN$ , Matrix containing in each row the vector of true negatives.
W <sub>11</sub>	$FN$ , Matrix containing in each row the vector of false negatives.
W <sub>12</sub>	$Accuracy$ , Matrix in which each row contains the accuracy obtained when using the term as classifier.
W <sub>13</sub>	$Accuracy\_Balance$ , Matrix containing the AC_Balance each (term, class).
W <sub>14</sub>	$BNS$ , An array that contains the value for each BNS per (term, class).
W <sub>15</sub>	$DFreq$ , Document frequency matrix containing the value for each (term, class).
W <sub>16</sub>	$FMeasure$ , F-Measure matrix containing the value for each (term, class).
W <sub>17</sub>	$OddsRatio$ , An array containing the OddsRatio term-weighting.
W <sub>18</sub>	$Power$ , Matrix containing the Power value for each (term, class).
W <sub>19</sub>	$ProbabilityRatio$ , Matrix containing the ProbabilityRatio each (term, class).
W <sub>20</sub>	$Max\_Term$ , Matrix containing the vector with the highest repetition for each term.
W <sub>21</sub>	$RF$ , Matrix containing the RF vector.
W <sub>22</sub>	$TF \times RF$ , Matrix containing $TF \times RF$ .

# Aprendizaje de esquemas de pesado con PG

- Función objetivo: maximizar  $f_1$ -measure usando validación cruzada en el conjunto de entrenamiento
  - low-rank linearized SVM (LLSVM)
- Se usa una implementación de PG estándar con parámetros por default

Silva, S., Almeida, J., 2003. **GPLAB-a genetic programming toolbox for matlab**. Proceedings of the Nordic MATLAB conference. pp. 273–278.

Zhang, K., Lan, L., Wang, Z., Moerchen, F., **Scaling up kernel SVM on limited resources: A low-rank linearization approach**. Proceedings of the 15th International Conference on Artificial Intelligence and Statistics(AISTATS), 2012.

# Resultados experimentales

- Experimentos con 3 tipos de tareas:
  - Clasificación temática
  - Atribución de autoría
  - Clasificación de imágenes (BVW)
- Se redujo el vocabulario por frecuencia para acelerar el proceso de optimización
- Se realizaron 5-corridas del programa genético por cada conjunto de datos

Text categorization				
Data set	Classes	Terms	Train	Test
Reuters-8	8	23583	5339	2333
Reuters-10	10	25283	6287	2811
20-Newsgroup	20	61188	11269	7505
TDT-2	30	36771	6576	2818
WebKB	4	7770	2458	1709
Classic-4	4	5896	4257	2838
CADE-12	12	193731	26360	14618

Authorship attribution				
Data set	Classes	Terms	Train	Test
CCA	10	15587	500	500
Poetas	5	8970	71	28
Football	3	8620	52	45
Business	6	10550	85	90
Poetry	6	8016	145	55
Travel	4	11581	112	60
Cricket	4	10044	98	60

Image Classification				
Data set	Classes	Terms	Train	Test
Caltech-101	101	12000	1530	1530
Caltech-tiny	5	12000	75	75

# Resultados experimentales

- Clasificación temática:

Data set	PG- Avg.		Best baseline		
	$f_1$	Acc.	$f_1$	Acc.	Baseline
Reuters-8	<b>90.56<sup>+</sup><sub>-1.43</sub></b>	<b>91.35<sup>+</sup><sub>-1.99</sub></b>	86.94	88.63	TF
Reuters-10	<b>88.21<sup>+</sup><sub>-2.69</sub></b>	91.84 <sup>+</sup> <sub>-1.01</sub>	85.24	<b>93.25</b>	TFIDF
20-Newsgroup	<b>66.23<sup>+</sup><sub>-3.84</sub></b>	<b>67.97<sup>+</sup><sub>-4.16</sub></b>	59.21	61.99	TF
TDT-2	<b>96.95<sup>+</sup><sub>-0.41</sub></b>	<b>96.95<sup>+</sup><sub>-0.57</sub></b>	95.20	95.21	TFIDF
WebKB	<b>88.79<sup>+</sup><sub>-1.26</sub></b>	<b>89.12<sup>+</sup><sub>-1.30</sub></b>	87.49	88.62	B
Classic-4	<b>94.75<sup>+</sup><sub>-1.08</sub></b>	<b>95.42<sup>+</sup><sub>-0.67</sub></b>	94.68	94.86	TF
CADE-12	<b>41.03<sup>+</sup><sub>-4.45</sub></b>	<b>53.80<sup>+</sup><sub>-4.0</sub></b>	39.30	41.89	TF

# Resultados experimentales

- Atribución de autoría:

Data set	PG- Avg.		Best baseline		
	$f_1$	Acc.	$f_1$	Acc.	Baseline
CCA-10	<b>70.32<sup>+</sup>2.73</b>	<b>73.72<sup>+</sup>2.14</b>	65.90	73.15	TF-IG
Poetas	<b>72.23<sup>+</sup>1.49</b>	<b>72.63<sup>+</sup>1.34</b>	70.61	71.84	TF-IG
Football	76.37 <sup>+</sup> 9.99	83.76 <sup>+</sup> 4.27	<b>76.45</b>	<b>83.78</b>	TF-CHI
Business	<b>78.08<sup>+</sup>4.87</b>	<b>83.58<sup>+</sup>1.57</b>	73.77	81.49	TF-CHI
Poetry	<b>70.03<sup>+</sup>7.66</b>	74.05 <sup>+</sup> 7.38	59.93	<b>76.71</b>	B
Travel	<b>73.92<sup>+</sup>10.26</b>	<b>78.45<sup>+</sup>6.72</b>	71.75	75.32	TF-CHI
Cricket	88.10 <sup>+</sup> 7.12	<b>92.06<sup>+</sup>3.29</b>	<b>89.81</b>	91.89	TF-CHI

# Resultados experimentales

- Categorización de imágenes:

Data set	PG- Avg.		Best baseline		
	$f_1$	Acc.	$f_1$	Acc.	Baseline
Caltech-101	<b>61.91<sup>+</sup><sub>-1.41</sub></b>	<b>64.02<sup>+</sup><sub>-1.42</sub></b>	58.43	60.28	B
Caltech-tiny	<b>89.70<sup>+</sup><sub>-2.44</sub></b>	<b>91.11<sup>+</sup><sub>-2.36</sub></b>	85.65	86.67	TF

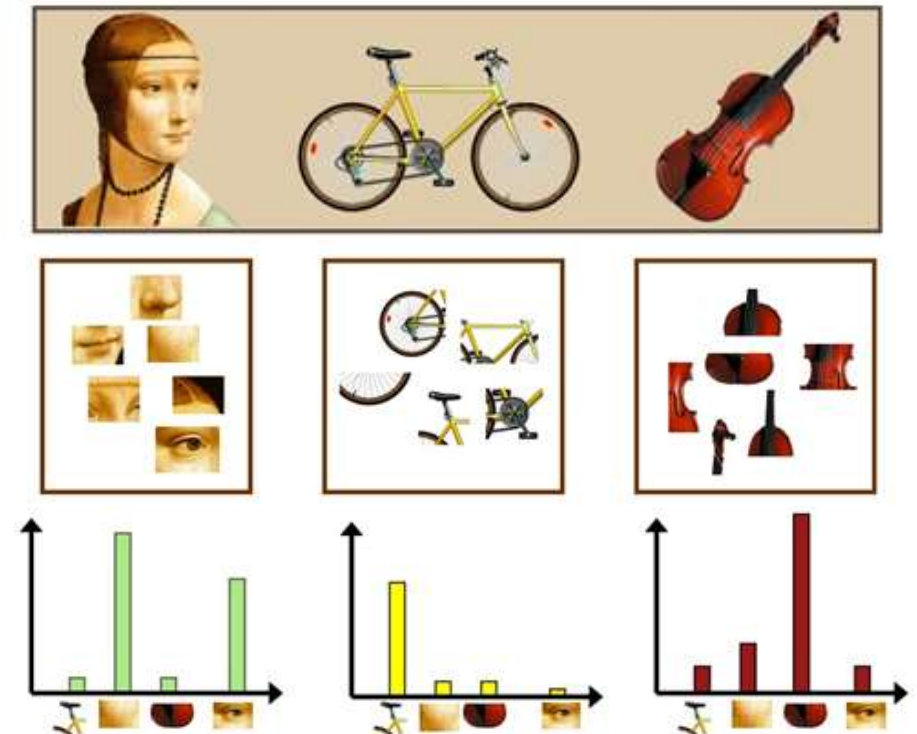
# (Bolsa de palabras visuales)

- Idea: representar a imágenes como histogramas que cuentan la frecuencia con que ocurren descriptores visuales prototípicos (las palabras visuales)

Aprendizaje de vocabulario visual



Representación de imágenes

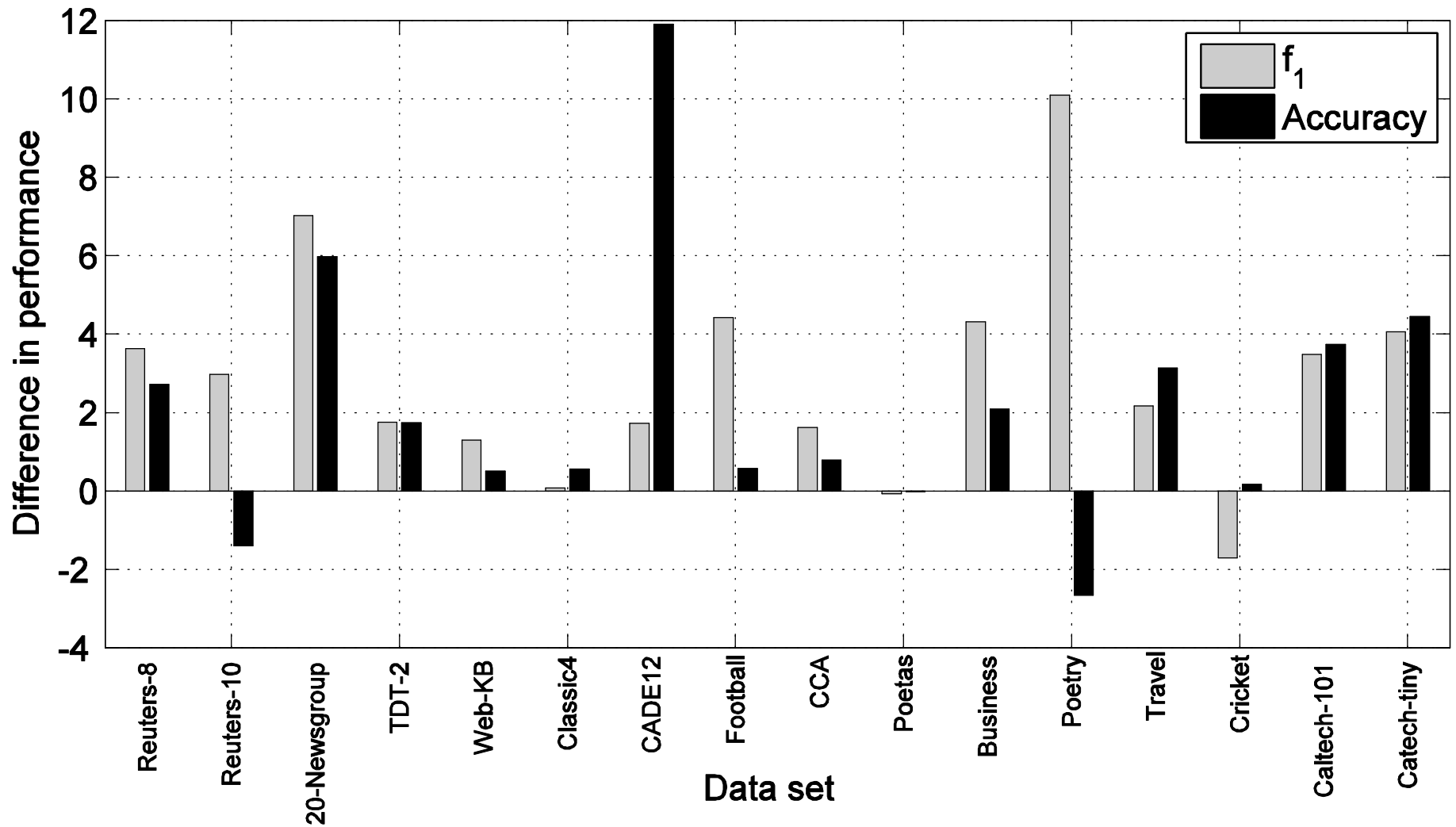


# Resultados experimentales

- Categorización de imágenes:

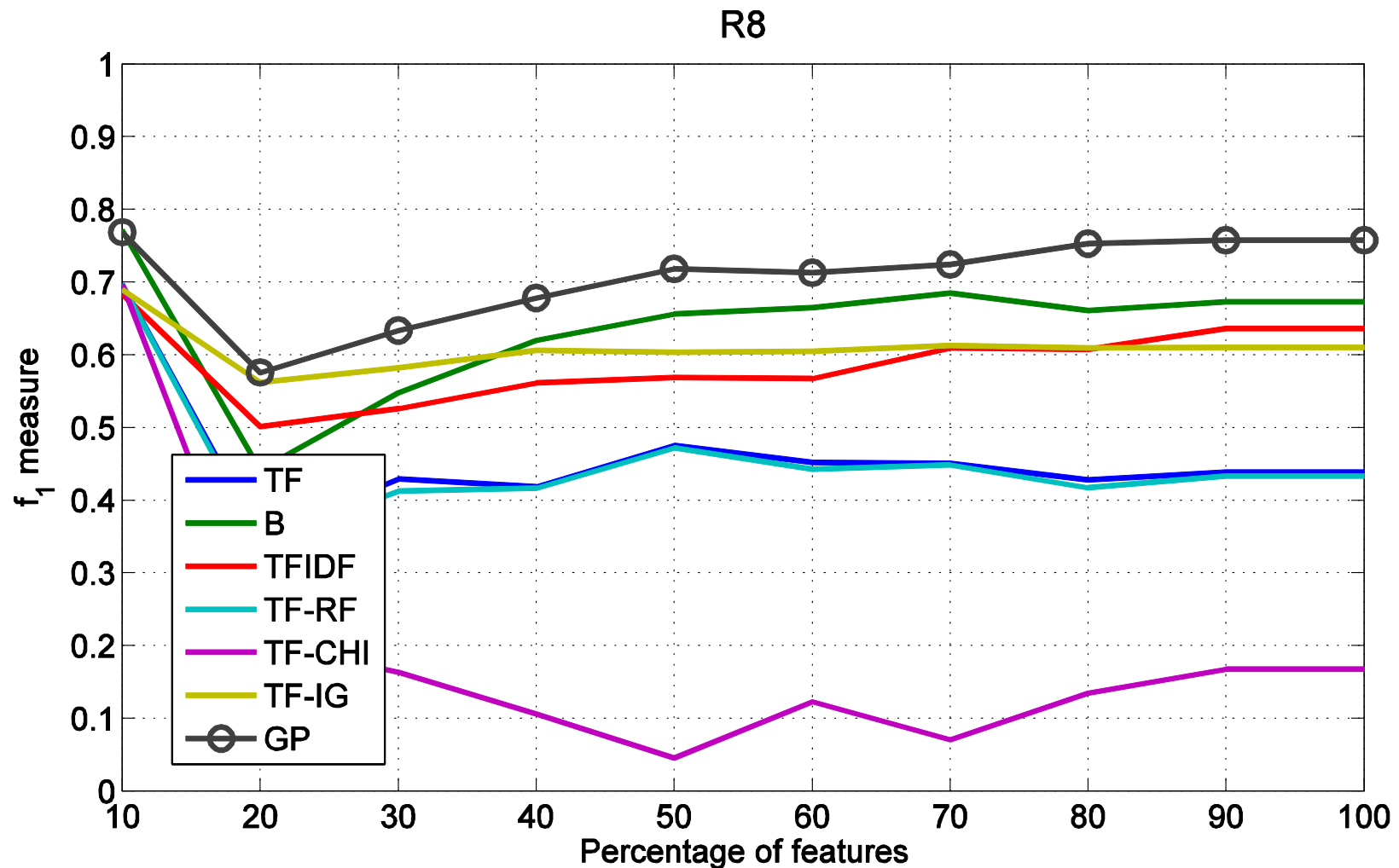
Data set	PG- Avg.		Best baseline		
	$f_1$	Acc.	$f_1$	Acc.	Baseline
Caltech-101	<b>61.91<sup>+</sup><sub>-1.41</sub></b>	<b>64.02<sup>+</sup><sub>-1.42</sub></b>	58.43	60.28	B
Caltech-tiny	<b>89.70<sup>+</sup><sub>-2.44</sub></b>	<b>91.11<sup>+</sup><sub>-2.36</sub></b>	85.65	86.67	TF

# Resultados experimentales



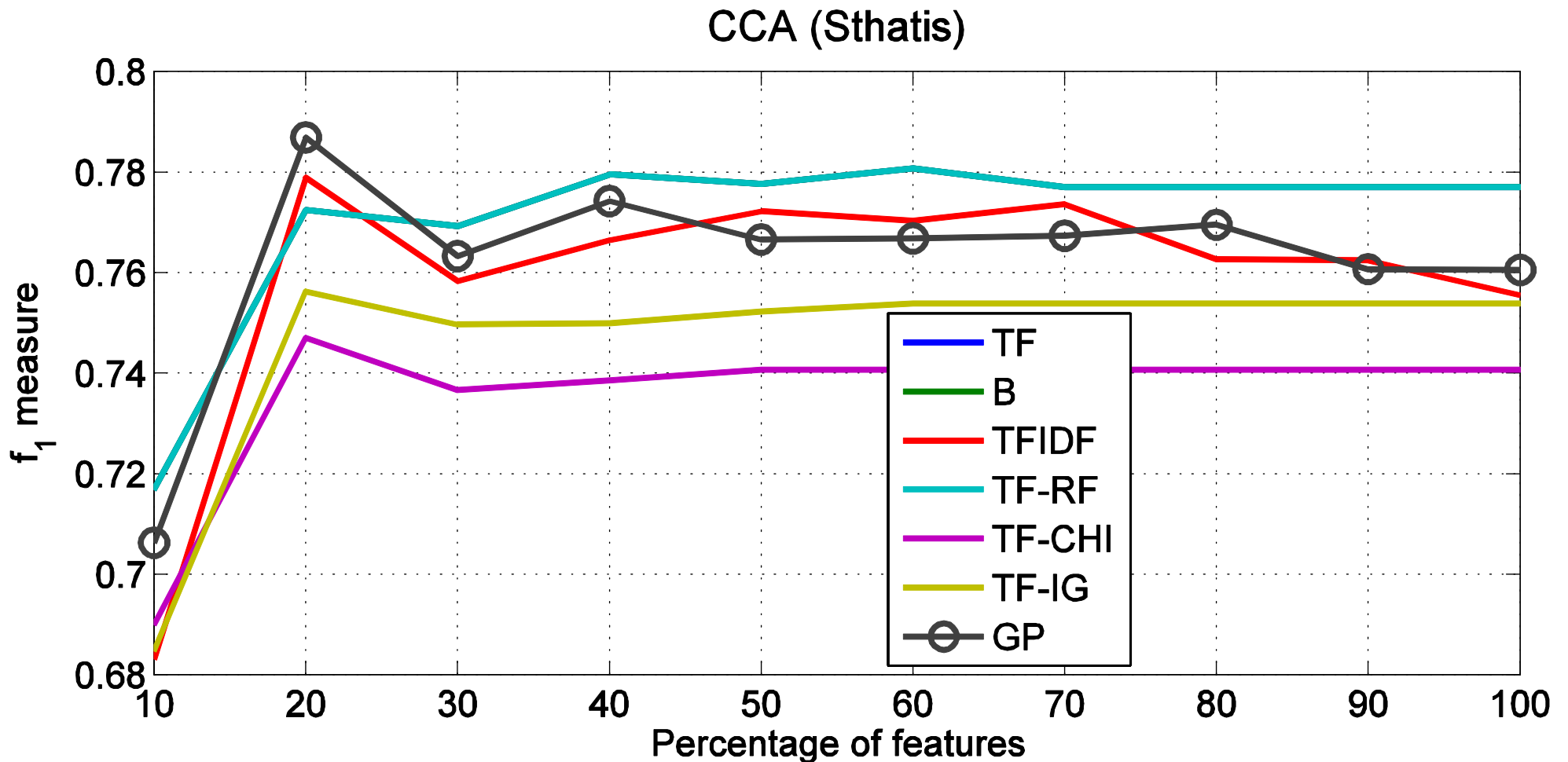
# Resultados experimentales

- Variando la cantidad de términos utilizados



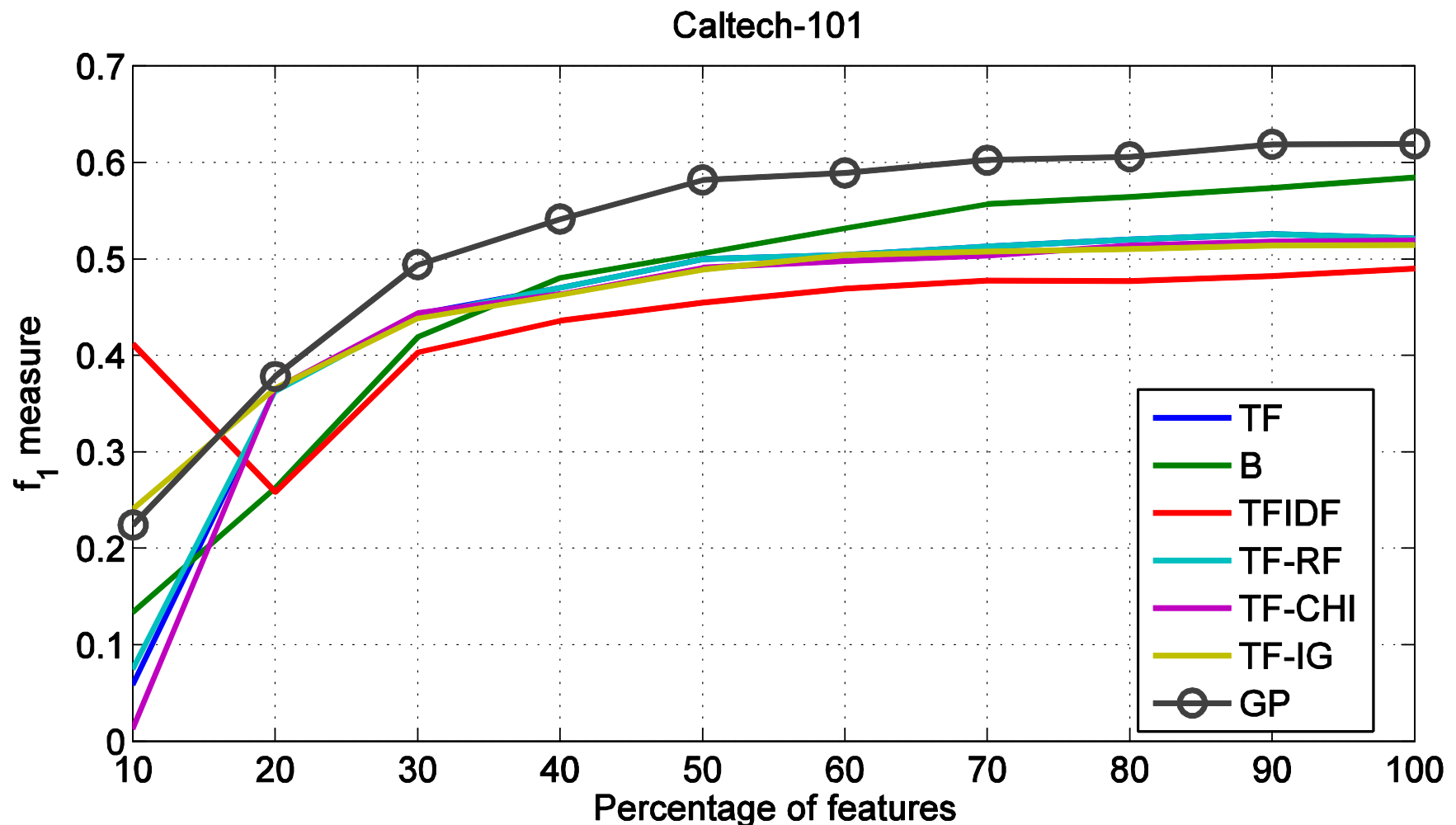
# Resultados experimentales

- Variando la cantidad de términos utilizados



# Resultados experimentales

- Variando la cantidad de términos utilizados



# Resultados experimentales

- ¿Cómo son los pesos aprendidos?

Text categorization			
ID	Data set	Learned TWS	Formula
1	Reuters-8	$-(\text{sqrt}(\text{TFIDF}), \text{div}(\log_2(\text{sqrt}(\text{ProbR})), \text{RF}))$	$\sqrt{\mathbf{W}_5} - \frac{\log \sqrt{\mathbf{W}_{19}}}{\mathbf{W}_{21}}$
2	Reuters-10	$\text{sqrt}(\text{div}(\text{pow}_2(\text{sqrt}(\text{TFIDF})), \text{div}(\text{pow}_2(\text{TF}-\text{RF}), \text{pow}_2(\text{TF}-\text{RF}))))$	$\sqrt{\frac{(\sqrt{\mathbf{W}_5})^2}{\frac{\mathbf{W}_{22}^2}{\mathbf{W}_{22}^2}}}$
3	20-Newsgroup	$\text{sqrt}(\text{sqrt}(\text{div}(\text{TF}, \text{GLOBTF})))$	$\sqrt{\sqrt{\frac{\mathbf{W}_6}{\mathbf{W}_7}}}$
4	TDT-2	$\text{sqrt}(\times(\text{sqrt}(\text{sqrt}(\text{TFIDF})), \text{sqrt}(\times(\text{sqrt}(\text{TFIDF}), \text{IG}))))$	$\sqrt{\sqrt{\sqrt{\mathbf{W}_5}} \times \sqrt{\sqrt{\mathbf{W}_5} \times \mathbf{W}_4}}$
5	WebKB	$\text{div}(\text{TF}-\text{RF}, +(+((\text{RF}, \text{TF}-\text{RF}), \text{FMEAS}), \text{FMEAS}))$	$\frac{\mathbf{W}_{22}}{(((\mathbf{W}_{21} + \mathbf{W}_{22}) + \mathbf{W}_{16}) + \mathbf{W}_{16})}$
6	Classic-4	$\times(\text{ProbR}, \text{TFIDF})$	$\mathbf{W}_5 \times \mathbf{W}_{19}$
7	CADE-12	$\text{div}(\text{TF}, \text{sqrt}(\log_2(\text{ACCU})))$	$\frac{\mathbf{W}_6}{\sqrt{\log \mathbf{W}_{12}}}$

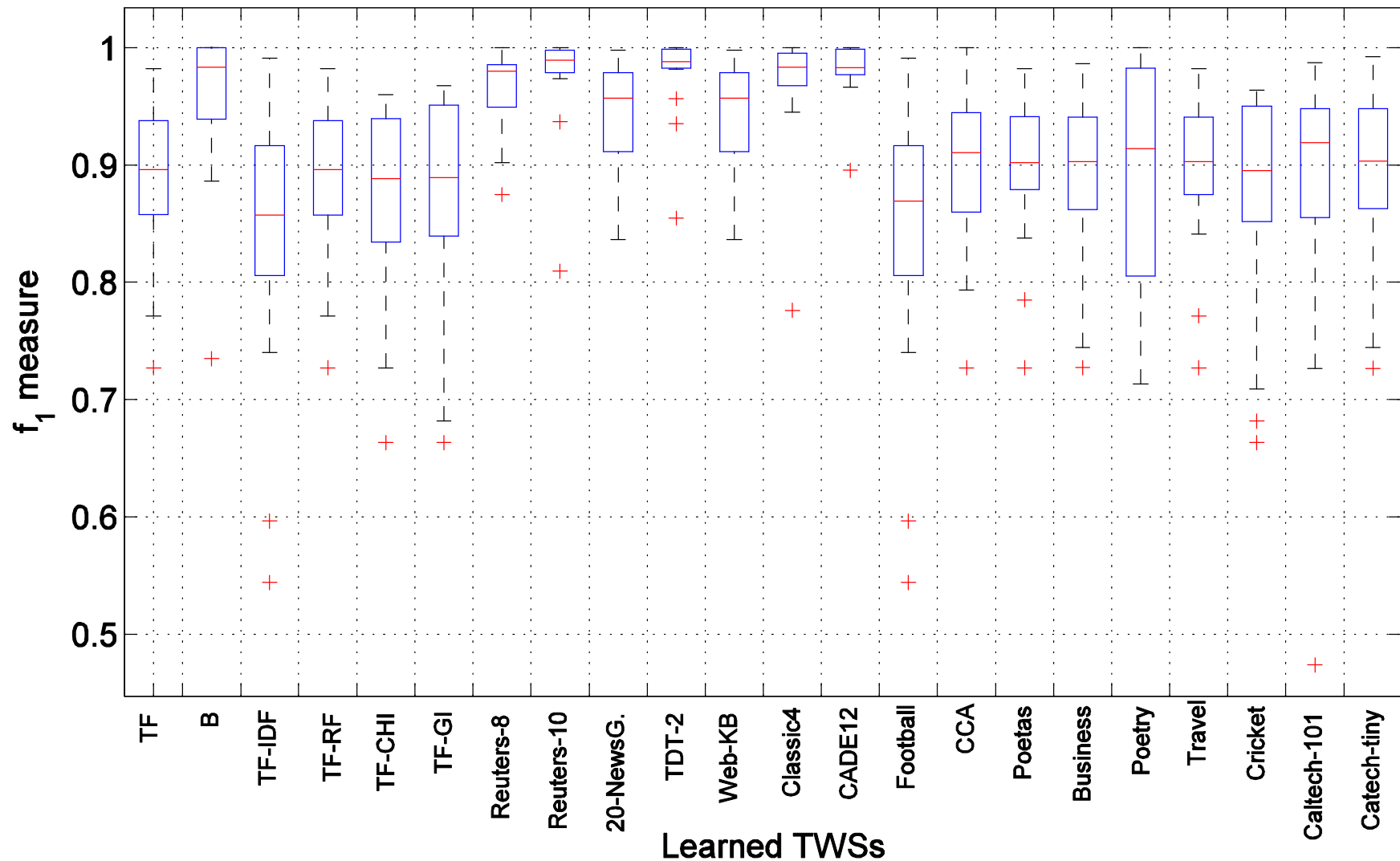
# Resultados experimentales

- ¿Cómo son los pesos aprendidos?

Authorship attribution			
ID	Data set	Learned TWS	Formula
8	CCA	-(IG,plus(TF-RF,TFIDF))	$W_4 - (W_{22} + W_5)$
9	Poetas	-(-(RF,TF-RF),TF-IDF)	$(W_{21} - W_{22}) - W_5$
10	Football	div(TF-RF,pow2(ODDSR))	$\frac{W_{22}}{W_{17}^2}$
11	Business	minus(TF-RF,PROBR)	$W_{22} - W_{19}$
12	Poetry	div(TF,log2(div(TF,log(TF-RF))))	$\frac{W_6}{\log \frac{W_6}{W_{22}}}$
13	Travel	+(-(TF-RF,-(-(TF-RF,-(TF-RF,POWER))),POWER)),TF)	$(W_{22} - ((W_{22} - (W_{22} - W_{18})) - W_{18})) + W_6$
14	Cricket	×(IG,TF-RF)	$W_4 \times W_{22}$
Image Classification			
ID	Data set	Learned TWS	Formula
15	Caltech-101	sqrt(sqrt(-(ODDSR,sqrt(sqrt(TF-RF))))))	$\sqrt{\sqrt{W_{17}} - \sqrt{\sqrt{W_{22}}}}$
16	Caltech-tiny	sqrt(-(TF-RF,ACBAL))	$\sqrt{W_{22} - W_{13}}$

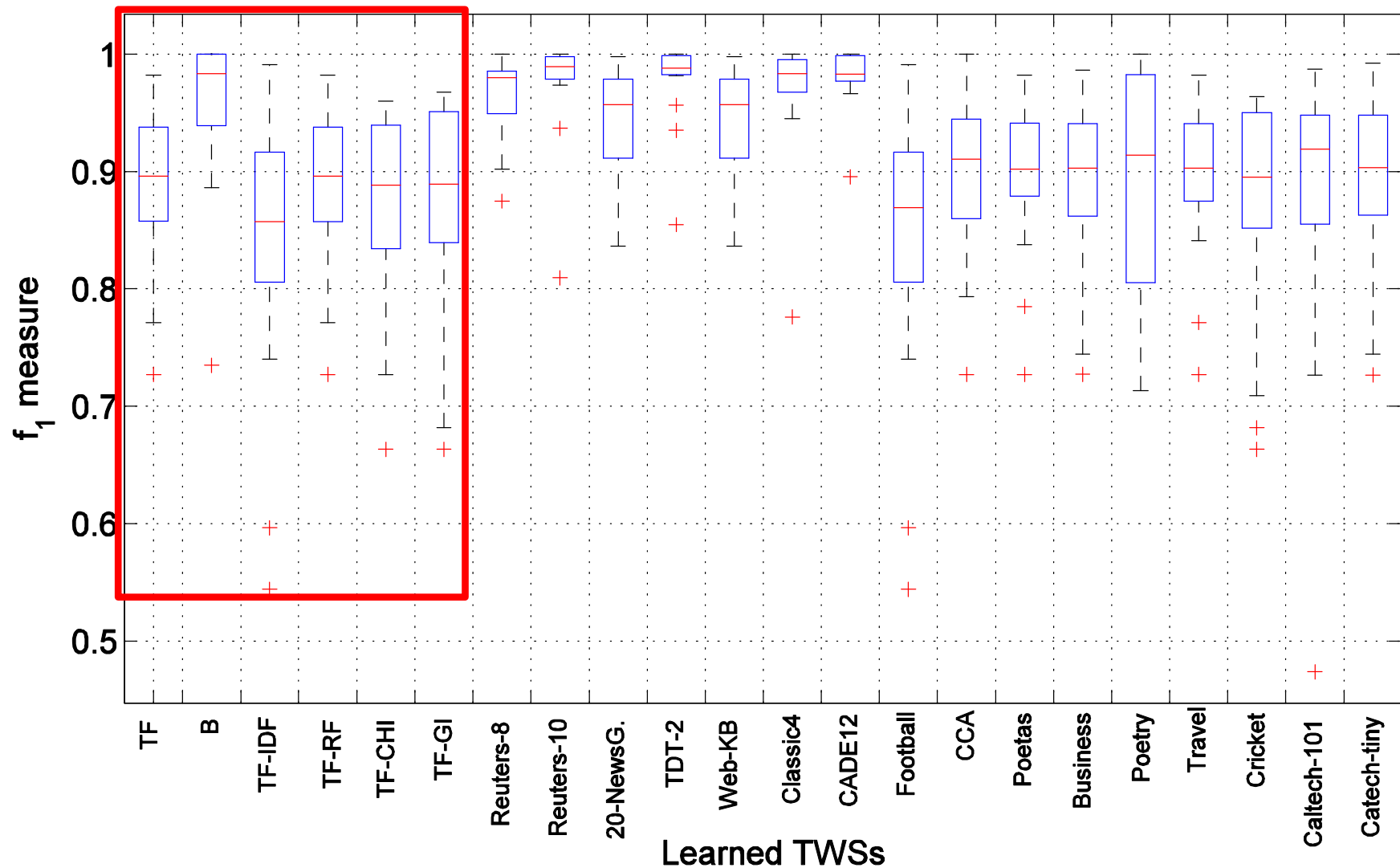
# Resultados experimentales

- Generalidad de los pesos aprendidos I



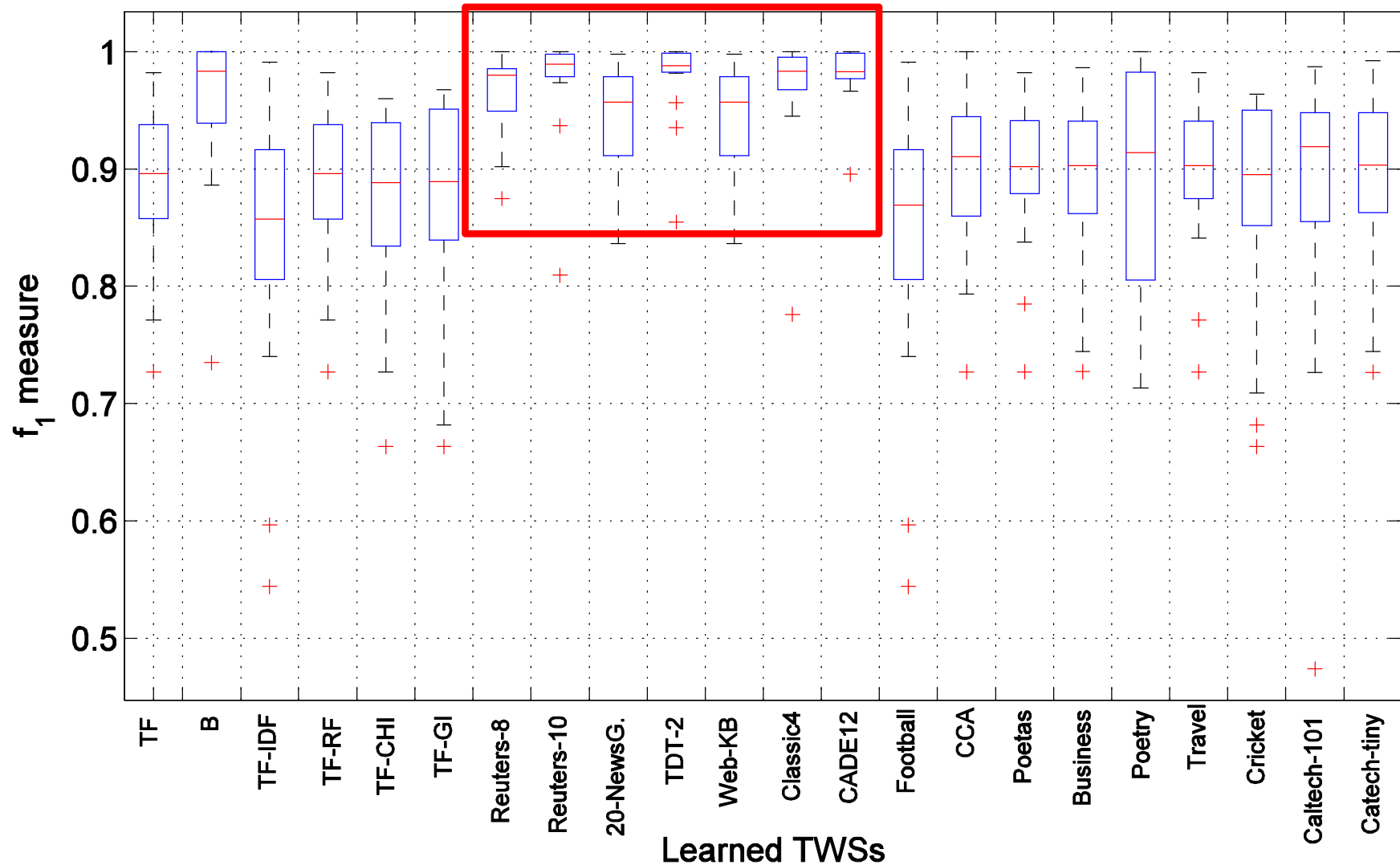
# Resultados experimentales

- Generalidad de los pesos aprendidos I



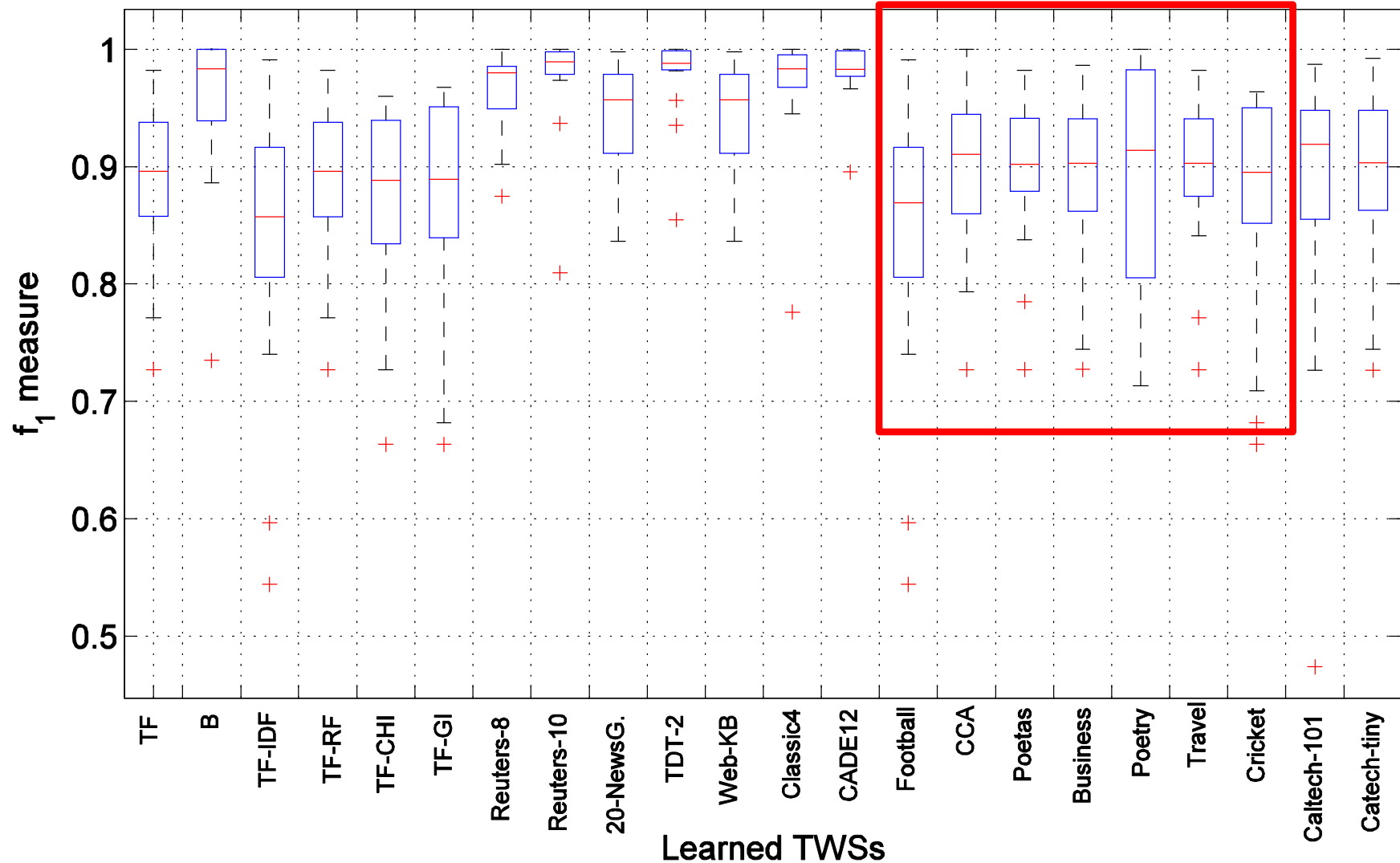
# Resultados experimentales

- Generalidad de los pesos aprendidos I



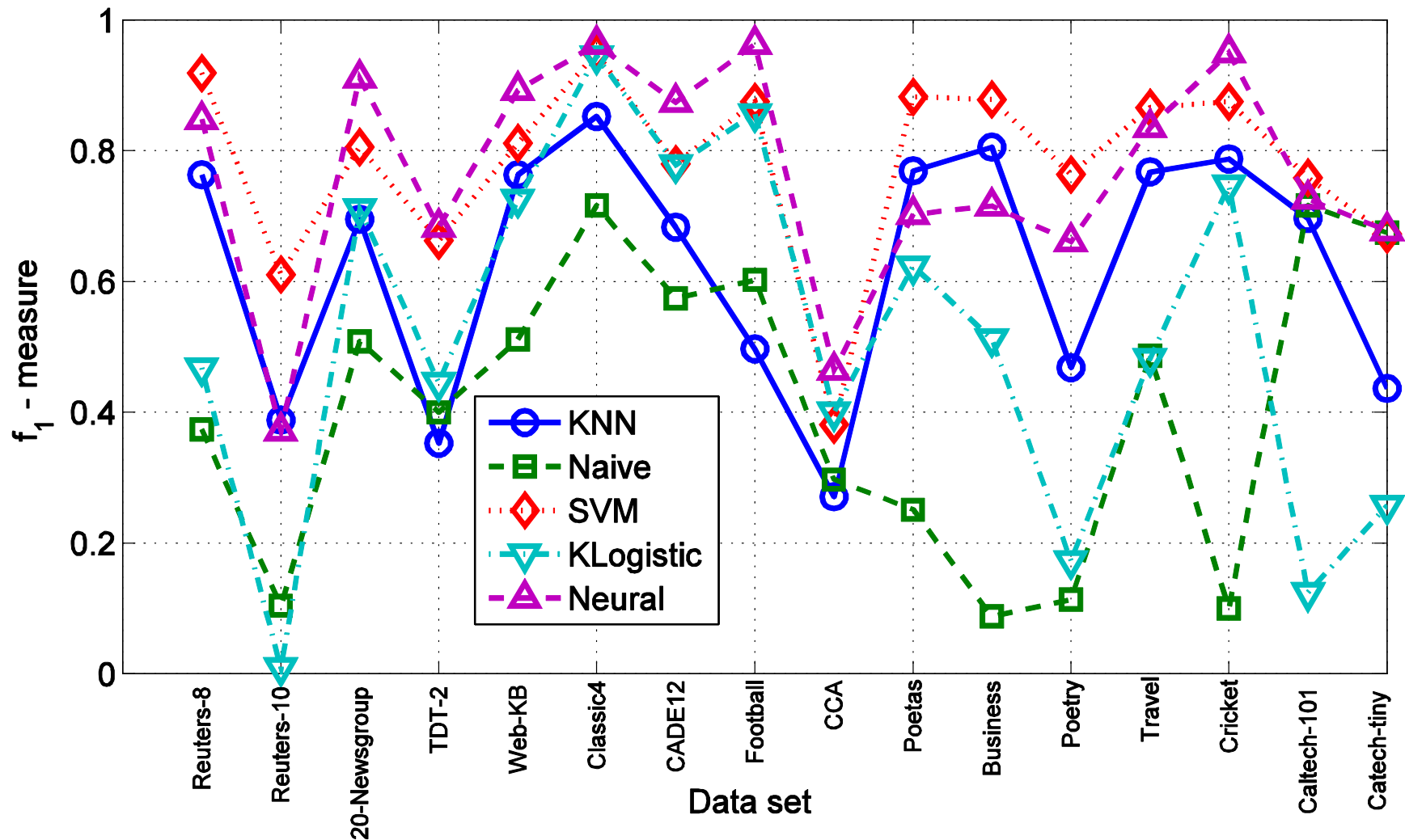
# Resultados experimentales

- Generalidad de los pesos aprendidos I



# Resultados experimentales

- Generalidad de los pesos aprendidos II



# Conclusiones (I): generales

- La definición de esquemas de pesado tiene un impacto importante en tareas de clasificación de imágenes
- En atribución de autoría esquemas de pesado supervisado son más efectivos

# Conclusiones (II): de nuestro método

- Esquemas de pesado aprendidos mejoran el desempeño de esquemas tradicionales y supervisados
- La efectividad de los esquemas de pesado no varía considerablemente, cuando se varía el tamaño del vocabulario (CT)
- En atribución de autoría es mejor idea seleccionar un tamaño de vocabulario apropiado antes de aplicar nuestro método
- Esquemas de pesado aprendidos para una modalidad pueden aplicarse a otra modalidad diferente, sin degradar el rendimiento notablemente (principalmente CT y CI)
- Los esquemas aprendidos son fáciles de analizar

# Trabajo futuro

- El método es sumamente costoso (comp.): acelerar la búsqueda por medio de modelos surrogados
- Estudiar con detalle el impacto que tiene el esquema de pesado en otras tareas de visión computacional o incluso en procesamiento de voz
- Aprendizaje de representaciones con otro tipo de paradigmas

**11<sup>o</sup> TALLER DE  
TECNOLOGÍAS  
DEL LENGUAJE HUMANO**  
Octubre 16-17 Tonantzintla, Puebla

**ORGANIZACIÓN Y ESTRUCTURACIÓN DE LA  
RED TEMÁTICA EN  
TECNOLOGÍAS DEL LENGUAJE**  
*REUNIÓN GENERAL*

# ¿Preguntas?

Hugo Jair Escalante, Mauricio García-Limón, Alicia Morales, Mario Graff, Manuel Montes-y-Gómez, Eduardo Morales. **Learning term-weighting schemes for text classification.** *Knowledge based systems, 2015*

# Conclusions

- GP is a competitive solution for several (open) problems in machine learning and related fields
- Computationally expensive, and no guarantees on finding the *optimum model*, Yet:
  - In these cases it is unknown whether there is an optimum solution
  - It is infeasible to use standard/exact optimization techniques

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- [Simultaneous Generation of Prototypes and Features through Genetic Programming](#). Mauricio García-Limón, Hugo Jair Escalante, Eduardo Morales, Alicia Morales. GECCO '14 Proceedings of the 2014 conference on Genetic and evolutionary computation, pp. 517-524, (Full paper, Oral presentation), Vancouver, Canada, July, 12-17, 2014.
- [Genetic programming of text representations](#). Mauricio García-Limón, Hugo Jair Escalante, Manuel Montes-y-Gómez, Alicia Morales, Eduardo Morales. GECCO Comp'14 Proceedings of the 2014 conference companion on Genetic and evolutionary computation companion, pp. 1459-1460, (Late-breaking abstract, Oral presentation), Vancouver, Canada, July, 12-17, 2014.
- [An Evolutionary Multi-Objective Approach for Prototype Generation](#). Alejandro Rosales, Hugo Jair Escalante, Jesus A. Gonzalez, Carlos A. Coello, Carlos A. Reyes. CEC'14: Proceedings of the IEEE Congress on Evolutionary Computation, pp. 1100–1007, (Full paper, Oral presentation), Beijing, China, July 6-11, 2014.
- [Object Recognition with Naive Bayes-KNN via Prototype Generation](#). Hugo Jair Escalante, Mauricio Sotomayor, Manuel Montes, A. Pastor López-Monroy. In J.F. Martínez Trinidad, J. A. Carrasco-Ochoa, J. A. Olvera-López, J. Salas Rodríguez, C. Y. Suen (Eds.): Pattern Recognition - 6th Mexican Conference, MCPR 2014, Cancun, Mexico, June 25-28, 2014. Proceedings. Springer 2014 Lecture Notes in Computer Science ISBN 978-3-319-07490-0
- [Evolutionary Multi-Objective Approach for Prototype Generation and Feature Selection](#). Alejandro Rosales-Pérez, Jesús A. González, Carlos A. Coello Coello, Carlos A. Reyes García, Hugo Jair Escalante. CIARP 14: Progress in Pattern Recognition, Image Analysis, Computer Vision, and Applications, LNCS, Vol. 8827, pp. 424-431, 2014,
- [Towards Simultaneous Prototype and Feature Generation](#). Mauricio Alfonso García Limón, Hugo Jair Escalante Balderas and Eduardo Morales Manzanares. Proceedings of the XVI IEEE Autumn Meeting of Power, Electronics and Computer Science ROPEC 2014 INTERNACIONAL, pp. 393—398, 2014. ([slides](#))
- [Learning to Assemble Classifiers via Genetic Programming](#). Niusvel Acosta-Mendoza, Alicia Morales-Reyes, Hugo Jair Escalante, Andres Gago-Alonso. International Journal of Pattern Recognition and Artificial Intelligence, Accepted, 2014 (Impact factor: 0.558 -JCR)

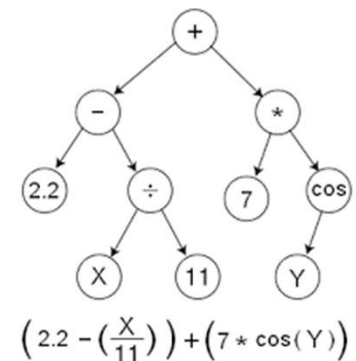
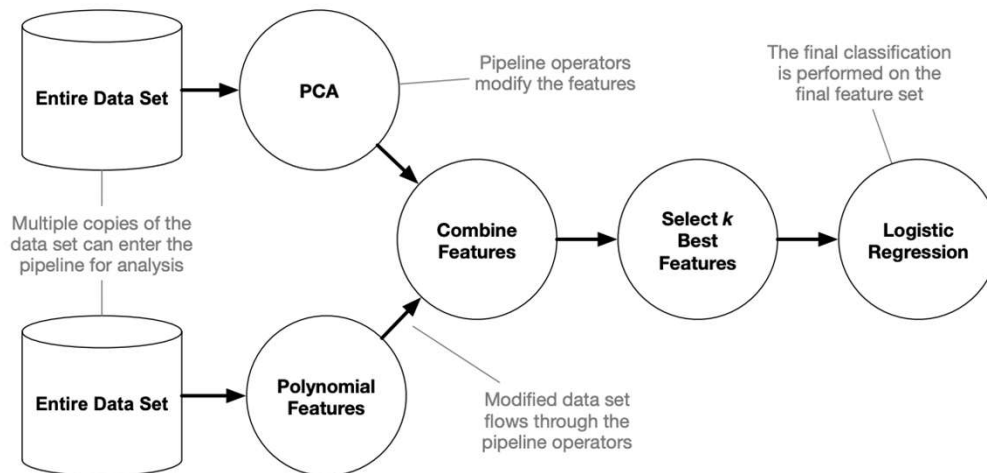
AutoML

NAS

# **APPLICATIONS OF GP 2: OTHER ML APPLICATIONS**

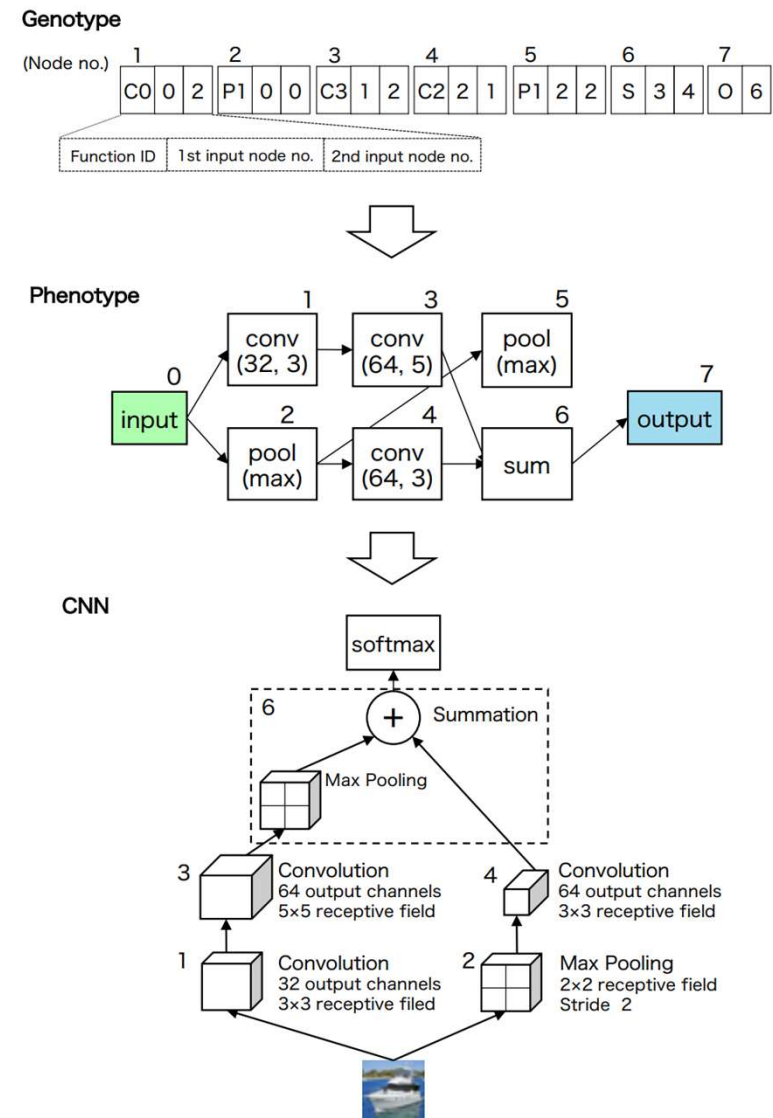
# TPOT: Tree-based Pipeline Optimization Tool

- Uses genetic programming to explore the space of programs (classifiers) that can be built starting from a set of primitives



# Neural architecture search with GP

- A GP that searches for CNNs!
- CNNs are coded as graphs, nodes codify modules (layers) and edges codify connectivity



Human action recognition

Object recognition

Content-based image retrieval

# **APPLICATIONS OF GP 3: COMPUTER VISION**

Human action recognition

Object recognition

Content-based image retrieval

# **APPLICATIONS OF GP 3: COMPUTER VISION**

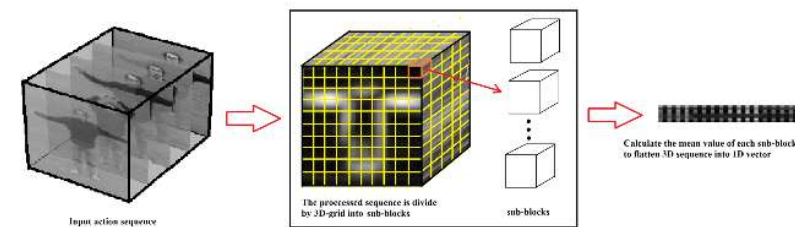
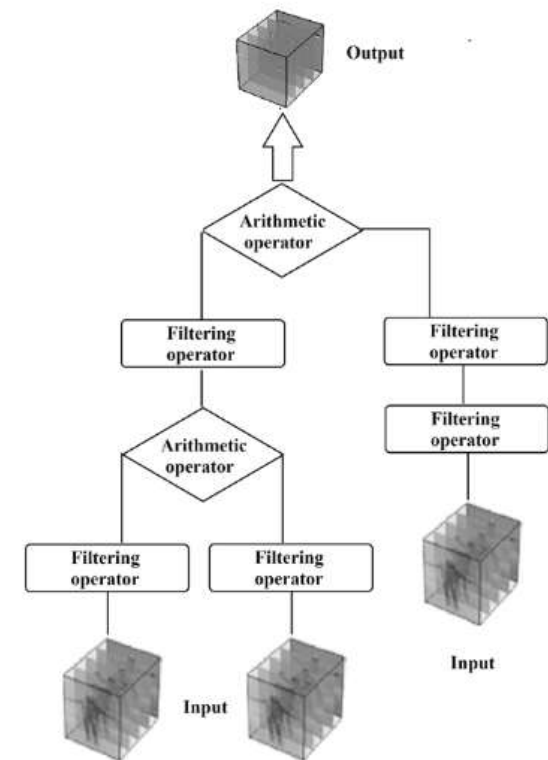
# Human action recognition

- **Problem:** to learn a spatio-temporal descriptor to represent videos for human action recognition
- An STD must (effectively) represent the content of a video
- Traditional STDs are handcrafted by processing the 3D signal



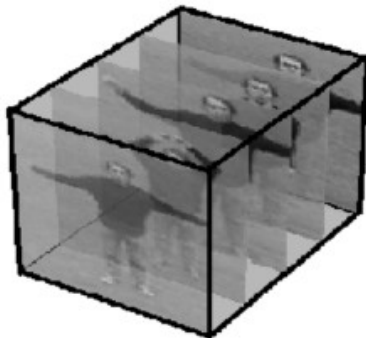
# Human action recognition with GP

- Proposal: to learn a STD from data via GP
  - Standard GP (GPLab)
  - Fitness function: cross-validation SVM error
  - Crossover (90%) & mutation (10%)
- Preprocessing: Normalization of all videos including an action



# Human action recognition with GP

- Terminals: Cubes of dim. 100x100x70



- Function set: filters and arithmetic operators

Operator name	Inputs	Function description	Operator type
GauPy1	1	The first level of a Gaussian pyramid which applies a 3D Gaussian filter with $\sigma = 2$ on input sequences	Filter
GauPy2	1	The second level of a Gaussian pyramid which applies a 3D Gaussian filter with $\sigma = 2$ on sequences obtained from first level of a Gaussian pyramid	Filter
GauPy3	1	The third level of a Gaussian pyramid which applies a 3D Gaussian filter with $\sigma = 2$ on sequences obtained from second level of a Gaussian pyramid	Filter
LapPy1	1	The first level of a Laplacian pyramid which applies a subtraction between GauPy1 and GauPy2	Filter
LapPy2	1	The second level of a Laplacian pyramid which applies a subtraction between GauPy2 and GauPy3	Filter
Wavelet1	1	The first level of a wavelet pyramid which applies a CDF '9/7' wavelet filter on input sequences	Filter
Wavelet2	1	The second level of a wavelet pyramid which applies a CDF '9/7' wavelet filter once again on sequences obtained from first level of wavelet pyramid	Filter
Dof	1	Subtraction between the adjacent frames of input sequences	Filter
absDof	1	Subtraction between the adjacent frames of input sequences and then taking the absolute values of the processed sequences	Filter
Med	1	Apply median filter with filtering window size $5 \times 5$ on the input sequences	Filter
Mean	1	Apply mean filter with filtering window size $5 \times 5$ on the input sequences	Filter
Maxfilter	1	Use 3D maxpooling technique with pooling window size $4 \times 4 \times 4$ on the input sequences	Filter
Add	2	Add the input sequences	Arithmetic
Sub	2	Subtract the input sequences	Arithmetic
Mult	2	Multiply the input sequences	Arithmetic
absSub	2	Absolute subtraction of the input sequences	Arithmetic

# Human action recognition with GP

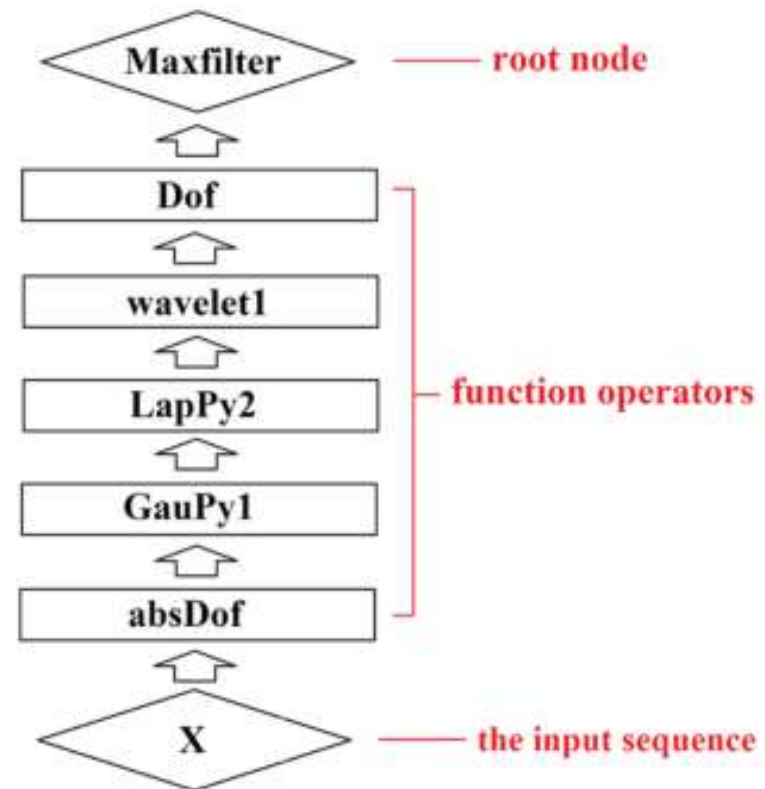
- Results

Table 2: Action recognition accuracies (%) on the mixed KTH-Weizmann dataset, independent KTH and independent Weizmann datasets, respectively, for different methods

Methods \ Database	KTH-Weizmann	KTH	Weizmann
GP-based descriptor	96.9	93.8	100
Niebles <i>et al.</i> [23]	-	83.3	72.8
Jhuang <i>et al.</i> [9]	-	91.7	98.8
Fathi and Mori [5]	-	90.5	100
Ji <i>et al.</i> [10]	-	90.2	-
Schindler and van Gool [26]	-	92.7	-
Liu and Shah [18]	-	94.2	-

Table 3: Comparison of action recognition accuracies (%) on the IXMAS dataset for different methods

Methods \ Actions	Cam 1	Cam 2	Cam 3	Cam 4	Cam 5	Cam 1-5 fusion
GP-based descriptor	86.5	89.3	88.1	84.7	78.3	93.6
Varma and Babu [32]	76.4	74.5	73.6	71.8	60.4	81.3
Liu and Shah [18]	76.7	73.3	72.1	73.1	-	82.8
Wu <i>et al.</i> [35]	81.9	80.1	77.1	77.6	73.4	88.2
Weinland <i>et al.</i> [33]	-	-	-	-	-	93.3



Best descriptor found after weeks of processing

# Human action recognition with GP

- A very effective descriptor was obtained *automatically*
- Results comparable to state of the art (compared to works using handcrafted STDs)
- Time consuming process (is this an issue nowadays?)
- Main drawback: interpretation of operators?, generality?

Human action recognition

Object recognition

Content-based image retrieval

# **APPLICATIONS OF GP 3: COMPUTER VISION**

# Object recognition

- **Problem:** to learn a new visual descriptor to be used for object recognition and related tasks
- Traditional visual descriptors (e.g., SIFT) are handcrafted:
  - Feature extraction of local features
  - Image description of local patches centered around keypoints
  - Image matching/OR using local information



# Object recognition with GP

- Proposal: to learn a visual descriptor from data
  - Standard GP (GPLab)
  - Fitness function: F-measure (on the # of matches)

$$Q = \operatorname{argmax} \left\{ F(P^x, R^x) = \sum_{i=1}^n \frac{2 \cdot (p_i \cdot r_i)}{p_i + r_i} \right\}$$

- Crossover (90%) & mutation (10%)
- 50 iterations, population of 50 individuals (24hrs running an experiment)

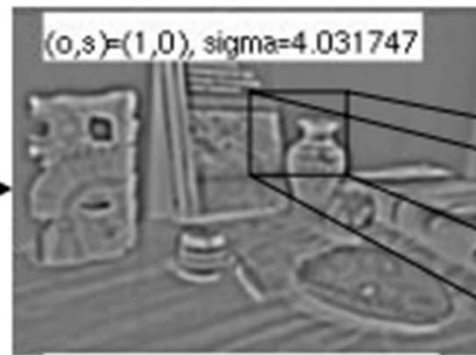
$$\text{FuncSet} = \left\{ +, | + |, -, | - |, *, \div, \sqrt{I_t}, \frac{I_t}{2}, \log_2(I_t), D_x G_\sigma, D_y G_\sigma, G_\sigma \right\}$$

$$\text{TermSet} = \{ I, D_x, D_{xx}, D_{yy}, D_{xy}, D_y \}$$

# Object recognition with GP



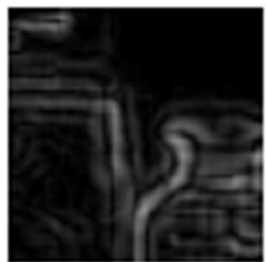
Image



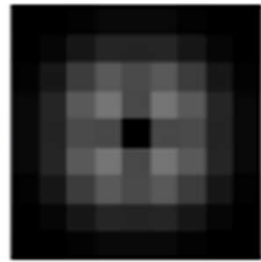
(a) Image from DoG



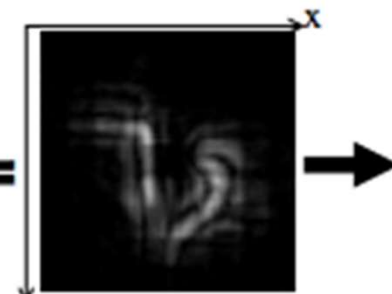
(b) Region



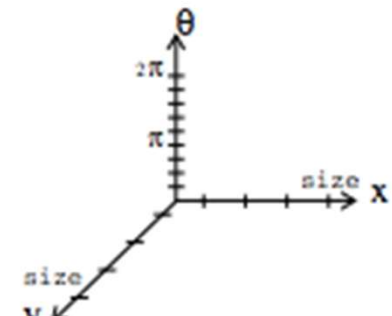
(c) Gradient magnitude



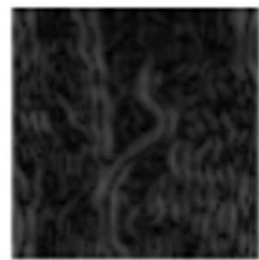
(d) Gaussian weight



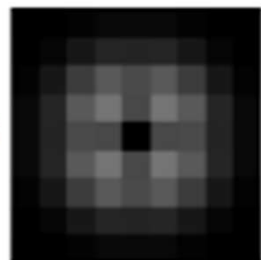
(e) Weighted gradient



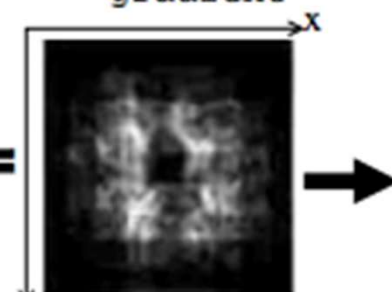
(f) SIFT descriptor



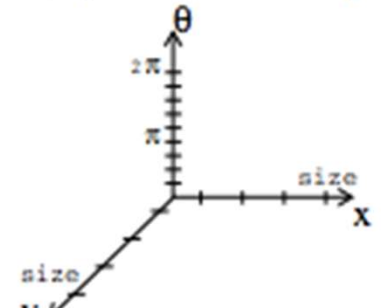
(g) RDGP operator



(h) Gaussian weight



(i) Weighted RDGP operator



(j) RDGP descriptor

# Object recognition with GP

## DATASET



Boat image pair



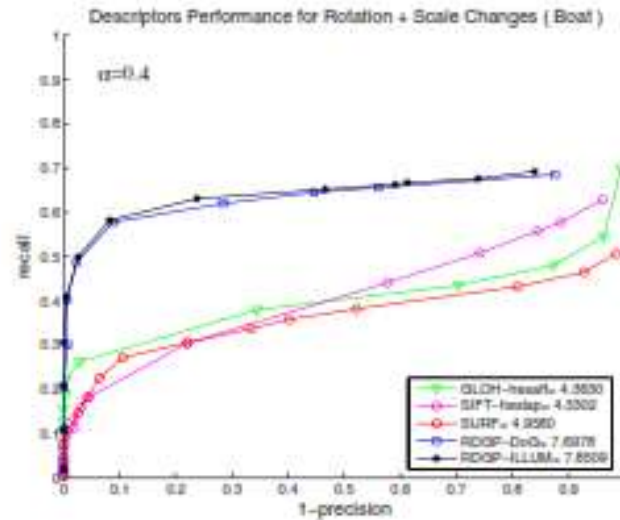
Leuven image pair



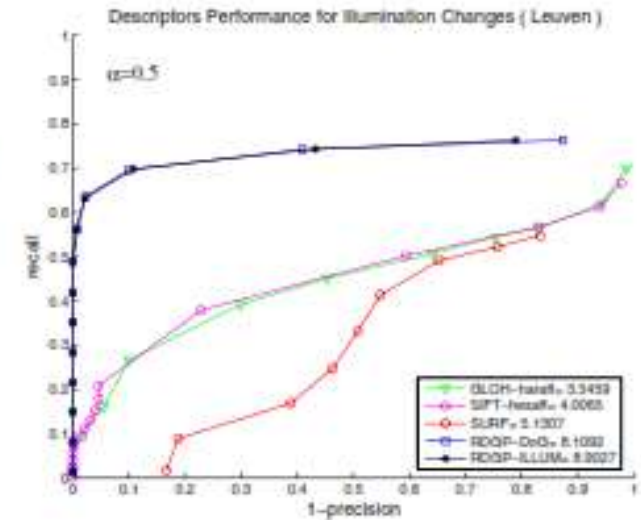
Bikes image pair



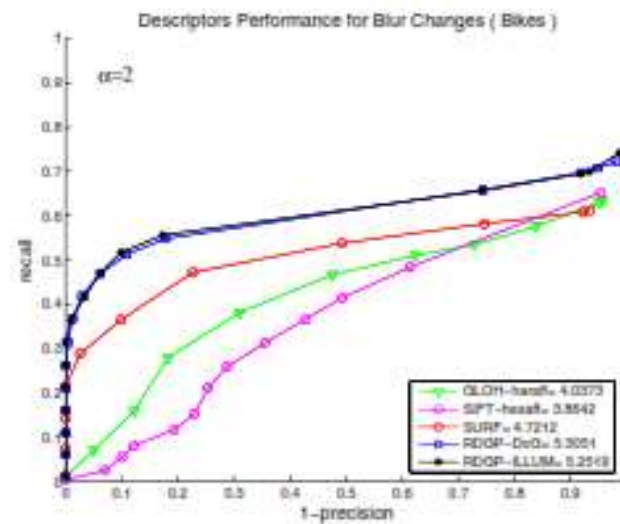
UBC image pair



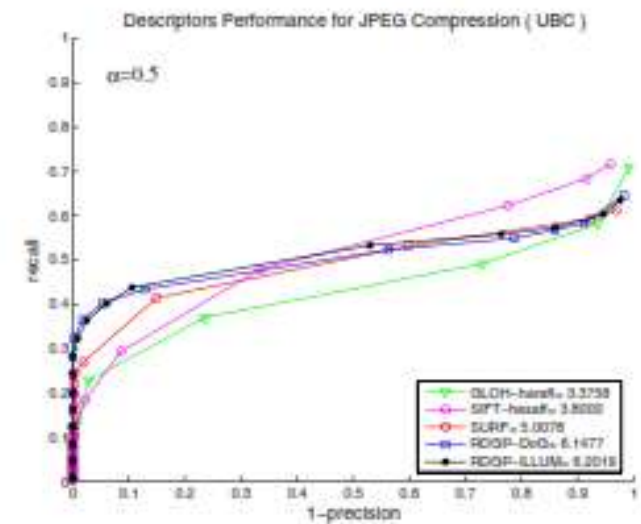
a) Boat image pair



b) Leuven image pair

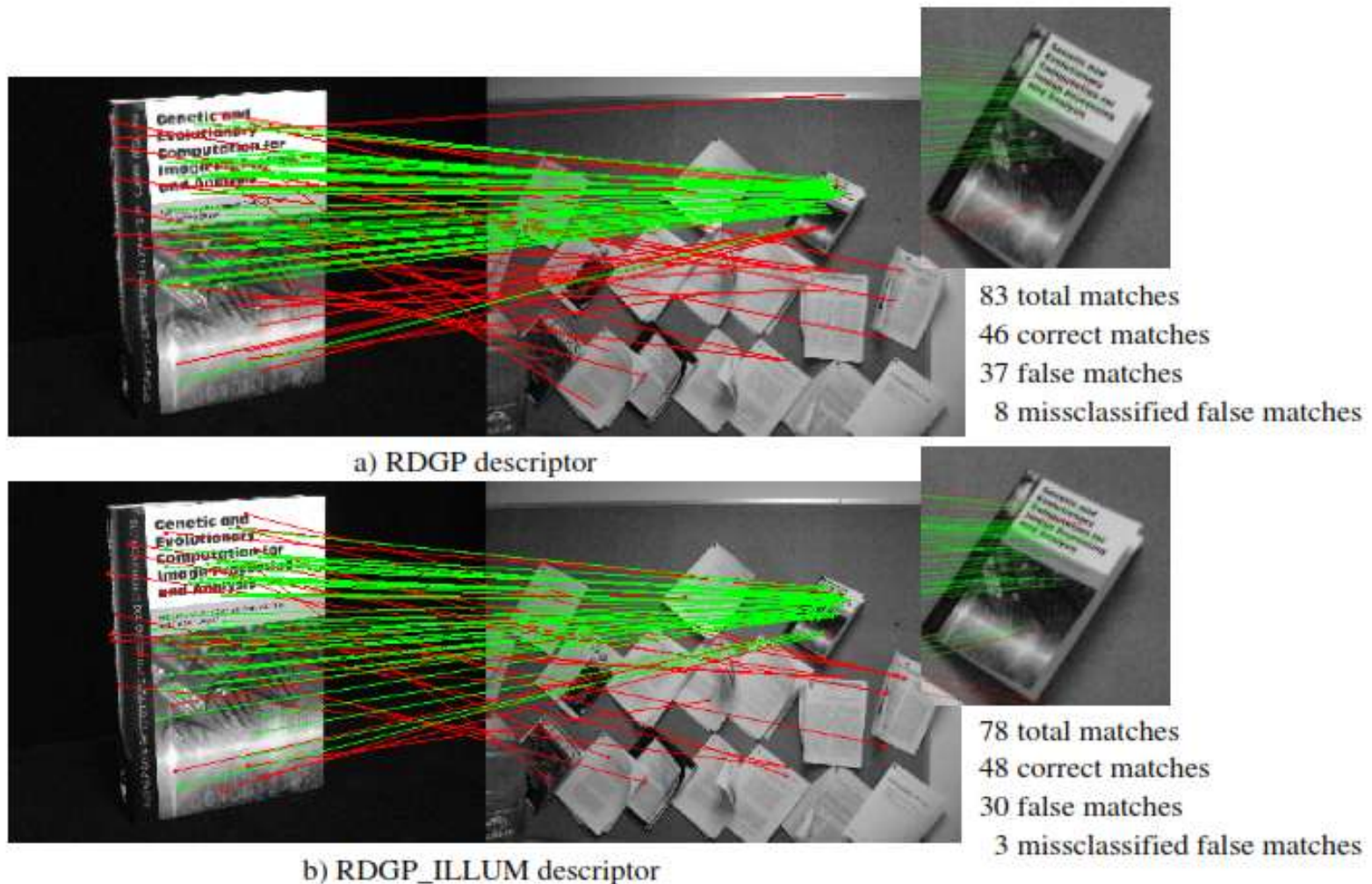


c) Bikes image pair









d) UBC image pair

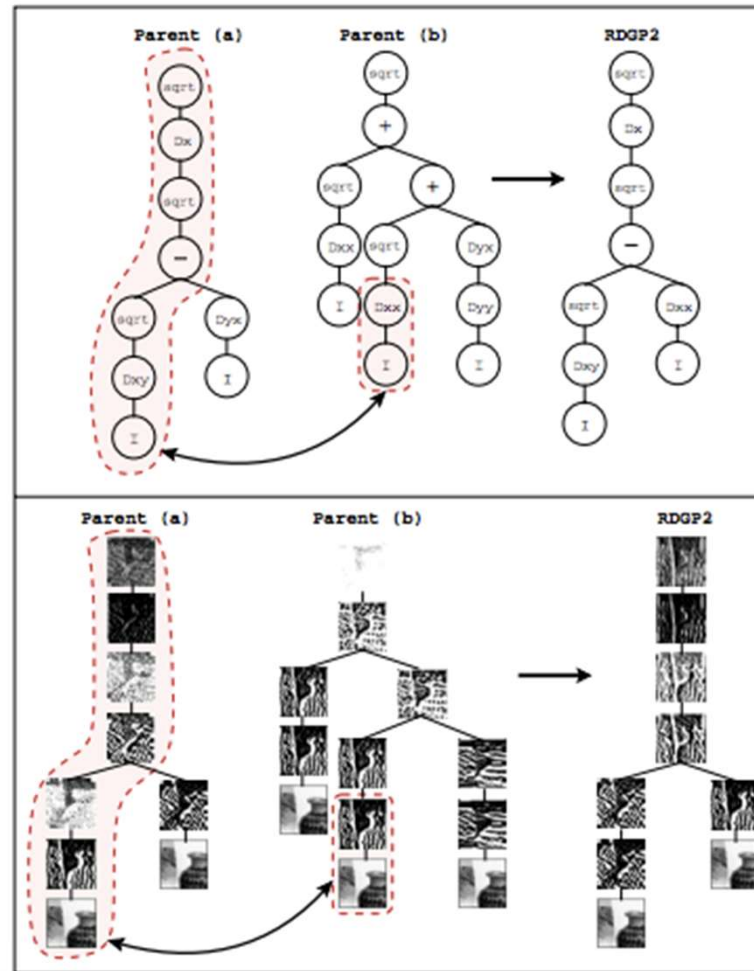
# Object recognition with GP



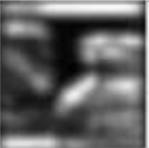




# Object recognition with GP

 Image region without any operation		 Image region after SIFT's weighted gradient		
Descriptor	Fitness	Individual's Expression	Mathematical Expression	Image Region
$RDGP_1$	7.4158	$\text{sqrt}(\text{sqrt}(D_x(\text{sqrt}(D_x(\text{sqrt}(D_{xy}(\text{image})))))))$	$\sqrt{\sqrt{D_x(\sqrt{D_x(\sqrt{D_{xy}(I)})})}}$	
$RDGP_2$	7.4859	$\text{sqrt}(D_x(\text{sqrt}(\text{subtract}(\text{sqrt}(D_{xy}(\text{image})), D_{xx}(\text{image}))))$	$\sqrt{D_x(\sqrt{\sqrt{D_{xy}(I)} - D_{xx}(I)})}$	
$RDGP_4$	7.3928	$\text{Gauss2}(\text{absdif}(\text{Gauss2}(\text{absdif}(\text{absdif}(D_y(\text{image}), D_x(D_x(\text{image}))), D_y(\text{Logarithm}(D_x(D_x(\text{image}))))), \text{Half}(D_x(D_y(\text{image}))))))$	$G_{\sigma=2}   G_{\sigma=2} (  D_y(I) - D_{xx}(I)   - D_y(\log(D_{xx}(I)))  ) - \frac{D_{xx}(I)}{2}  $	
$RDGP_5$	7.4053	$\text{Gauss1}(\text{sqrt}(\text{Gauss2}(\text{sqrt}(\text{sqrt}(\text{subtract}(\text{sqrt}(\text{Gauss1}(D_y(\text{image}))), \text{divide}(D_{xx}(\text{image}), \text{absadd}(D_x(\text{image}), D_y(\text{image}))))))))$	$G_{\sigma=1} \sqrt{G_{\sigma=2} \sqrt{\sqrt{G_{\sigma=1}(D_y(I)) - \frac{D_{xx}(I)}{ D_x(I)+D_y(I) }}}}$	



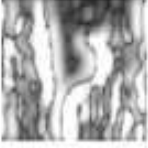
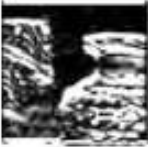
# Crossover



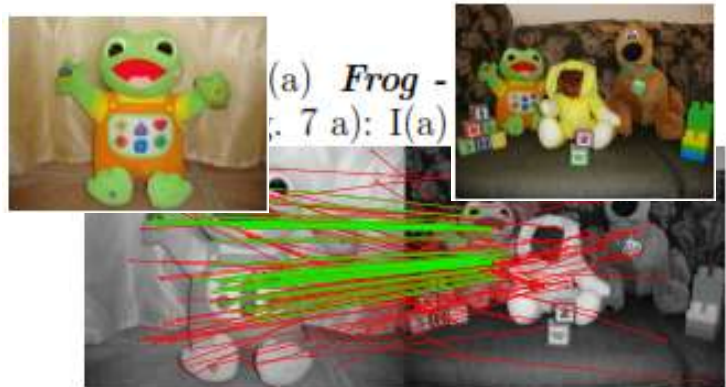
# Object recognition with GP

$RDGP_5$	7.4053	$Gauss1(\sqrt{Gauss2(\sqrt{\sqrt{subtract(\sqrt{Gauss1(D_y(image))}, divide(D_{xx}(image), absadd(D_x(image), D_y(image))))}}))})$	$G_{\sigma=1} \sqrt{G_{\sigma=2} \sqrt{\sqrt{G_{\sigma=1}(D_y(I)) - \frac{D_{xx}(I)}{ D_x(I) + D_y(I) }}}}$	
$RDGP_{11}$	7.3736	$Half(G_2(G_2(\sqrt{D_{xx}(Log(D_{xy}(image))))}))$	$\frac{G_{\sigma=2}(G_{\sigma=2} \sqrt{(D_{xx}(\log_2(D_{xy}(I))))})}{2}$	
$HILL_1$	6.2854	$add(D_{xx}(image), \sqrt{\sqrt{sqrt(D_x(image))}})$	$D_{xx}(I) + \sqrt{\sqrt{D_x(I)}}$	
$HILL_2$	6.1779	$add(D_y(image), \sqrt{Gauss1(\sqrt{Gauss2(D_{xx}(image))})})$	$D_{yy}(I) + \sqrt{G_{\sigma=1} \sqrt{G_{\sigma=2}(D_{xx}(I))}}$	
$HILL_3$	6.1389	$absdiff(D_y(image), subtract(D_{xy}(image), Log(Half(Gauss1(D_{xx}(image))))))$	$ D_y(I) - [D_{xy}(I) - \log(\frac{G_{\sigma=1}(D_{xx}(I))}{2})] $	

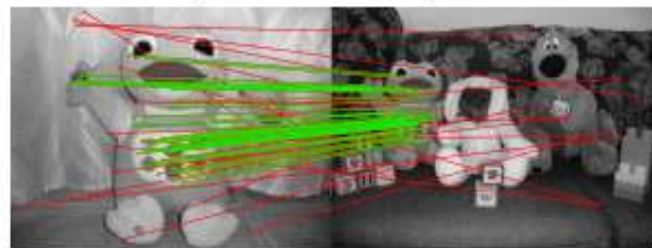
# Object recognition with GP

$HILL_2$	6.1779	$add(D_y(image), sqrt(Gauss1(sqrt(Gauss2(D_{xx}(image))))))$	$D_{yy}(I) + \sqrt{G_{\sigma=1} \sqrt{G_{\sigma=2}(D_{xx}(I))}}$	
$HILL_3$	6.1389	$absdif(D_y(image), subtract(D_{xy}(image), Log(Half(Gauss1(D_{xx}(image))))))$	$\left  D_y(I) - \left[ D_{xy}(I) - \log \left( \frac{G_{\sigma=1}(D_{xx}(I))}{2} \right) \right] \right $	
$HILL_4$	6.1345	$sqrt(Half(sqrt(Gauss2(D_{xx}(image))))))$	$\sqrt{\frac{\sqrt{G_{\sigma=2}(D_{xx}(I))}}{2}}$	
$HILL_5$	6.1245	$absadd(sqrt(Log(subtract(D_{xx}(image), Half(D_y(image))))), D_y(image))$	$\left  \left[ \sqrt{\log(D_{xx}(I) - \frac{D_y(I)}{2})} \right] + D_y(I) \right $	

# Object recognition with GP



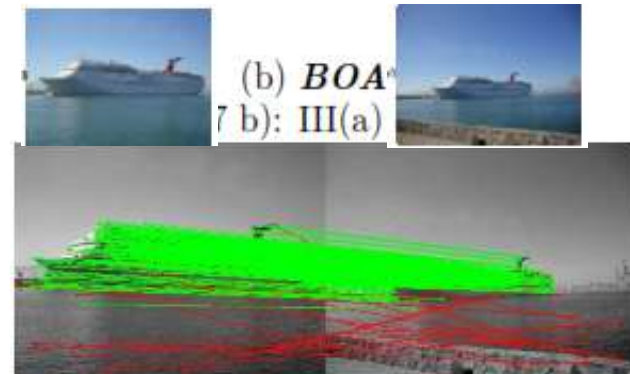
i) *SIFT* descriptor



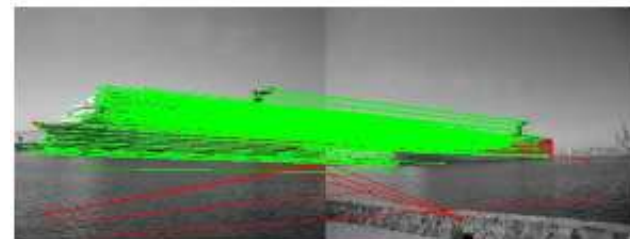
ii) *SIFT - RDGP<sub>2</sub>* descriptor



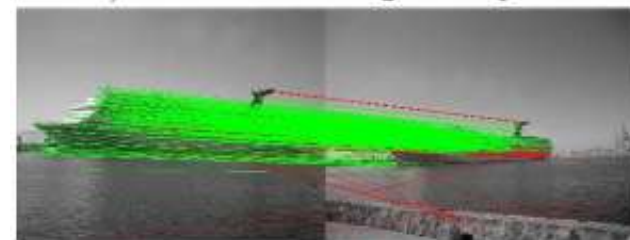
iii) *SIFT - HILL* descriptor



iv) *SIFT* descriptor



v) *SIFT - RDGP<sub>2</sub>* descriptor



vi) *SIFT - HILL* descriptor

# Object recognition with GP

- GP an effective approach to generate useful descriptors
- No handcraft work is required to obtain competitive descriptors
- Main drawback: interpretation of operators?, generality?

Questions?